

EXECUTIVE SUMMARY

Specialet omhandler en teoretisk tilgang til prisfastsættelse af syndikerede lån udstedt af højt gearede virksomheder¹. Med udgangspunkt i Leland's (1994) teori for prisfastsættelse af virksomhedsgæld udarbejdes en prisfastsættelsesmodel for sekventielt opdelt gæld. Modellen anvendes på et case study, hvorfra priserne for de underliggende trancher i ISS' gældsstruktur determineres. En sammenligning mellem de beregnede teoretisk priser og de egentlige observerede markedspriser indikerer, at senior tranchen indeholder en betydelig likviditetspræmie.

Som følge af likviditetskrisen er leveraged loan markedet blev utrolig hårdt ramt. Tidligere tiders ekstremt høje likviditet er blevet erstattet af et stort salgspres fra såvel banker som institutionelle investorer. Specielt market value CLOs og hedge funds har været tvunget til at mindske deres gearing og derved sælge ud af deres porteføljer. Dette har været med til at skabe en ubalance mellem udbud og efterspørgsel. Endvidere har den nuværende recession betydet, at priserne er faldet endnu mere. Lån, der tidligere blev handlet omkring kurs 100, kunne d. 31.12.2008 erhverves i omegn af kurs 60.

Fundamentet for en korrekt prisfastsættelse af leveraged loans beror på en dybdegående forståelse af markedets drivkræfter samt strukturen på de forskellige låntyper. Leveraged loans er typisk udstedt i forbindelse med, at et givent selskab opkøbes af en kapitalfond. Finansieringen af gælden ydes i et fællesskab af banker på enslydende vilkår. De ledende agentbanker har i den forbindelse tjent store fees på først at yde lånene for så efterfølgende at sælge store dele videre i en nøje struktureret syndikeringsproces. Dette har blandt andet ført til, at bankerne har været i hård konkurrence for at vinde mandater til at arrangere disse omfattende gældsstrukturer. Som følge heraf er gearingen og kompleksiteten af strukturerne på leveraged finance transaktioner blevet væsentligt forøget. Dette har været stærkt medvirkende til lånenes betydelige forringelse efter finanskrisen begyndelse.

¹ Fremover kaldet leveraged loans

PREFACE

This paper is a thesis for the M.Sc. in Economics and Business Administration majoring in Applied Economics and Finance, and Finance and Accounting - both at Copenhagen Business School. Given our specific majors, this thesis is concentrated around financial theory.

In the process of writing the thesis, we have relied greatly upon valuable insight into the leveraged loan market. Especially industry specialists Torben Skødeberg, Capital Four Management, and Mike Christiansen, Danske Merchant Capital, have been of invaluable help. Without access to their institutional knowledge, it would have been extremely difficult to write this thesis due to the privacy of the market. We would like to thank both of them very much for their contribution. Finally, we would like to thank our advisor David Lando for his very helpful and focused guidance. His assistance, especially in relation to the theoretical modelling, has been essential to the contribution provided in this thesis.

Data files for the analysis are provided electronically in the back of the paper.

Enjoy your read,

Jacob and Martin

Table of Contents

1. PROBLEM IDENTIFICATION.....	6
1.1. INTRODUCTION.....	6
1.2. MOTIVATION.....	7
1.3. RESEARCH QUESTIONS.....	8
1.4. METHODOLOGY.....	8
1.5. STRUCTURE OF THESIS.....	9
PART 1	11
2.1. FOUNDATION OF LOAN SYNDICATION.....	12
2.2. ISSUERS IN THE SYNDICATED LOAN MARKET.....	15
2.3. SYNDICATION STRATEGIES IN A LEVERAGED FINANCE AGREEMENT.....	16
2.4. SYNDICATION PROCESS IN AN UNDERWRITING DEAL.....	17
2.5. FEE STRUCTURE.....	20
2.6. SECONDARY MARKET TECHNIQUES.....	23
2.7. CHAPTER SUMMERY.....	24
3. SYNDICATED LOAN FACILITIES.....	25
3.1. THE CAPITAL STRUCTURE OF A LEVERAGED BUYOUT.....	25
3.2. LEVERAGED LOAN CHARACTERISTICS.....	26
3.2.1. Coupons - Floating Rate.....	26
3.2.2. Tenor - Maturity and Call-ability.....	26
3.2.3. Covenants - Early Warning.....	27
3.2.4. Security - Lien against Assets and Shares.....	28
3.2.5. Seniority - Corporate and Legal Ranking.....	28
3.2.6. Market and Information - Private Market.....	30
3.3. LEVERAGED LOANS VERSUS HIGH YIELD BONDS.....	31
3.4. STRUCTURES OF LEVERAGED LOANS.....	32
3.4.1. Structure of a Revolving Credit Line.....	32
3.4.2. Structure of a First Lien Term Loan - Amortising and Institutional.....	32
3.4.3. Structure of a Second Lien Term Loan.....	33
3.4.4. Structure of a Mezzanine Loan.....	34
3.4.5. Structure of a Payment-in-kind Loan.....	35
3.5. PRICING STANDARDS.....	35
3.6. CHAPTER SUMMARY.....	36

PART 2	38
4. CLO STRUCTURE.....	39
4.1. FOUNDATION OF A CLO	39
4.2. PURPOSE OF THE CLO.....	40
4.3. CREDIT ENHANCEMENT TECHNIQUES	42
4.4. HEDGE FUNDS.....	48
4.5. CHAPTER SUMMARY	50
PART 3	51
5. PRIMARY MARKET ANALYSIS.....	52
5.1. DEVELOPMENT IN THE PRIMARY MARKET.....	52
5.1.1. The CLO Issuance Comes to an End.....	54
5.2. THE IMPACT OF THE CREDIT CRISIS ON THE PRIMARY MARKET.....	56
5.3. CHAPTER SUMMARY	62
6. SECONDARY MARKET ANALYSIS	64
6.1. DEVELOPMENTS IN THE SECONDARY MARKET	64
6.2. THE IMPACT OF THE CREDIT CRISIS ON THE SECONDARY MARKET	66
6.2.1. Looking Into 2009.....	69
6.3. CHAPTER SUMMARY	71
PART 4	73
7.1 THE MERTON MODEL.....	74
7.2. THE LELAND MODEL.....	78
7.3. EXTENSION OF THE MODEL FRAMEWORK TO INCORPORATE SUBORDINATION	82
7.4. CHAPTER SUMMARY	85
8. THEORETICAL FRAMEWORK OF INPUT ESTIMATION	86
8.1. ESTIMATING ENTERPRISE VALUE.....	86
8.1.1. Relative Valuation Approach.....	87
8.2. ESTIMATING VOLATILITY	92
8.3. THE FRACTION α LOST TO BANKRUPTCY COSTS	93
8.4. CHAPTER SUMMARY	94
PART 5	95
9. INPUT ESTIMATION	96
9.1. THE ISS CASE	96

9.2 PEER GROUP ANALYSIS	96
9.3. ESTIMATION OF ENTERPRISE VALUE	98
9.4. ESTIMATION OF VOLATILITY	100
9.5. DETERMINATION OF BANKRUPTCY COSTS, TAX, AND RISK FREE RATE.....	102
9.6. CHAPTER SUMMARY	103
10. THE PRICING OF ISS'S DEBT	104
10.1 PRACTICAL FOUNDATION FOR INCONSISTENCIES.....	107
10.2. THEORETICAL FOUNDATION FOR INCONSISTENCIES.....	111
10.3 RECAPITULATION	112
11. CONCLUSION	114
12. REFERENCE LIST	118

1. PROBLEM IDENTIFICATION

1.1. INTRODUCTION

The high yield debt market has experienced a tremendous development in recent time. With the entrance of leveraged loans, below-investment-grade borrowers were offered an alternative to traditional high yield bonds. Leveraged loans soon became an important source of financing in particular for private equity funds, since the loans were launched through a syndication process as a private market transaction. The loan asset class rapidly became the most compelling alternative among high yield investors, due to the distinct features of the loans. Leveraged loans offered returns comparable to high yield bonds, but with a better degree of principal protection. This was due to their placement in the top part of the capital structure and in addition often secured by specific assets of the firm. Consequently, the rate of new loan issuance clearly outpaced the new issuance of public high yield bonds in the years preceding the credit crisis.

The leveraged loan market gained its acceptance during the days of large leveraged buyouts in the mid-1980s. While the U.S. leveraged loan market has gradually evolved ever since, its European counterpart did not get its breakthrough until the turn of the century. However, the European market has gone through an incredible growth since its origin, with the experience of the U.S. market at hand. In the very beginning, banks were the only investors purchasing the loans to achieve their high returns. Utilising a buy-and-hold strategy, the need for a secondary market was very limited.

However, the European loan market changed significantly with the entrance of institutional investors. Attracted by the combination of high yields and low correlation to other asset classes, portfolio managers had long desired the loan asset class. The CLO structure allowed institutional investors to enter the leveraged loan market. As a consequence of their more active investment strategies a secondary market developed - improving liquidity and transparency. In less than a decade, institutional investors substituted banks as the dominant market player.

Beginning in the summer of 2007, the European leveraged loan market was forced to its knees, as the credit crisis unfolded and the global economic slowdown became more apparent. The formerly busy primary market, characterized by large deals and elaborate structures, effectively closed with the disappearance of overwhelming liquidity. Secondary market prices, which had

previously traded in a narrow band around par value, all of a sudden began to decline sharply. With prices in steady decline and no evidence of deteriorating credit quality among highly leveraged companies, technical market conditions seemed to be the driving force. A comprehensive deleveraging process created a supply/demand imbalance in consequence of a broader credit system being severely overextended. The disproportionate amount of supply and a contracting investor base drove prices to a record low (McGaiven & Yang, 2009). As 2008 progressed, fundamental factors started to substitute the technical selling pressure and concerns of increasing underperforming credits became ever more real. Consequently, a new wave of falling prices accelerated in this total collapse of the leveraged loan market.

1.2. MOTIVATION

Our motivation for addressing the topic of leveraged loans is three-fold. Firstly, we want to investigate the forces behind the rapid development of the leverage loan market. In particular, in terms of supply and demand from private equity funds and high yield investors, respectively. Secondly, we find it interesting to study the underlying reasons for the market's downturn resulting from the onset of the credit crisis.

Thirdly, by observing leading leverage loan indexes trading below 60 as of 31/12/2008, loan spreads seem to more than compensate for the most pessimistic expectations to default and recovery rates. On the basis of this hypothesis, we wish to examine whether the market prices reflect the actual conditions of leveraged buyouts, or if a technical created supply/demand imbalance has distorted the price setting of leveraged loans.

1.3. RESEARCH QUESTIONS

In line with our motivation, this thesis addresses the following research question:

- Can market prices of leverage loans be supported from a theoretical point of view?

To answer our research question we need to examine the following areas:

- The characteristics of the leveraged loan market.
- How a CLO is structured to deal with leveraged loans.
- Institutional investors and their influence to leveraged loan market.
- Influences of the credit crisis to the leveraged loan market.
- A theoretical approach to pricing leveraged loans.
- An implementation of the model on a leveraged buyout case.

1.4. METHODOLOGY

In the initial stage of our research we observed that leverage loan indexes were trading historically low (McGaiven & Yang, 2009). On the basis of this observation, we formulated a hypothesis from which the thesis takes its starting point. The hypothesis is then translated into the main research question of the thesis.

The thesis evolves around the derivation of a model that prices the debt issued by leveraged buyouts. This is done to provide a qualified answer to whether market prices of leveraged loans correspond with the actual conditions of the issuing company. The model is developed on the basis of the theoretical framework provided by Leland (1994) for pricing corporate debt. We wish to extend his approach to incorporate subordination of debt.

In order to determine whether market prices can be supported from a theoretical point of view, the model is tested on a case study. In continuation the model's general applicability is discussed.

The ability to construct and subsequently apply a satisfying model for pricing leveraged loans relies on an in-depth understanding of the leverage loan market. Consequently, the first half of the thesis establishes a preliminary acquaintance with the overall dynamics of the leverage loan market.

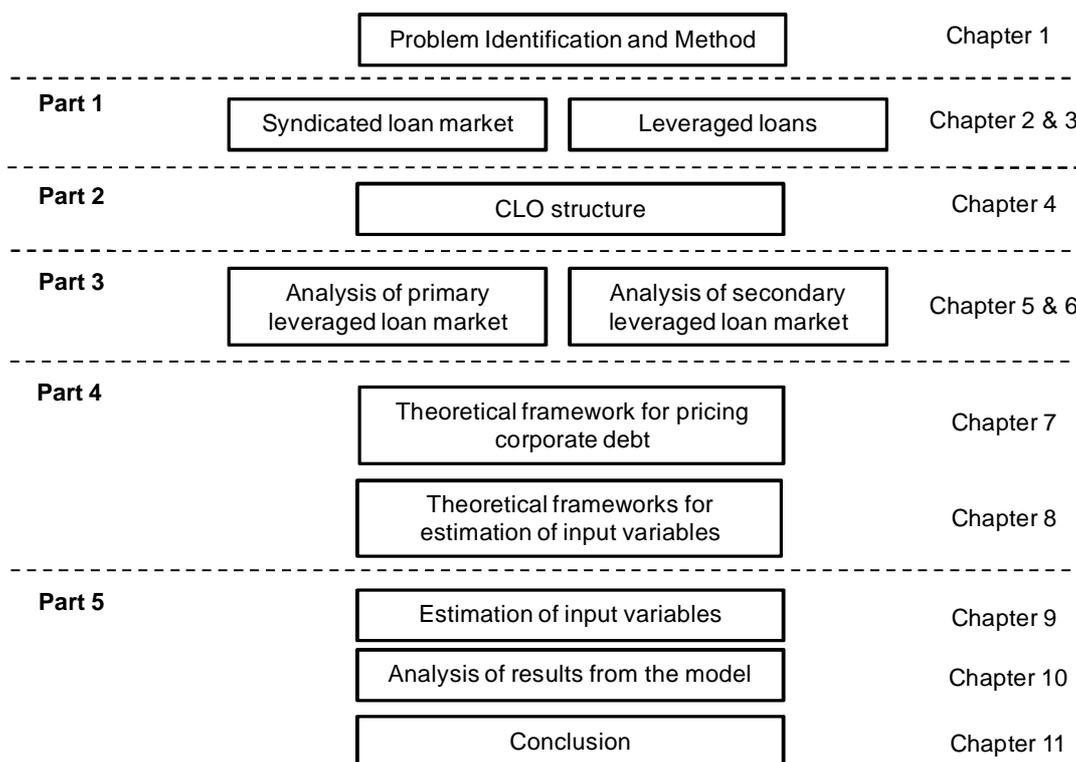
Furthermore, the ability to draw general conclusions relies on the quality of the data utilised throughout the study. To ensure a high quality we have therefore chosen to let the study rely

on both primary and secondary data. The availability of relevant and updated secondary data is to some degree limited, due to the privacy of the leverage loan market. Consequently, we have utilised primary approaches such as informal discussions with industry specialists. In this way, we have gathered unique knowledge essential for the study.

1.5. STRUCTURE OF THESIS

To provide a complete overview of the paper, this section highlights the structure of the thesis. So far the introduction has identified the problem area, the underlying motivation, and the methodology of the thesis. The following treatment of the research question is structured into five parts which are illustrated in figure 1.1.

Figure 1.1: Structure of thesis



Source: Own creation

Part 1 introduces the reader to the characteristics of the syndication process in which the loans are launched in the market. Furthermore, the distinct features of leveraged loans are examined. Insight into how leveraged loans differentiate from the more traditional high yield debt products provides the reader with a fundamental understanding of the underlying dynamics in the market.

Part 2 entails an introduction to the fundamental CLO structure through a detailed description of the various techniques applied. The purpose of this part is to provide the reader with a better understanding of the following analysis concerning the effects of the financial crisis on the leveraged loan market.

Part 3 provides an in-depth analysis of the primary and secondary leveraged loan market. On the basis of knowledge acquired from the former parts, the purpose of part three is to examine the actual effects of institutional investors entering the leveraged loan market. This includes an analysis of the rapid growth of the market preceding the credit crisis, followed by an analysis of how these investment vehicles have influenced the total collapse of the leveraged loan market as a result of the credit crisis.

Part 4 includes a presentation of a theoretical framework for pricing corporate debt issued in connection with leveraged buyouts. On the basis of Leland (1994) the model is derived to handle debt when tranced according to priority. Furthermore, the reader is introduced to frameworks for estimation of model input variables.

In Part 5 the theoretical framework is tested through a case study. Before an execution of the model can take place, the input variables must be carefully estimated. Subsequently, the results of the model are discussed. The purpose of this part is to determine whether market prices are in correspondence with theory. Lastly, the findings of the thesis are summarised in the conclusion.

PART 1

Part 1 includes chapter 2 and 3. The section provides the reader with an introduction to the basics of the syndicated loan market and leveraged loans, respectively. As in any other form of trading in the capital markets, it is simply necessary to understanding the conventions of the market and the fundamentals of the product in question. Without this preliminary step, we are not able to price the loans of ISS in our later case study.

	Problem Identification and Method	Chapter 1
Part 1	Syndicated loan market Leveraged loans	Chapter 2 & 3
Part 2	CLO structure	Chapter 4
Part 3	Analysis of primary leveraged loan market Analysis of secondary leveraged loan market	Chapter 5 & 6
Part 4	Theoretical framework for pricing corporate debt	Chapter 7
	Theoretical frameworks for estimation of input variables	Chapter 8
Part 5	Estimation of input variables	Chapter 9
	Analysis of results from the model	Chapter 10
	Conclusion	Chapter 11

2. THE ABCs OF LOAN SYNDICATION

In the following chapter the most fundamental aspects of the syndicated loan market will be presented. At first, a brief introduction to loan syndication takes place, followed by a description of the primary issuers and the different kinds of syndication strategies. Afterwards, the reader is provided with a more detailed explanation of a typical syndication process in an underwritten deal. This leads to a discussion of the associated fee structure and its major impacts on the syndicated leveraged loan market. Finally, the chapter includes a description of trading techniques applied in the secondary loan market.

The following chapter relies on Citigroup (2005), Gadanez (2004), LMA (2009), LMA (2009a), Taylor & Sansone (2006), Yang, Gupte & Lukatsky (2009). In addition to this personal communication with Christiansen (2009) and Skødeberg (2009).

2.1. FOUNDATION OF LOAN SYNDICATION

The European syndicated loan market has experienced a tremendous development since its origin. The syndicated loan market has evolved to become a dominant way for European companies to access the debt markets, since it initially began taking its shape when the euro was launched in 1999. Strongly influenced by the entrance of institutional investors, the loan market has increasingly changed from the old bilateral bank lending relationships towards a new world that is much more transaction and market orientated. Even though, the European syndicated loan market is still affected by banks remaining a dominate market player, the loan market is today much more comparable with the more traditional capital markets, such as bond and equity markets. From this perspective, it is hard not to acknowledge the loan market's impact on the European corporate lending culture. However, due to the nature of its privacy, the public in general are not familiar with the syndicated loan market and its associated lending procedure.

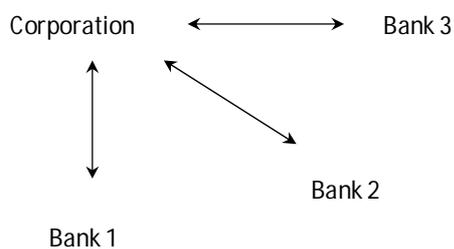
"A Syndicated loan is one that is provided by a group of lenders and is structured, arranged, and administered by one or several commercial or investment banks known as arrangers. They are less expensive and more efficient to administer than traditional bilateral, or individual, credit lines." (Yang et al, 2009:7)

Syndicated loan arrangements entail a group of lenders that provide funds for a borrower without joint liability. The creditors can roughly be divided into two groups consisting of (1) The arrangers and (2) Institutional investors along with participant banks. The borrower mandates one or several lead banks to arrange the syndication and initially underwrite the loan facility. The syndicate gets formed around these arrangers which are often the borrower's relationship banks. When the terms of the loan agreement is finalised the arrangers engage other participant banks and institutional investors willing to commit a part of the loan. The total number of participants may vary according to the size, complexity and pricing of the loan.

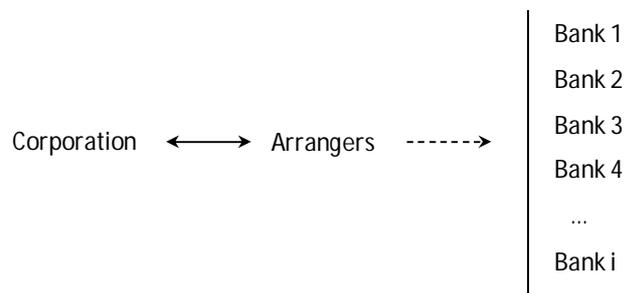
Loan syndication simplifies the borrowing process as the issuer uses a single loan agreement that covers the entire group of banks. Instead of entering a series of bilateral arrangements with each bank, a total loan agreement tends to be much more administratively efficient.

Figure 2.1: Bilateral Versus New Multilateral Lending

A. Traditional Bilateral Lending



B. New Multilateral Lending



Source: Own Construction

It can be argued that this new multilateral lending structure is based less on relationship lending than seen in the traditionally bank-client lending environment. Close relationships between the borrower and the bank have increasingly been replaced with a more transaction orientated lending form. Even though arranging banks continue to emphasize the importance of the overall profitability when committing a loan, it is hard to neglect the fact that the syndication process is a strong element of a more market driven distribution of corporate loans. In particular, banks and institutional investors participating in the subsequent syndication process commit their loan without any specific relationship to the borrower

Looking at the main advantages of establishing this new lending form, it is quite easy to understand why the market has experienced a rapid growth. All the major types of market participants (borrowers, banks and institutional investors) are in their own way apparent beneficiaries.

The borrower is typically able to access a larger pool of funding than otherwise available from the aggregate facilities offered by single banks, since all lenders share the same loan documentation. In addition, syndicated loan agreements allow for multiple loan tranches with different features and terms. Combined, these aspects provide the borrower with one of the largest and most flexible sources of funding available. In particular private equity funds have frequently utilised this more complete menu of financing options in connection with leveraged buyouts. In this respect, large sophisticated loan facilities are often required.

Similarly, the syndicated loan market offers several advantages to the banks according to their role in the syndicate. For the larger banks, operating as arrangers, syndication techniques enable them to offer efficient funding options which are effectively more competitive with the bond markets in connection with corporate finance businesses. Putting their expertise in loan origination at the borrower's disposal, allows for a substantial amount of fee collection due to structuring, underwriting and servicing large loans (see section 2.5). At the same time, the syndication process facilitates the exact desired amount of exposure on the arrangers' own balance sheets to be obtained. Effectively, syndication offers the potential for a broader dispersion of credit risk. This provides banks with an opportunity to diversify loan portfolios and avoid excessive single-name exposure in compliance with regulatory limits on risk concentration. Thus, the individual arranger is able to meet the borrower's demand for capital without having to undertake the entire loan. Furthermore, the relationship with the borrower is sustained in order to provide additional services to ongoing financial needs.

Finally, to the institutional investors, syndicated loans are simply another asset class which has proven attractive returns and low correlation to other asset classes. Thus, adding syndicated loans to a portfolio elevates returns and reduces volatility. At the same time, the low volatility allows for more confident use of leverage to increase returns. This has in particular been an important feature to highly leveraged investment vehicles such as CLOs and hedge funds (see part 4).

2.2. ISSUERS IN THE SYNDICATED LOAN MARKET

The syndicated loan market consists of two main borrower segments (1) The high-quality investment grade sector consisting of loans rated “BBB-” or higher, and (2) The high yield leveraged loans rated “BB+” or lower.

Investment grade issuers are usually large, established firms with little balance sheet leverage and strong profitability, which in most cases makes it less expensive to borrow in the public market via bonds or commercial papers than directly from banks. As a result, most of the syndication in the investment grade market is just plain-vanilla loans, typically unsecured revolving credit facilities, used to finance the backup of short-term commercial papers or to support the working capital. Moreover, many investment grade borrowers syndicate their loans themselves, simply using the arranger to craft documents and administer the process.

The issuers in the leveraged loan market are usually firms with non-investment grade ratings. Traditionally, companies with non-investment grade status were reserved for fallen angels, companies that were downgraded from investment grade as a result of earnings deterioration. In the past few years, the leveraged loan market has changed radically and is now heavily dominated by original-issuance from noninvestment grade companies taking action in leveraged transactions. Contrary to investment grade loans, syndicated leveraged loans support a greater number of different purposes; be it common corporate activity including working capital, capital expenditures and expansion, recapitalisation, or M&A activity. In particular private equity sponsors frequently make use of the syndicated loan market, to line up the right finance package, in connection with acquisitions of their targets.

In contrast to investment grade loans, leveraged loans are structurally much more complex and constitute various types of funding in the capital structure. Leveraged firms tend to have capital structures in which debt clearly exceeds equity. Typically, leveraged issuers have debt-to-EBITDA ratios of three or more (Citigroup, 2005). As a consequence of the riskier credit profiles, leveraged loans act as secured instruments with tightly drawn maintenance covenants in virtually all cases. This leaves leveraged loan investors first in line among creditors and with the ability to renegotiate the loan conditions before it becomes severely impaired. Finally, newly issued loans pricing at spread premiums in the area of LIBOR + 125 or higher, are characterised as leveraged loans (Citigroup, 2005).

The rest of the paper focuses strictly on the syndicated leveraged loan market which implies that the investment grade class will not be discussed any further.

2.3. SYNDICATION STRATEGIES IN A LEVERAGED FINANCE AGREEMENT

Globally there are three types of syndication arrangements when entering the leveraged loan market (1) Underwritten deals, (2) "Best-efforts" syndications, and (3) "Club deals". When choosing the optimal syndication strategy different factors, such as size and complexity of the transaction and time-to-close, should normally be taken into consideration. However, recent years extremely high liquidity has more or less obviated these aspects. Instead the market has developed some fairly flat frames depending on geographic location. In the European loan market underwritten deals are almost exclusively employed, whereas in the U.S the best-efforts approach is preferable.

The biggest difference between an underwritten deal and best-efforts is the amount of risk the arrangers undertake in connection with the syndication process. In an underwritten deal the arrangers guarantee the entire commitment before syndicating the loan to other banks and institutional investors. This essentially removes the market risk with respect to the borrower. As a result, the loan can be syndicated after it is closed, to the advantage of the borrower, in the sense that the funds are received more promptly. If the loan cannot be fully subscribed, this may entail some of the arrangers end up holding a larger position of the loan on their balance sheets than originally intended. Alternatively, they can choose to sell the loan at a discount sufficient to attract more participants.

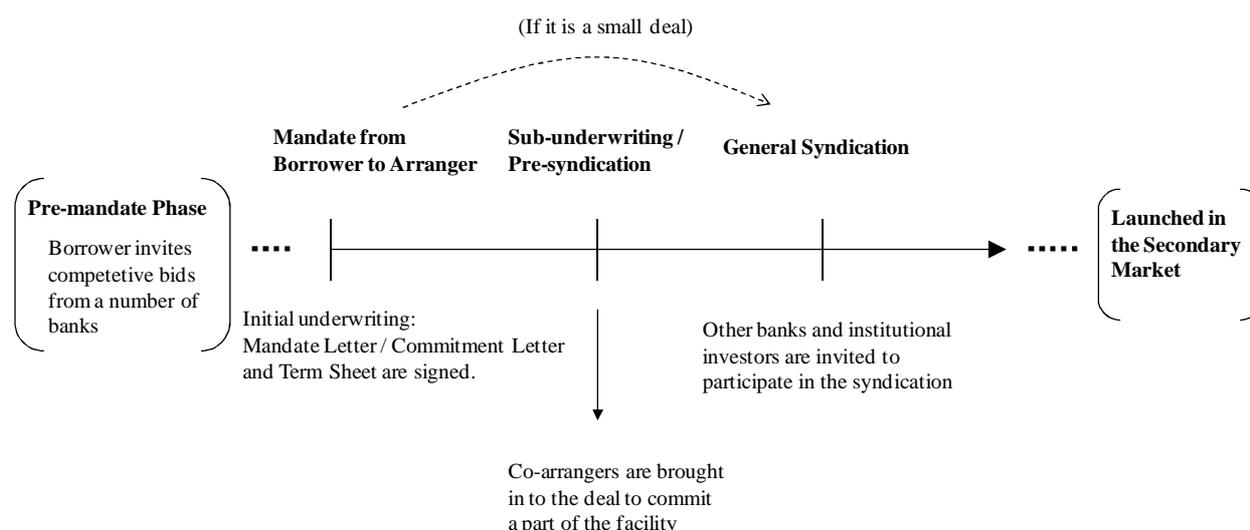
In contrast, a best-efforts arrangement implies that the loan must be syndicated prior to closing because the arrangers only commit to underwrite less than the full principal. For the remaining part it is up to the market to decide whether the credit is worth committing. Thus, under this approach the arrangers do not guarantee the borrower that they will be able to obtain the full funding at the desired terms. If the investor demand appears to be low, the arrangers need to assess whether certain changes in the term structure can make the deal more attractive. If the arrangers are not able to convince the market, they are in their right to cancel the syndication process.

2.4. SYNDICATION PROCESS IN AN UNDERWRITING DEAL

The structure of leveraged buyouts has in the past few years become increasingly complex and today the transactions often incorporate various types of debt instruments. Typically, syndication arrangements contain first and second lien as well mezzanine or high yield bonds. Consequently, the issuer might choose to practise a dual track approach to syndication whereby the lead arrangers handle the senior agreements while a specialist mezzanine fund concentrates on the subordinated part. However, in the following description of the syndication process, we take the approach as if the financing only includes a single loan agreement.

The primary syndication is normally performed in stages which can be divided into three phases consisting of (1) The credit facility is structured and lead arrangers are mandated to initially underwrite the deal, (2) Co-arrangers are brought in to participate in sub-underwriting, and (3) The general syndication process takes place. The role of the arrangers and the lenders is based on their relationships in the market and access to paper, respectively. On the arrangers' side, the players are determined by their track record indicating how well they can access capital in the market. On the lenders' side, it is about getting access to as many deals as possible. Depicted below is a typically timetable of the different phases in an underwritten deal.

Figure 2.2: Timetable of a Syndicated Loan (Underwritten Deal)



Source: Own Construction

The syndication process originates when a private equity fund has screened the market and found an interesting company to target. At first, a mandated lead arranger (MLA) needs to be appointed. This is done in an open process where several banks compete to win the mandate to structure and manage the syndication process. The borrower will choose the most convenient offer on the basis of the terms, under which the corresponding banks are able to put forward the necessary funding. The corresponding bank gets designated as lead arranger. A term sheet is attached to the mandate letter describing the conditions of the credit in terms of pricing, structure, collateral, covenants, etc. At the time the mandate letter and term sheet are signed by both parties the deal is then initially underwritten by the lead arranger.

In the formative years of the syndicated loan market, the prestigious job of being awarded as mandated lead arranger was handed out to a single bank - leaving only one agent to syndicate each loan. As the loan market has developed and the deals have grown in size, it is today common that more than one bank acts as lead arranger. For instance, in most of the larger deals, such as TDC and ISS, a group of banks have joined forces and offered a finance package together. These deals have simply proven too large for a single bank to undertake the entire commitment and carry the full underwriting risk.

When the mandate is awarded, the lead arrangers start planning the forthcoming syndication to a wider group of lenders. At first, one of the arrangers is appointed bookrunner which entails managing the entire syndication sales process and taking on the administrative tasks associated with the procedure of finding investors. This includes issuing invitations to potential investors, dissemination of information to banks, and providing the borrower information about the progress of the syndication.

Additionally, one of the lead arrangers starts to prepare an information memorandum that contains descriptive and financial information concerning the borrower. This includes the management financial projections. The recipients of the memorandum need to sign a confidentiality agreement, due to the non-public information composed in the sales material. If some of the potential investors act on the public side of the wall they will receive a public version of the memorandum excluding all confidential material. In continuation of the distributed sales material, the agents and the issuer's management will meet with prospective investors to present the company's business plan and prospects. The primary purpose of these

investor meetings is to give the borrower the opportunity to underpin the terms of the credit while simultaneously giving the investors a chance to meet the issuer's management in person.

Smaller transactions typically go directly from the arranger's initial underwriting into general syndication, while the primary sales process may be divided into two stages for the larger deals. In the latter, arrangers find it necessary to line up participant banks as sub-underwriters due to their inability or unwillingness to carry the entire underwriting risk themselves. This part of the syndication process is referred to as pre-syndication, because the co-arrangers commit a portion of the facility before it enters general syndication. In fact, the most successful lead arrangers have often sold off larger chunks even before initially underwriting the deal. The primary co-agent is designated as the joint lead arranger (JLA) - representing the bank that makes the largest sub-underwriting commitment.

When the potential sub-underwriting phase is completed the transaction goes into general syndication. In this stage, the syndication opens up to the institutional investors along with other banks. Commitments from new investors reduce the portion the underwriting banks end up holding on their own books.

At the time the syndication process is completed, the arrangers will allocate the facility among the committed investors. The announcement of this allocation is the point at which the primary syndication ends, and the loan will immediately break into secondary market trading (see section 2.6).

Additional administrative agents are regularly involved in order to realise the above described syndication process. The most important ones are the facility agent and the security agent. The facility agent constitutes the bank that administers the syndicate on a daily basis and acts as a focal point between the lenders and the borrower. This includes keeping track of syndicate members' commitments, repayments, secondary trades, etc. In this way the borrower avoids to deal with all the syndicate banks individually. If the syndicated loan contains a complex security package, a lender from the syndicate may be appointed as security agent. The role of the security agent is to oversee the management of the underlying security, in particular with regards to the intercreditor agreement and guarantees.

2.5. FEE STRUCTURE

Syndicated lending contains several different fees which are allocated in the multiple phases of syndication. The specific fee structure is part of commercial negotiations between the different parties participating in the deal. In general, the fee structure reflects the lender's position in the deal, be it MLA, JLA or participant. The higher the ranking within the syndicate, the greater is the share of underwriting fees. This reflects the greater amount of risk and labour entailed.

Following the structure of figure 2.3, the section will make a brief survey of the most commonly used fees in a syndication process. This will lead to a discussion of how the fee structure has played an essential role in recent years over-leveraging within leveraged finance transactions.

Figure 2.3: Fee Structure in a Syndicated Loan Agreement

Fee	Type	Remarks
Arrangement fee/ Underwriting fee	Upfront	Received and retained by the lead arrangers in return for structuring and underwriting the deal.
Reverse flex or Structural flex fees	Upfront	Paid to the lead arrangers if they are able to gain discounts in the market (spreads or cheaper tranches) compared to the initial agreement.
Upfront/ Participant fee	Upfront	Paid by the arrangers to the participants taking a part of the commitment
OID (Original issue discount)	Upfront	Spread enhancement borne by the issuer (alternative to upfront fees)
Agency fee	Per annum	Remuneration of the administrative bank's services

Source: Own Construction

Arrangement fees are one-time upfront fees paid by the issuer to the arrangers. An arrangement fee is paid for the service provided in terms of underwriting and arranging the debt structure. The amounts of these fees have in recent years increased substantially due to an increased size and complexity of buyout transaction. Consequently, taking part in the arrangement of leverage finance deals has gradually become more and more profitable for banks. Investment banks in particular have managed to skim fees on initial commitments which

are mostly sold off even before syndication takes place. This is referred to as back-to-back and has been a major money spinner in recent years' pleasant market conditions.

The increased institutional investor base has induced the concept of market flex pricing to become more standard in Europe. Market flex pricing refers to the possibility of arrangers changing the loan spreads during syndication. In this way, arrangers can adjust pricing to current liquidity levels. To attract more investors into buying the credit, arrangers have the possibility of raising spreads, or "flex up". In contrast, when liquidity is high and demand outstrips supply, arrangers may decrease spreads, or "reverse flex".

A structural flex occurs when the arranger adjusts the relative composition of tranches during syndication. This implies that the arrangers can adjust the size of the different tranches to reflect current liquidity levels. An arranger may change the overall loan structure by moving debt from the more expensive tranches to cheaper ones, and vice versa. For instance, in pleasant market conditions parts of the mezzanine debt may be replaced in favour of second lien or first lien.

In recent years' extraordinary high demand of leveraged loans, reverse flex and structural flex possibilities have become increasingly more important aspects from an arranger's point of view. This is due to the fact that arrangers partially profit from the potential discounts they successfully negotiate in the market. How the discounts exactly are allocated between the borrower and the arrangers respectively, are predetermined in the fee letter.

Upfront fees or participant fees are also one-time payments, but are paid by the arrangers - not the issuer - to the lenders. These fees are typically drawn from the arrangers' underwriting fees and paid as an incentive to bring lenders into the deal. As an example, an issuer may pay the arranger 2 % of the deal from where the arranger may pay participant banks 0.50 %. The latter will typically be tiered according to the size of the commitment and position in the deal.

Instead of paying participant banks and institutional investors upfront fees arrangers can chose to make a deal more attractive through an original issue discount (OID). An OID indicates that loans are sold at a discount to par. For instance, a loan may be issued at 99 to pay par. The OID, in this case, is said to be 100 bps. OIDs and upfront fees have many similarities, but are in fact structurally different. From a lenders perspective there is no difference, but for the issuer and arrangers the distinction is far more than a question of semantics. Upfront fees are generally

paid from the arrangers' underwriting fees, making them more issuer friendly, whereas an OID is generally borne by the issuer. If a deal includes a 1 % OID, the arranger would still receive its 2 % fee, but the issuer would only receive 99 cents for every dollar of loan sold. Consequently, an OID is a better deal for the arranger, making them more likely to appear in challenging markets.

A final notable fee is the agency fee which is an annual fee paid to the administrative agent for administering the loan. This entails distribution of interest payments to the syndication group, updating lender lists, and managing borrowings.

The recent years' hyper-liquid market conditions made it very attractive to be mandated as lead arranger. The possibility to earn a large arrangement fee from structuring and underwriting debt facilities, in a market with effectively no syndication risks, attracted an increasing number of banks' attention. As a result, banks forced each other to compose aggressive loan structures in their eagerness to win the mandate. The total amount of leverage was set at levels so high that the companies could just precisely service the debt at issuance. The global economy was expected to remain strong and companies were, in general, performing very well reflecting pleasant base case scenarios. In this way, the high gearing was effectively ignored by the perception of improving future earnings being sufficient to delever the capital structure. In addition, it is in hindsight obvious that the stress tests executed by the arrangers were not at all in compliance with worst case scenarios.

Furthermore, it became more frequent that banks' decisions to underwrite a deal went from traditional credit committees to syndication desks. Particularly investment banks let the decision depend on anticipated investor demand. Well aware that the loans were subsequently syndicated in the market, the arrangers were not exactly given much incentive to reconsider if the credit quality actually was acceptable.

Moreover, the flex fee structure gave the arrangers an additional motivation to make the loan agreements even more aggressive than initially intended. Earning additional fees by tightening the loan conditions encouraged the arrangers to lower the spreads and increase the inherent risk associated with the different tranches.

Finally, in the years when the leveraged loan market was at its height, greed had unfortunately become an important factor. Lots of bankers had huge bonus agreements dependent on the

amount of money they made within the leveraged finance business. Consequently, it could be very hard to turn down deals on the basis of their highly leveraged structures, knowing that they could easily be syndicated in a market filled with other greedy investors.

From this perspective, it is obvious that the syndication fee structure has been a crucial factor in the previous years over-leveraging within private equity owned companies. Lead banks tend to operate more like investment banks which strongly indicates a shift in the balance of interests. The role of whom to represent, when intermediating the competing interests of the lending group and the borrower, has blurred. Traditionally, the lead banks primarily represented the lending syndicate, but today arrangers tend to view the borrower as their client. Their first priority is now to fulfil the needs of the borrower in order to collect syndication fees and obtain recurring businesses. This might engage in opportunistic behaviour in the syndication process. A potential moral hazard problem arises due to information asymmetry between lead arrangers and participants. This entails that arrangers may retain a larger share of high-quality loans and a lower share of low-quality loans than would be retained if there were no information asymmetries.

2.6. SECONDARY MARKET TECHNIQUES

Following the primary syndication the loans start to trade in the secondary market. In the secondary market loan trades are typically done through dealer desks at the large underwriting banks and can be executed in one of two ways: (1) Assignments or (2) Participations.

Under an assignment there is a true sale between the two parties. This necessitate that the loan is effectively transferred to the new investor who receives interest and principal payments directly from the administrative agent. Consequently, a new financial obligation between the new lender and the borrower is designed. This typically requires the consent of the borrower and the agent.

On the contrary, participation is executed through an agreement between an existing lender and a participant. In a participation agreement the primary investor remains on the books as the official lender, and it is only the credit risk and the interest payments which are transferred to the buyer. In this way, the buyer becomes a participant in a share of the original lender's loan and the original loan contract does not need to be changed. Purchasing a loan through participation can be subject to a riskier way of trading. In the case where the original lender

becomes insolvent the participant does not have a direct claim on the loan. Instead the participant becomes a simple creditor of the lender and needs to wait for claims to be sorted out to collect on its participation.

2.7. CHAPTER SUMMERY

The chapter outlined the main characteristics of the syndicated loan market. The primary issuers are companies involved in a leveraged buyout. Through a syndicate of banks sharing the same loan agreement, private equity funds have been able to obtain the high amount of debt, utilised in recent years growing buyout transactions. In Europe, the syndication process is typically structured with lead arrangers initially underwriting the entire commitment, before participant banks along with institutional investors are invited to attend the loan syndicate. With recent years' pleasant market conditions effectively eliminating the syndication risk, it became very attractive to be mandated as lead arranger. In banks' eagerness to win the mandate loan structures became increasingly aggressive. Arrangers started to act more like investment banks and a potential moral hazard problem arose due to the information asymmetry between the lead arranger and other loan participants.

3. SYNDICATED LOAN FACILITIES

In the following chapter the focus is directed at the terms and structures of the most common types of leveraged loans. At first, we will take a closer look at a typical capital structure of a leveraged buyout company in order to determine which kind of debt instruments it contains. On the basis of the identified loan facilities, general loan characteristics will be presented. At last, the most important structural differences among the various types of loans will be pointed out.

The following chapter relies on Citigroup (2005), EHYA (2009), LMA (2009a), Smead (2005), Taylor & Sansone (2006), Yang, Gupte & Lukatsky (2009). In addition to this personal communication with Christiansen (2009) and Skødeberg (2009).

3.1. THE CAPITAL STRUCTURE OF A LEVERAGED BUYOUT

Private equity allows for radical changes in the capital structure of their targets due to the active and focused ownership. Their takeover is performed through the issuance of large amounts of debt in their target company in order to maximise the internal rate of return (IRR) on their committed funds. Depicted below is a typical capital structure for a leveraged buyout company.

Figure 3.1: Typical Capital Structure of a LBO (Pre-turmoil)

Capital Structure	% of EV
Senior Debt RCF Capex Acquisition TLA TLB TLC	45 - 55 %
Second Lien	0 - 10 %
Subordinated Mezzanine or High Yield	15 - 30 %
PIK	0 - 5 %
Equity	20 - 30 %

Source: Own Construction based on data from Cummings et al (2009)

As seen in figure 3.1, leveraged buyouts tend to have a complex financial structure consisting of a wide range of different debt products. The capital structure typically involves senior debt, second lien, and some kind of subordinated debt, such as mezzanine or high yield bonds and occasionally PIK notes.

3.2. LEVERAGED LOAN CHARACTERISTICS

Based on the illustrated capital structure above, the following section will give an exposition of the general terms of the most commonly seen leveraged loans.

3.2.1. Coupons - Floating Rate

Leveraged loans are structured with variable interest payments set by a pre-determined spread above a certain reference rate. In Europe the most frequently used benchmark rates are Libor and Euribor. To investors, floating rate structures work as a hedge against interest rate changes whereas borrowers, on the contrary, are exposed to changes in the reference rate. The loan agreement, typically, dictates the borrower to hedge against interest rate changes as an extreme vulnerability towards this risk is present.

3.2.2. Tenor - Maturity and Call-ability

Leveraged loans have maturities as short as one to five years for working capital revolvers while leveraged term loans normally mature in seven to ten years. Typically maturities are: TLA - 7 years, TLB - 8 years, TLC - 9 years, TLD – 10 years, etc. Carrying a floating rate generally makes the term loans callable at par. This entails that the issuer can repay their loans partially or in total at any time. Occasionally, some leveraged loans will have embedded non-call periods or call protection in them, requiring the issuer to pay a penalty premium for an early redemption. However, investors are exposed to a credit spread call option, since loans are usually callable immediately. The decision of the company to call will be based on an assessment of whether the company can access loan funds more cheaply due to improved market conditions, improvements in the company's creditworthiness, or if it simply generates excess cash. In recent years' pleasant market conditions, it has become increasingly popular to execute a dividend recap. This implies that the private equity firm withdraws capital and replaces it with additional debt in connection with a total refinancing.

3.2.3. Covenants - Early Warning

One of the most important aspects associated with leveraged loans is the comprehensive covenant package. Covenants are outlined in the legal credit agreement as series of restrictions that dictate how borrowers can operate and carry themselves financially. In this way, covenants limit a borrower's ability to increase credit risk beyond certain specific parameters. The size of the covenant package varies according to the borrower's financial risk at issue. In general, there are three primary types of loan covenants: (1) Affirmative, (2) Negative, and (3) Financial.

Affirmative covenants state what action the borrower must do to be in compliance with the loan. Most of these requirements are usually boilerplate such as paying taxes, complying with laws, and meeting financial obligations. Things the borrower would normally do without being instructed by a lender. Additionally, almost every credit agreement includes a more comprehensive disclosure covenant which requires the borrower to deliver annual audited and monthly unaudited financial statements. In this way, the lenders get the possibility to continuously monitor the performance of the borrower.

Negative covenants are structured and customised to limit some specific activities of the borrower according to its conditions. The most common restrictions are within no dividend payments, cross default, negative pledge, change of control, new investments, indebtedness, sale of assets, mergers and acquisitions, and guarantees.

Financial covenants are the most comprehensive types of covenants appearing in the loan agreement. These covenants impose minimum financial performance measures against the borrower. Covenant tests reveal the credit health of a borrower and allow lenders to take action in the event a borrower gets into credit trouble. Usually, financial covenants are tested every quarter. If a covenant is breached the lenders can require the loan to be repaid or agree to amend the covenant to keep the borrower in compliance with the credit agreement.

A credit agreement for a leveraged loan will typically contain up to four types of financial covenants depending on the credit risk of the borrower and market conditions at issue. Some of the most commonly used covenants are:

- Debt Coverage: Total debt/EBITDA
- Cash Flow Coverage: Cash flow/Net debt service
- Interest Coverage: EBITDA/Net finance charges
- Maximum CAPEX

3.2.4. Security - Lien against Assets and Shares

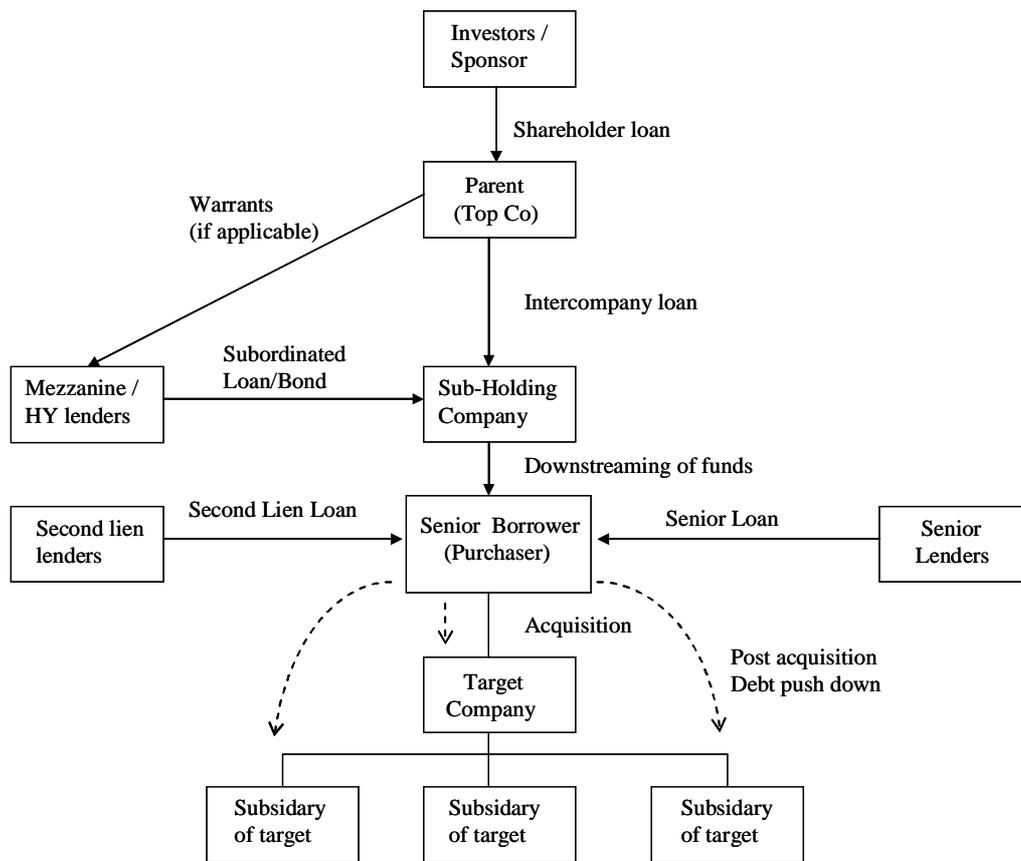
In general, leveraged loans are structured with a lien against all material assets of the borrower, which are relatively easy to pawn without being too costly. This usually includes receivables, inventory and cash, fixed assets and real property. In addition, the loan holders have a lien against all the shares of the operating company and material subsidiaries. The lien provides a claim on the control of the company including its assets, and gives secured loan holders several advantages over unsecured investors. In the event of a default, the secured lenders can take possession of the assets they claim to and sell or operate them for cash. Although, such a liquidation option is rarely used in practice, it does put the lender in an excellent position to maximise the recovery of principal in a restructuring.

3.2.5. Seniority - Corporate and Legal Ranking

As illustrated in figure 3.1 above, private equity owned companies tend to have complex capital structures containing several different products with different security. In this respect it is of great importance to ensure the right order of payments - particularly in connection to underperformance or default. This is usually achieved in two ways: (1) Structural and (2) Legal.

Depicted below, in a schematic drawing of a simplified leveraged debt structure, the private equity fund typically structures the transaction in accordance with the various investors' priority.

Figure 3.2: Simplified Debt Structure of a Leveraged Buyout



Source: Loan Market Association (2009a)

Starting from the bottom, potential dividends will be paid from the subsidiaries through the target company, gradually moving further up the corporate structure. As long as the company stays healthy the total amount of dividends will be large enough to please all levels of investors. If the company, on the other hand, experiences difficulties generating sufficient cash flows in order to pay all of its creditors, it will experience a default. In the event of a default the position of the “Senior Borrower” helps to preserve structural seniority for the senior lenders against the subordinated classes of debt. As a result, the senior lenders will be paid before potential excess cash will be allocated to the subordinated debt holders.

As illustrated in the figure, leveraged buyout transactions usually exercise a so-called debt push down in its post acquisition phase. This implies that different parts of the senior debt will be transferred to the subsidiaries in order to optimise the tax payments of the company. This is of course performed without changing the original structural priority within the group of lenders.

In a legal sense, intercreditor agreements and cross-guarantees, likewise, work to ensure lender rights. The intercreditor agreement outlines the ranking and specifies the priority of repayment to all lenders in the case of a default. Cross-guarantees similarly ensure that the varied operating units associated with a borrower guarantee their shares and assets as collateral. Thus, should one part trigger a default, all the associated companies will be equally responsible and their assets will be available for repayment.

3.2.6. Market and Information - Private Market

An important distinction between high yield bonds and leveraged loans is the underlying information material. Loans are strictly private securities, while high yield bonds are characterised as public instruments. Syndicated loans are originated and maintained based on information which often contains material of non-public character. Consequently, syndicate information shared between the issuer and the lender group is considered to be confidential. However, it is still possible to preserve the option to trade in the public securities market, although taking part in the loan market. As earlier mentioned, most arrangers will prepare a public version of an information memo in which private information, like projections, are omitted. These memos will be distributed to accounts which request to trade on the basis of public information. Furthermore, the arrangers will arrange a public version of the subsequent bank meeting.

One of the main reasons why leveraged buyouts are capable of obtaining such high degrees of leverage is the comprehensive due diligence material. The private equity fund hires a series of consultancies to perform different types of due diligences on its target working as a fixture of the carefully structured purchasing process. This involves exhaustive analyses of private information which is put at the private equity fund's disposal. On the basis of these in-depth analyses, potential investors get a much better understanding of the underlying business of the firm. This entails that lenders confidence in investing in the companies increase. On the contrary, the high yield bond investors have to be content with the public material available. This, of course, results in a much higher degree of uncertainty with respect to the insight of the performance of the company. Consequently, the due diligence process equips the investors in the private loan market with much better possibilities to predict how well the specific company will perform in the future. In general, this allows for a higher amount of leveraged compared to what investors typically are willing to accept.

3.3. LEVERAGED LOANS VERSUS HIGH YIELD BONDS

Although high yield bonds are not a product launched in the syndicated loan market, these are similar to leveraged loans in many ways, most importantly, they are both frequently used debt instruments in leveraged buyout transactions. However, despite their similarities, leveraged loans and high yield bonds do differ in several notable aspects regarding general terms and structures.

Leveraged loans carry floating interest rates with spreads quoted over a pre-determined reference rate, unlike traditional high yield bonds which often have fixed coupon payments. Setting interest payments as a floating rate coupon offers the investors an effectively built-in hedge against rising interest rates. Comparison of leveraged loans to high yield bonds also involves a trade-off between seniority and call-ability. The maturities of leveraged loans are typically seven to ten years, but due to the floating rate structure they are callable at any time. High yield bonds generally have longer maturities, on average 10 years, but on the other hand with investor friendly non-call provisions - typically the first five years. To offset this structural advantage, leveraged loans offer a senior secured position in the capital structure with more restrictive financial covenants (often bonds do not even have any). Consequently, defaulted secured loans consistently exhibit higher recovery rates than unsecured high yield bonds when utilised in the same transaction. However, nothing comes for free and the reduced risk inherent in the senior secured status results in a lower yield. A final notable difference is the information gap. Most leveraged loan investors enjoy access to more complete information due to the fact that they are traded on the basis of private information. High yield bond investors, on the other hand, must rely on the public information available.

To sum up, leveraged loans have evolved to be the fixed income asset class receiving the most investor attention. This is primarily due to their distinct features which neatly addresses two of the primary risks in fixed income investing: (1) Floating rate coupons help to mitigate interest rate risk, and (2) Protective covenants and senior position help mitigate credit risk. As a result, recent years' total new issuance of leveraged loans has by far outpaced the new issuance of public high yield bonds (EHYA, 2009).

3.4. STRUCTURES OF LEVERAGED LOANS

Moving on from the general terms of leveraged loans, the following part of the paper distinguishes between the individual loan types, providing a fundamental understanding of the specific loan structures. Understanding the basics of how the different loans work in practise is simply necessary from a potential investor's point of view.

3.4.1. Structure of a Revolving Credit Line

The revolving credit facility constitute a maximum aggregate amount of unfunded or partially funded commitments which can be drawn, repaid and re-drawn at the borrowers discretion until maturity. The structure of the facility resembles that of a credit card, with the exception that borrowers are charged an additional non-use facility fee on unused amounts. Revolving credit lines generally serve as liquidity facilities to fund working capital or capital expenditures. Maturities are in general either one year or in the range of three to five years. From an investor perspective revolvers are complicated to administer and fund due to the uncertain funding requirements and interest payments. Consequently, these loans are held almost entirely by traditional banks.

3.4.2. Structure of a First Lien Term Loan - Amortising and Institutional

In compliance with the demand of the two primary syndicated lender constituencies - banks and institutional investors – first lien loans are structured as either: (1) Amortising debt or (2) Institutional debt.

Amortising TLAs are typically structured as fully funded term loans with progressive repayment schedules running seven years or less. As the principal gets repaid, the borrower is unable to re-borrow the money, thereby differentiating them from the revolving credit facility. TLAs are primarily structured to be committed by traditional banks, due to the nature of accelerated amortisation payments. However, in some syndicated agreements, institutional investors have made commitments to the term loan A as a way to secure a larger portion of the institutional tranches.

In order to comply with the increased institutional investor demand, the structures of an increasing number of deals have been adjusted by entirely excluding the term loan A in favour of institutional tranches.

Most of the institutional debt consists of the first lien term loan facilities TLB and TLC. These tranches are jointly referred to as TLBs, because of their bullet payments and the fact that they are lined up behind TLAs. Institutional term loans possess a variety of structural differences compared to their less-liquid amortising counterparts. As the name implies, the tranches are structured primarily to favour the rising number of institutional investors in the form of more predictable funding requirements and interest payments. Maturities are, in general, gradually increasing, e.g. term loan B might be eight years, term loan C nine years, term loan D ten years, etc. These loans are priced higher than amortising term loans, because of the longer maturities and bullet repayment schedules. Leveraged loan investors usually expect to receive an additional 25 bps – 75 bps in coupon for each additional year until maturity. In practice, however, spreads of course reflect what the market is demanding in compensation for longer maturities.

3.4.3. Structure of a Second Lien Term Loan

Second lien has, since its entrance in the European loan market in 2004, joined the ranks of mezzanine as a financing alternative in private equity transactions. Second lien is a bi-product of the hyper-liquid market conditions of recent years'. It is a debt instrument used as an extension of the senior part of the capital structure on behalf of the more expensive subordinated debt. Consequently, second lien has always been more popular among borrowers than lenders. However, in years with plenty of liquidity, the utilisation of second lien has steadily grown. In fact, in the days preceding the credit crisis it became almost an intrinsic part of LBO financing.

Generally seen, second lien loans are structured much like the more common institutional first lien loans. They are typically: (1) Fully drawn, with (2) bullet maturities (3) floating rate coupons (4) secured lien on the assets of the borrower, and (5) share the same covenant package as first lien facilities. Although, second lien loans are really just another type of syndicated loan facility, they are rather more complex. The following points show the primary characteristics that set second lien term loans apart from the more liquid first liens:

- As the name implies a second lien on asset collateral of the borrower. First lien lenders are entitled to be paid in full before any distributions are made to second lien holders
- Larger coupons due to the higher risk
- Longer maturity, usually set a year after the first lien maturity date
- A waiver of certain rights in case of bankruptcy to the first lien lenders which are spelled out in the legal intercreditor agreement. E.g. first lien holders have the right to decide on disposition of shared collateral, including asset sales and bankruptcy exit financing.

3.4.4. Structure of a Mezzanine Loan

A mezzanine loan is a subordinated debt instrument that carries second-ranking security, or third-ranking security, if the capital structure includes second lien. Mezzanine fills the gap between senior debt and equity in the capital structure and is often referred to as "in between" debt. Mezzanine loans are typically used as an alternative to high yield bonds when companies do not have enough assets or current cash flow to qualify for additionally senior debt. Instead of lining up additional equity mezzanine debt serves to stretch out the total debt structure. Investors may be rewarded with yield enhancements such as warrants since mezzanine debt contains higher risk than senior secured loans. By incorporating "equity kickers" lenders are given a stake in the company's upside potential.

Historically, mezzanine has been an option for smaller transactions while the high yield bond market provided the subordinated financing for larger deals. Mezzanine debt was primarily a funding option when the financial needs were too small to qualify for the high yield bond market. However, mezzanine has in the past few years extended its reach to include larger deals, due to the hyper-liquid conditions in the leveraged loan market. Actually mezzanine has become a staple of LBO financings because of its relatively strong position in the subordinated part of the capital structure and its strong covenants². Furthermore, mezzanine loans have shorter non-call provision - typically one to three years - plus prepayment penalties at 102 bps and 101 bps in the subsequent years. This appeal to private equity funds with respect to exiting their targets. In these situations it will be cheaper to repay mezzanine than high yield bonds which generally have longer non-call periods embedded.

² Mezzanine typically carries the same financial covenants as senior bank loans though some facilities include a haircut on the covenants. Usually the looser level is around 10 %, placing the headroom in the 30 – 35 % area.

3.4.5. Structure of a Payment-in-kind Loan

Payment-in-kind loans (PIK) are debt instruments that pay investors in the form of additional principal rather than cash coupons. Like zero-coupon bonds, they give a company breathing space before having to make cash outlays at maturity. PIK loans are primarily utilised when the purchase price of the target exceeds leverage levels, up to which lenders are willing to provide additional senior, second lien, or mezzanine loans. As a result, PIK loans rank last in the capital structure and are used as a final substitute for equity. However, with the rich yields offered by PIK loans, the private equity fund has to be very diligent in assessing whether the cost of incorporating PIK loans does not outbalance the IRR on its equity investment.

3.5. PRICING STANDARDS

For many years, European loan prices were not very flexible and market-driven. The loan market had a well-established pricing standard from where most deals started out. The revolving credit facilities and TLAs usually began at a base rate (BR) + 225 bps, whereas each of the following institutional tranches were added an additional 50 bps - pricing TLB at BR + 275 bps and TLC at BR + 325 bps etc. While the pricing of the most senior tranches for many years were relatively fixed, the spreads of the more optional loans, such as second lien and mezzanine, have varied more widely. Second lien loans have usually been priced in the BR + 500 bps area, depending on the complexity and riskiness of the underlying credit. In the same way, the subordination of the mezzanine loans make the margin considerably higher than on senior loans - ranging anywhere from BR + 700 bps to BR + 1.100 bps. In addition to spread premiums, mezzanine debt may have warrants included to provide lenders an unlimited upside potential, should the issuer perform well. Deals with warrants of course carry lower spreads than those without.

Market flex pricing has become more standard in Europe, thanks to the increased institutional investor base. As previously mentioned, margin flex pricing allows the arranger to change spreads during syndication to adjust pricing to current liquidity levels. Consequently, in the years prior to the liquidity crunch, the vast majority of deals opened at prices slightly below older standards. In this period, borrowers profited from the hyper-liquid market conditions reducing the price levels on the senior tranches to BR + 200/250/300 bps. However, once the

financial crisis accelerated the opening spread levels went up and exceeded the old standards by far.

Although market-flex structure has become standard, pricing of leveraged loans is not yet fully driven by capital market forces. Contrary to the U.S., the European leveraged loan market is still affected by banks remaining a dominant market player. In the U.S., the pricing is exclusively determined by the predominant institutional investor appetite.

3.6. CHAPTER SUMMARY

The leveraged loan market consists of loans made for speculative grade borrowers. The vast majority of loans are senior secured floating rate papers which the issuer can prepay with little or no restrictions or fees. The senior loans are either denoted as first lien or second lien which reflects their security ranking in the capital structure and, thus, their claims on collateral. In addition, mezzanine loans have become an increasingly used LBO financing tool within the subordinated debt ranking. Due to the high credit risk incorporated in leveraged loans, the issuers are restricted by comprehensive covenant packages which state how loose they can operate and carry themselves financially. In addition, the various loan types are structured with different maturities, repayment schedules and pricing standards. All of which are summed up in table 3.3.

Table 3.3: General Terms of Debt Instruments Utilised in a Leveraged Buyout

	Senior	Second Lien	Mezzanine	High Yield	PIK Notes
Coupon	Floating rate	Floating rate	Floating rate	Fixed/Floating rate	Fixed/Floating rate
Tenor	<ul style="list-style-type: none"> • Usually 7, 8, 9 years for TLA, TLB, TLC respectively • Pre-payable without penalty • Repayable on change of control 	<ul style="list-style-type: none"> • 9.5 years • Typically pre-payable without penalty • Repayable on change of control 	<ul style="list-style-type: none"> • 10 years • No-call provision for one to three years, plus pre-payment penalties at 102, 101 in the subsequent years • Repayable on change of control 	<ul style="list-style-type: none"> • Typically 10-year • Not usually pre-payable for 5 years • Penalty of ½ coupon after year 5, diminishing thereafter to zero • 101 put on change of control 	<ul style="list-style-type: none"> • 11 years • Non-call protection, generally in first 3 - 4 years
Covenants	Broad range of financial and non-financial maintenance covenants. Headroom typically 20 – 25%	Same package of covenants as senior. Headroom typically 20 – 25%	Similar package of covenants to senior but headroom usually 10% higher	Incurrence covenants only	Incurrence same as HY but set one level higher
Security	Enjoys first pledge over all major subsidiaries through combination of structural / contractual subordination	Shares security with Senior; however, is second in line for repayment	Second/third (if structure has second lien)	None or second lien (subordinated)	None
Seniority	1st ranking	Ranks equal to Senior but above Mezzanine and High Yield	Ranks behind Senior and 2L but above any High Yield	Behind senior, 2L, Mezzanine	Ranks last
Repayments	<ul style="list-style-type: none"> • TLA amortising • Other tranches bullet repayments 	Bullet	Bullet	Bullet	Bullet
Market/ Information	<ul style="list-style-type: none"> • Private market • Information mostly private 	<ul style="list-style-type: none"> • Private market • Information mostly private 	<ul style="list-style-type: none"> • Private market • Information mostly private 	<ul style="list-style-type: none"> • Public market • Public information 	Public or Private
Spread	BR + 225 bps starting from term loan A adding an additionally 50 bps for each of the following tranches	BR + 500 bps	<ul style="list-style-type: none"> • A hybrid product often consisting yield enhancements such as warrants and PIKs. • Total margin ranging anywhere from BR + 700 bps to BR + 1100 bps 	7,5 - 12 %	8 - 15 %

Source: Own Construction

PART 2

Part 1 provided the reader with a basic understanding of the infrastructure in the syndicated loan market - including the terms and structures of the most commonly issued leveraged loans. In relation to this, we discussed some of the most important reasons for increased investor attention to the leveraged loan market. In particular, the fee structure's major impact on the behaviour of arranging banks and the distinct features differentiating leveraged loans from traditional high yield debt products were addressed.

Effectively, part 1 provides an analysis of the characteristics of the leveraged loan market.

Part 2 includes chapter 4 exclusively. The section presents the reader with an introduction to the fundamental CLO structure. This particular investment vehicle has fuelled the growth of the leveraged loan market, and it is therefore important to outline its operational approach. This is essentially achieved through a thorough examination of the various techniques utilised. The presentation of the CLO structure will facilitate the forthcoming analysis of the leveraged loan market with respect to understanding the impact of CLOs.

	Problem Identification and Method	Chapter 1			
Part 1	<table style="width: 100%; border-collapse: collapse;"> <tr> <td style="width: 50%; border: 1px solid black; text-align: center;">Syndicated loan market</td> <td style="width: 50%; border: 1px solid black; text-align: center;">Leveraged loans</td> </tr> </table>	Syndicated loan market	Leveraged loans	Chapter 2 & 3	
Syndicated loan market	Leveraged loans				
Part 2	CLO structure	Chapter 4			
Part 3	<table style="width: 100%; border-collapse: collapse;"> <tr> <td style="width: 50%; border: 1px solid black; text-align: center;">Analysis of primary leveraged loan market</td> <td style="width: 50%; border: 1px solid black; text-align: center;">Analysis of secondary leveraged loan market</td> </tr> </table>	Analysis of primary leveraged loan market	Analysis of secondary leveraged loan market	Chapter 5 & 6	
Analysis of primary leveraged loan market	Analysis of secondary leveraged loan market				
Part 4	<table style="width: 100%; border-collapse: collapse;"> <tr> <td style="width: 100%; border: 1px solid black; text-align: center;">Theoretical framework for pricing corporate debt</td> </tr> <tr> <td style="width: 100%; border: 1px solid black; text-align: center;">Theoretical frameworks for estimation of input variables</td> </tr> </table>	Theoretical framework for pricing corporate debt	Theoretical frameworks for estimation of input variables	Chapter 7 Chapter 8	
Theoretical framework for pricing corporate debt					
Theoretical frameworks for estimation of input variables					
Part 5	<table style="width: 100%; border-collapse: collapse;"> <tr> <td style="width: 100%; border: 1px solid black; text-align: center;">Estimation of input variables</td> </tr> <tr> <td style="width: 100%; border: 1px solid black; text-align: center;">Analysis of results from the model</td> </tr> <tr> <td style="width: 100%; border: 1px solid black; text-align: center;">Conclusion</td> </tr> </table>	Estimation of input variables	Analysis of results from the model	Conclusion	Chapter 9 Chapter 10 Chapter 11
Estimation of input variables					
Analysis of results from the model					
Conclusion					

4. CLO STRUCTURE

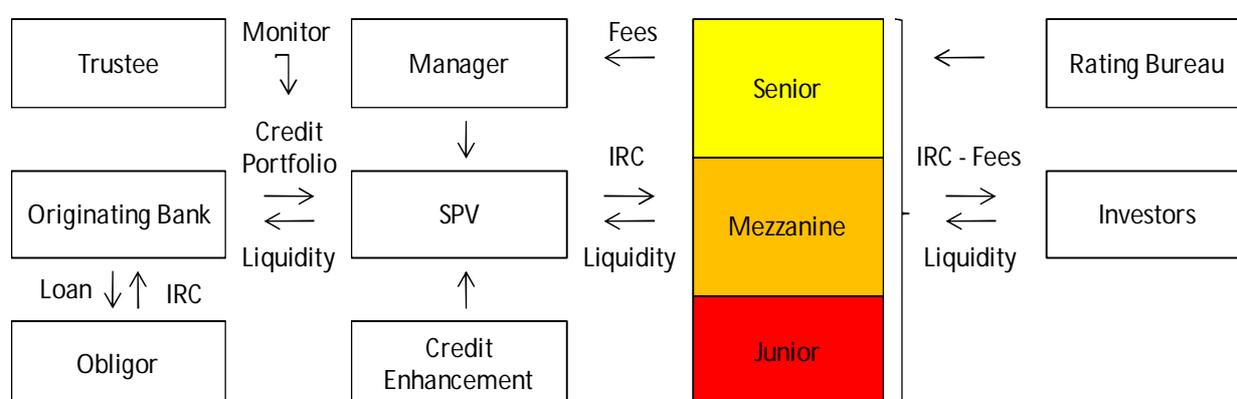
The following chapter focuses on the general structure of CLOs and the specific techniques utilised in the creation of the investment vehicle. To begin with, the structure and the different purposes the CLO seeks to serve are presented. This requires an introduction into securitisation and the usage of special purpose vehicles. Moreover, we examine the most commonly applied credit enhancement techniques. Finally, we present the concept of hedge fund which is an influential market participant. This makes their behaviour important to understand.

The following relies on Fabozzi & Kothari (2007), Lucas, Goodman & Fabozzi (2007), Plesner (2002), Plesner (2002a), Taylor & Sansone (2006). In addition to this personal communications with Christiansen (2009) and Skødeberg (2009).

4.1. FOUNDATION OF A CLO

In brief, a CLO is a special purpose vehicle (SPV) established to hold and manage a diversified pool of leveraged loans - referred to as collateral. The purchase of the collateral is financed by the issuance of a series of rated notes. These are sequentially tranches, with the higher rated tranches having a priority claim on the interest stream and increasingly higher levels of subordinated capital providing protection against losses in the collateral pool. The CLO is created as an arbitrage vehicle generating equity returns through the issuance of debt several times its equity contribution. Figure 4.1 illustrates a simplified CLO transaction.

Figure 4.1: Simplified CLO transaction



* IRC = Interest and Repayment minus Credit loss

Source: Own construction

The creation of a SPV plays a key role in the creation of a CLO as it enables asset based structuring to be applied to leveraged loans. The concept of securitisation concerns the issuance of securities with a direct connection to specific assets. In relation to CLOs, securitisation can be described as the process in which banks pool together the interests from leveraged loans in identifiable future cash flows. A SPV is created to which the claims on the future cash flows are transferred. The SPV serves the sole purpose of holding these financial claims and utilise the future cash flows to pay off investors over time. In fulfilling the role as originators, banks are effectively provided funding by selling a stream of cash flows that would otherwise be accrued to them. The originating bank which initially committed the loans, thereby obtains ongoing servicing fees associated with the transfer of interest payments - without burdening the capital adequacy requirements. In applying securitisation the originator is not affected by any risks associated with the underlying pool of assets, as it only distributes the cash flows generated by these.

Similarly, investors are not affected by any risks associated with the originator following the creation of the SPV as an independent legal entity. In order to obtain bankruptcy remoteness the interests of the investors must be safeguarded by a trustee in economical arms-length to the originator.

Effectively, banks achieve off-balance financing whereby regulatory capital restraints no longer limit their loan issuance. Simultaneously, they benefit from servicing the cash flows and maintaining the role as corporate relationship banks.

Before turning to the exposition of credit enhancement techniques the next section will outline the main reasons for the structuring of the investment vehicle.

4.2. PURPOSE OF THE CLO

The CLO concept was initially introduced with the purpose of providing banks regulatory capital relief. The creation of the balance sheet CLO facilitated banks in selling portions of their loan portfolio in the capital markets. According to Plesner (2002), banks rather easily disposed of the senior and mezzanine tranches, while they were often forced to retain the junior tranche due to its highly incorporated credit risk. As a consequence, the junior tranche was often referred to as equity.

The retention of the equity tranche soon resulted in banks issuing arbitrage CLOs in favour of the traditional balance sheet CLO. The investment objective of the new arbitrage CLO structure was to maximise excess spread, hence creating an arbitrage from the perspective of the equity investors³. To achieve the desired excess spread on the equity tranche an optimisation of the capital structure became crucial which led to an increased extent of applied credit enhancement. In outline credit enhancement refers to various techniques applied to mitigate risk with respect to expected as well as unexpected losses in the collateral pool. This allowed for more tranches in the capital structure to comply with different investor requirements and more leverage was obtained. In this way, a minimisation of total liability payments was achieved and returns on the reduced equity tranche increased to a degree which actually made the tranche desirable for investors.

The above mentioned structural shift from balance sheet to cash flow arbitrage highly increased the complexity of the CLO structure due to the credit enhancement and increased number of tranches. This complex structure was later criticised by loan market investors claiming that banks had forced the loans into the market. The accusations primarily concerned that banks had only been motivated by maximisation of their associated fees which gradually increased along with the complexity of the CLO structure. It is, however, worth remembering that the banks were only capable of selling what investors demanded. With the CLO structure enabling subordination of debt - resulting in tranches with different interest rates and credit ratings - different types of investor needs were addressed. In fact, the applied credit enhancement, which enabled investment-grade ratings to be obtained, was highly desirable to institutional investors due to the solvency burden associated with the lower rated leveraged loans.

In addition, institutional investors do not have departments specialised in the leverage loan business since leveraged loans only constitute a minor part of their total portfolio. Their limited expertise within the area is another important reason for institutional investors' considerable utilisation of CLOs. Investing directly in leveraged loans is a complicated and time consuming process which previously kept institutional investors out of the market. With the entrance of CLOs a golden opportunity to invest in diversified portfolios of leveraged loans arose. In this

³ For a numerical illustration of how excess spread is achieved see appendix A.

way, CLOs heavily impacted the rapidly increasing institutional investor base in the leveraged loan market.

To sum up, the CLO structure has provided banks the opportunity to achieve off-balance sheet financing while simultaneously generating fees from servicing the loans and remaining the corporate relationship bank. This highly motivated banks to apply asset based structuring as oppose to selling the loans directly to the investors. Likewise, the CLO structure has provided Institutional investors with a variety of opportunities to invest in leveraged loans with investment-grade ratings.

With the general purposes of the CLO in place, an introduction to how credit enhancement techniques allows for the fulfilment of these succeeds.

4.3. CREDIT ENHANCEMENT TECHNIQUES

Credit enhancement refers to the actions taken in order to mitigate the risk associated with default in the collateral pool. Credit enhancement is performed to achieve a certain target rating for the specific notes which implies different levels of enhancement for each class of securities. The three most commonly applied techniques are those of: (1) Excess spread, (2) Subordination, and (3) Overcollateralisation. While excess spread covers expected losses, unexpected losses are addressed by subordination and overcollateralisation.

Excess spread is generated when the weighted average rate of interest on the collateral is greater than the weighted average rate of interest on the liabilities. It is commonly known that lenders will charge a risk premium for credit risk which in the context of the CLO is the expected losses on the collateral pool. Excess spread is achieved to absorb the potential expected losses from the collateral pool. With senior note holders protected by the tranche with the lowest priority they are not exposed to the expected losses. This implies that the entire risk of the collateral pool is diverted to the most junior tranche, but so is the entire risk premium.

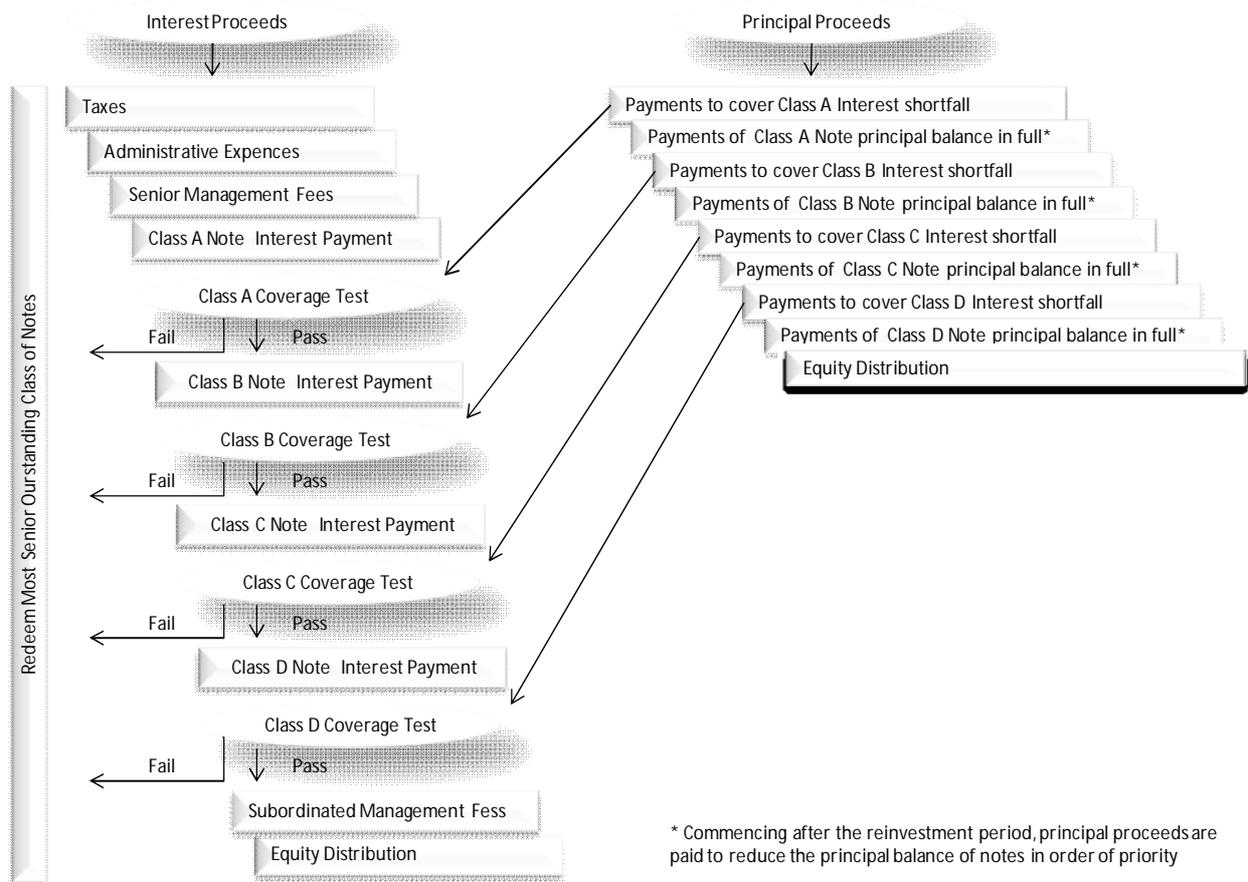
Subordination refers to the order of priority in the sequentially tranced notes. The most junior tranche is the first to suffer losses exceeding excess spread, and then moving upwards in the capital structure. With any tranche protected by subordinated debt, a higher credit rating than the actual collateral pool is achievable.

Overcollateralisation creates protection to investors by over-collateralizing the liabilities. The over-collateralized assets thereby become a subordinated share of the seller which is available

to offset losses in the collateral pool. Funding raised is simply backed by more collateral than the funding value.

Beginning with the payment waterfall, we now turn to look at how the above mentioned credit enhancement techniques function within the CLO, and how they are maintained.

Figure 4.2: Payment Waterfall



Source: Taylor & Sansone (2006)

The distribution of cash flows from the collateral pool is referred to as the payment waterfall. Cash flows generated by the collateral assets consist of two components: (1) Interest proceeds and (2) Principal proceeds. They are both addressed by the payment waterfall which dictates the priority of payments accruing to investors of different tranches. Initiating the waterfall of payment implies coverage of expenses to trustee fees, senior collateral management fees, and taxes. When these are covered, cash flows are directed to service debt payments - beginning with the senior most secure notes and descending in order of priority. Before descending to an underlying class of notes a coverage test is performed. The result of which will reveal whether

the collateral is performing within the rules set forth in the prospectus. Should the collateral value or cash flows be insufficient to pass a coverage test, distributions to investors below this point is terminated and diverted to redeem the most senior class of notes. Cash flows are continuously diverted until the test can be passed and, as such, the CLO structure is deleveraging as a self-correcting mechanism. This implies that any deterioration in the cash flows generated from the collateral will affect investors of the lowest prioritised tranche first. In addition, subordinated management fees are relinquished when failures to meet coverage tests occur in the capital structure.

The indenture, formulated upon the creation of the CLO, contains two types of covenants to protect note holders and maintain credit ratings on the notes. These are (1) Collateral coverage tests and (2) Portfolio quality tests.

Collateral coverage tests are designed to protect note holders against deterioration in the existing portfolio. This is performed to maintain the required minimum levels of credit enhancement and excess spread assigned to the specific ratings of the individual notes.

To ensure the credit enhancement whereby minimum asset coverage is achieved, an overcollateralisation test must be performed. The O/C test makes certain that each debt tranche is protected by a minimum level of par value asset coverage. The O/C ratio for a tranche is found by solving the following

$$O/C \text{ ratio} = \frac{\textit{Par value of collateral portfolio}}{\textit{(Par value of tranche + par value of all tranches senior to it)}}$$

The higher the ratio, the greater the protection to note holders. When performing the test the O/C ratio must be equal to or greater than the required minimum ratio which is referred to as the O/C trigger.

The excess spread is protected by an interest coverage test performed to ensure that adequate interest proceeds are available to pay interest due on the notes. The I/C ratio for a tranche is found by solving

$$I/C \text{ ratio} = \frac{(\text{Collateral coupon} - \text{senior fees and expenses})}{(\text{Specific tranche coupon} + \text{coupons from all tranches senior to it})}$$

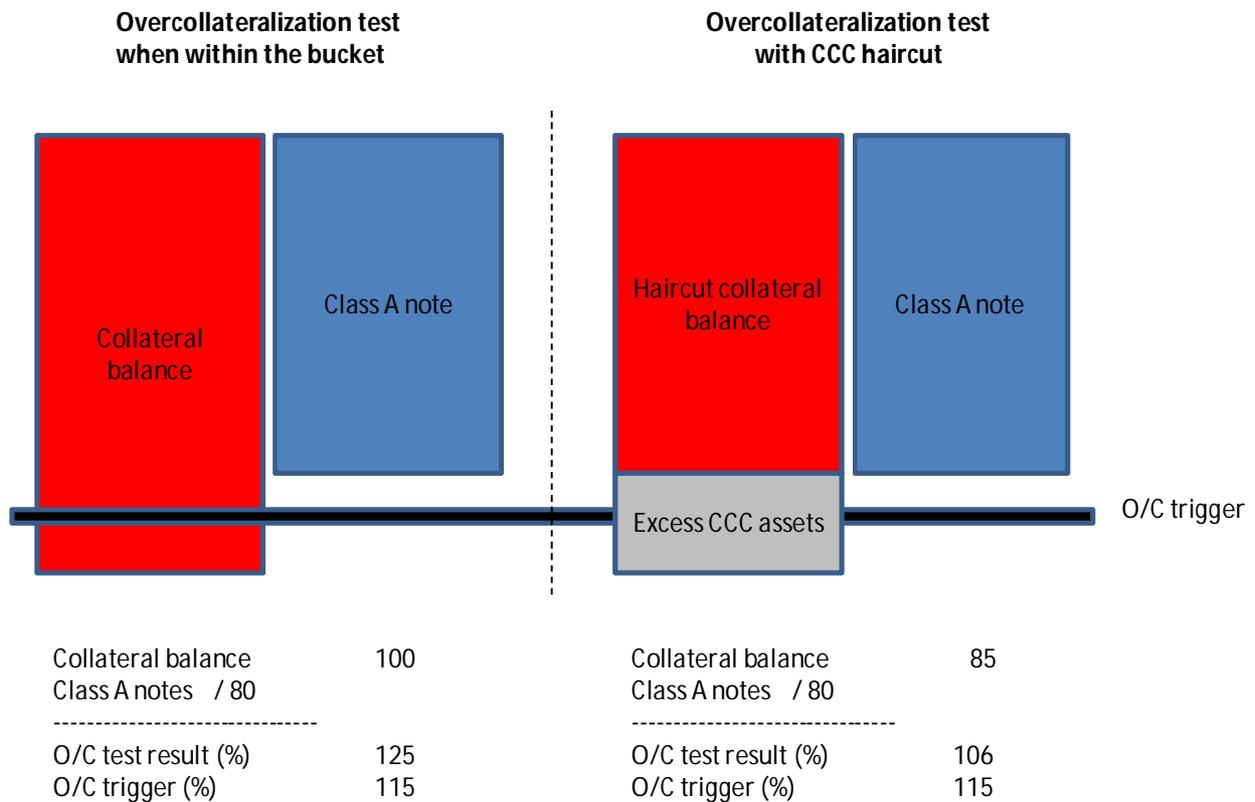
Once again, the higher the ratio the greater the protection is to the note holders. The interest coverage test for a tranche is passed if the I/C ratio is equal to or greater than the I/C trigger, which is the required minimum interest coverage ratio as specified in the indenture. If any of the above coverage tests are failed, actions are as described in the payment waterfall.

Quality tests are designed to ensure that certain criteria of the collateral pool are maintained on an ongoing basis. They are effectively investment restrictions assigned to maintain the initial credit rating of the specific note and therefore protect against deterioration in the credit quality of the portfolio. In general, asset quality tests constitute several individual tests, such as the minimum average credit rating test. This ensures that the weighted average rating of the collateral pool is at or above a specified level. Furthermore, tests for minimum levels of portfolio diversification typically limit the maximum percentage of collateral assets in the same industry or issued by the same obligor. Finally, quality tests only allow for a specific maximum amount of CCC-rated investments in the portfolio - often referred to as the CCC bucket.

Quality tests are typically described as maintain or improve tests - referring to how they merely restrict trading. Failure of meeting the requirement in a quality test will usually just result in subsequent trades being restricted to actions improving the collateral pool relative to the breached test. In contrast to coverage tests, quality tests do not directly influence the priority of the payment waterfall. However, failure to comply with the restrictions in a test can indirectly affect the waterfall by triggering a coverage test to fail as illustrated in the example below.

The CCC bucket in a CLO typically allows for a maximum of 5 – 7.5 percent CCC-rated assets. Any excess share of CCC rated assets will be mark-to-market which will inevitably influence the overcollateralisation test. Figure 4.3 illustrates how the overcollateralisation test is affected when the maximum level of the CCC bucket is breached.

Figure 4.3: Quality Test (CCC Bucket)



Source: Own Creation

In the first scenario, the amount of CCC assets in the portfolio is within the maximum limit defined in the indenture. In this case, the resulting ratio of the overcollateralisation test surpasses the pre-defined O/C trigger and passes the test. In the second scenario, the amount of CCC assets breaches the maximum limit resulting in the excess amount being marked to market. The collateral par value is still equal to 100. However, with an amount of 30 percent CCC assets in the portfolio and a bucket allowing for a maximum of only 5 percent, the excess of 25 percent is haircut at the market value, which in this case is set at 40 percent. Solving the haircut yields

$$\text{Haircut} = 25\% * (1 - 40\%) = 15\%$$

With a haircut of 15 percent the collateral balance then becomes $100 - 15 = 85$ to which the resulting ratio of the O/C test yields less than the O/C trigger, and thereby fails the test. Again, precautions are as prescribed in the payment waterfall.

In recent years, a new CLO structure has entered the market. The market value CLO resembles the above mentioned cash flow CLO in waterfall structure and ability to leverage the returns of the collateral. The separating point is the reliance on the market value of the portfolio to serve as protection for the debt holders. Where the traditional cash flow CLO structure depends on compliance with covenants concerning default rates and credit quality, the market value CLO have covenants restricting the minimum value of the collateral pool.

The market value of the collateral is "haircut" by assigning a pre-determined rate to the underlying collateral. The value of the haircut must be equal to or greater than the amount of debt. For example, if the haircut applied is 20 percent, the collateral is "haircut" by $1 - 0.2 = 0.8$. This implies that the market value must exceed 80 percent of the total value of debt. Should this criterion be violated, debt must be partially repaid in order to eliminate the deficiency, or in the worst case, fully liquidated.

For the market value CLOs and the cash flow CLOs, the issued notes are usually structured with a twelve to fifteen year maturity - although their life span is expected to be shorter. In general, a reinvestment period is incorporated during the first three to six years. In this period principal repayments on investments or proceeds from collateral sales are reinvested in new eligible collateral. When the reinvestment period has expired principal repayments on investments are applied to amortise the CLO note obligations, beginning with the most senior tranches and working down the capital structure. Equity investors will be distributed any principal proceeds only when all the notes have been repaid.

With an insight into how the CLO is structured and operates we are now able to identify the characteristics of the loan asset class which has made it ideally suited for securitisation before the onset of the credit crunch. These characteristics include:

- Par value erosion of the collateral pool in the event default has been very limited.
- Loan prices exhibited a profound stability enabling them to be reinvested at or near par in the event of early prepayment - thus avoiding collateral deterioration if only premium priced new collateral was available.
- The matching of floating-rate assets with floating-rate liabilities highly limits the exposure to interest rate risk.

- Returns on the loan asset class displayed low correlation with returns on practically any other asset class which created considerable diversification opportunities to aggregate investment portfolios.
- Finally, liquidity in the loan market progressively improved concurrently with the initiation of new CLOs, thereby creating a self-enforcing mechanism.

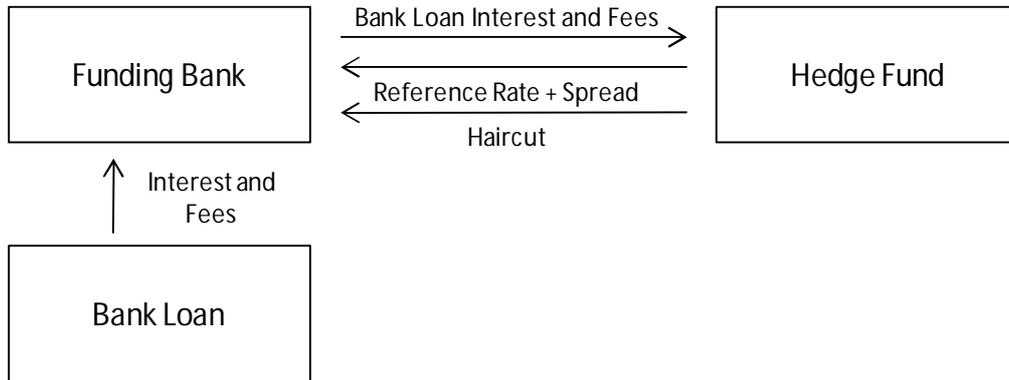
While leveraged loans have drawn the attention of CLOs, other structured vehicles have also taken the opportunity to invest in this asset class. In this leveraged loan market the most influential investment vehicle - next to the CLO - is the hedge fund. In the following, we will briefly introduce the methods utilised by hedge funds when investing in the leveraged loan market.

4.4. HEDGE FUNDS

Hedge funds involvement in the leverage loan market is attributable to bank loan total return swaps. Total return swaps (TRS) are derivative products offered by banks, allowing loan market participants to finance most types of bank loans including leveraged loans. Hedge funds use the TRS as a tool to obtain their desired leverage. In addition, they avoid the operational aspects of investing in bank loans.

Basically a bank loan TRS is a contract between two parties to exchange the return on a debt security for payments of a reference rate + spread. The funding bank purchases the bank loan and holds it directly on its balance sheet or places it in a special purpose entity. The hedge fund will then pay swap collateral to the funding bank - also known as the "haircut". The funding bank returns the haircut to the hedge fund when both parties have satisfied all of their obligations under the TRS. If the hedge fund fails to make any required payments under the TRS the funding bank is allowed to terminate all the swaps. In this respect, the haircut works as a safeguard to recover any amounts owed to the funding bank. The size of the haircut differs greatly, but the underlying methodologies for TRS usage are generally the same as presented in figure 4.4.

Figure 4.4: Bank Loan Total Return Swap



Source: Taylor & Sansone (2006)

In a simplified TRS transaction the funding bank of a 10.000.000 principal bank loan requires collateral in the amount of 1.000.000 equivalent of a 10 percent haircut. This implies that the hedge fund obtains 10 times leverage. The funding bank pays the hedge fund interest and potential fees received on the initial bank loan. In return the hedge fund pays a reference rate plus a spread which is calculated on the purchase cost of the bank loan. The bank loan spread exceeds the swap financing spread and provides the hedge fund with a positive net interest under the swap. This is, of course, only true so long as the bank loan is paying interest. The funding bank earns a net spread over its funding cost by simply passing through all interest and fees paid on the bank loan. This consists of the difference between the swap funding cost and its own funding cost of the loan.

The funding bank will pay the realised capital gains to the hedge fund, at the time the loan is sold or repaid. Realised losses, on the contrary, will be paid by the counterparty to the funding bank. Consequently, realised appreciation or depreciation can be highly influential on the total returns effectively obtained by the hedge fund.

Since TRS' are mark-to market products it is an important requirement that daily market prices for the underlying loans can be obtained. This feature makes syndicated leveraged loans - where secondary market pricing is widely available - some of the most suitable bank loans to finance through TRS'.

4.5. CHAPTER SUMMARY

To achieve off-balance financing, banks have provided institutional investors various investment vehicles which allowed them to enter the leverage loan market. These investment vehicles primarily constitute cash flow and market value CLOs along with hedge funds. The CLOs are structured around a payment waterfall which insures that interest and principal repayments occur in compliance with the priority of the different debt holders. To protect the debt holders, the cash flow CLO structure relies on default rates and credit quality of the underlying collateral. Market value CLOs and hedge funds on the other hand, depend on the market value of the underlying assets to serve as protection. Preceding the credit crisis, several characteristics of leveraged loans made them ideal investment objectives for institutional investment vehicles. Especially with respect to securitisation which allowed banks to transfer the credit risk of the financial assets to loan market investors. Simultaneously, they maintained the role as relationship bank. In turn, the loan market investors circumvented the risk to the originator due to the utilisation of a bankruptcy remote SPV.

PART 3

Part 2 provided the reader with a fundamental presentation of the CLO and the overall purposes it seeks to serve. In relation to this, the different techniques applied in order to achieve these purposes were presented. Provided with an insight into the operational approach of a CLO, an understanding of different factors driving the leveraged loan market was achieved. This enables the reader to better understand the following analysis concerning the effects of the financial crisis to the leveraged loan market.

All in all, part 2 provides an analysis of how a CLO is structured to deal with leveraged loans.

Part 3 includes chapters 5 and 6. The section provides an in-depth analysis of the primary and secondary leveraged loan market. On the basis of the obtained knowledge about the structure and the underlying techniques of institutional investment vehicles, we now wish to examine the actual affects of institutional investors entering the leveraged loan market. At first, this is performed to understand the rapid growth of the market in the years preceding the credit crisis. Subsequently, we attempt to facilitate the comprehension of the complex matters by which these investment vehicles have significantly influenced the total collapse of the leveraged loan market as a result of the credit crisis.

	Problem Identification and Method	Chapter 1
Part 1	<div style="border: 1px solid black; padding: 5px; width: 45%;">Syndicated loan market</div> <div style="border: 1px solid black; padding: 5px; width: 45%;">Leveraged loans</div>	Chapter 2 & 3
Part 2	CLO structure	Chapter 4
Part 3	<div style="border: 1px solid black; padding: 5px; width: 45%;">Analysis of primary leveraged loan market</div> <div style="border: 1px solid black; padding: 5px; width: 45%;">Analysis of secondary leveraged loan market</div>	Chapter 5 & 6
Part 4	Theoretical framework for pricing corporate debt	Chapter 7
	Theoretical frameworks for estimation of input variables	Chapter 8
Part 5	Estimation of input variables	Chapter 9
	Analysis of results from the model	Chapter 10
	Conclusion	Chapter 11

5. PRIMARY MARKET ANALYSIS

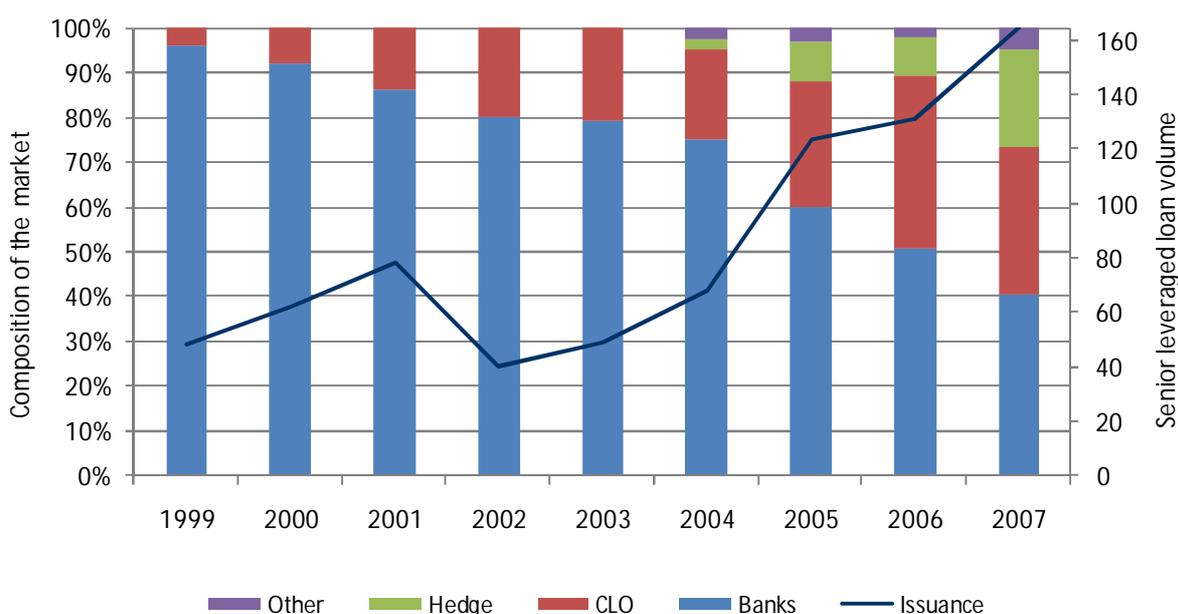
This chapter will study the actual effects of institutional investment vehicles in the European primary leveraged loan market. This includes an examination of the underlying spreads which have been one of the main motives for the issuance of CLOs. In the following, the reader is presented with a thorough analysis of how the financial crisis has affected the primary leveraged loan market. This entails an analysis of the development in loan issuance, debt and equity contributions, purchase price multiples, syndication style, debt structures, and finally, spreads.

The following relies on McGaiven (2009), McGaiven (2009a), McGaiven & Yang (2009), . In addition to this personal communication with Christiansen (2009) and Skødeberg (2009).

5.1. DEVELOPMENT IN THE PRIMARY MARKET

During the past decade the European leveraged loan market has raised capital like never witnessed before. The capital has been sourced from a variety of different lenders whom in entering the market brought along different investment styles to the asset class. Most profoundly was the advent of CLOs who began to share the market with traditional banks. Figure 5.1 illustrates the increasing share of primary issuance contributable to different investor groups.

Figure 5.1: Primary Market Composition and Leveraged Loan Volume



Source: Own Creation Based on Data from Cummings et al (2009)

The European leveraged loan market was introduced to CLOs in 1999. Throughout the year three institutional investment vehicles entered the market, all utilising cash flow CLOs to fund investments in senior and mezzanine leveraged loans. The cash flow CLO applied a buy and hold investment style which was similar to that utilised by banks. In their first year institutional investors ended up accounting for 4.2% of the primary market.

During the following years, the total number of investors more than doubled compared to 1999 figures. Leveraged loan issuance in the year of 2001 was close to € 80 billion, of which institutional investors had increased their share of the primary market to 13.9% - more than a treble of the 1999 share. Cash flow CLOs remained the preferred investment vehicle, maintaining the buy and hold investment style.

The year 2002 brought along the collapse of the telecom and cable industries, which in recent years had influenced the debt markets tremendously. The following period, characterised by increasing defaults, brought an end to the bull-run. Consequently, European leveraged loan issuance was reduced by nearly 50 percent of the 2001 record high €78 billion issuance. However, the overall commitment of the institutional investors proved consistent as their total market share reached new levels of 20%.

The crisis occurring in 2002 would prove to be of little significance to the loan market whose upturn was fast reverted. Throughout 2004, the increasing private equity activity drove volume back to €67.8 billion of which funds contributed 25%. The leverage loan market attracted more and more attention and new types of investment vehicles made their entry in the market. In recognition of the increasingly growing institutional appetite, the way deals were structured changed. This was reflected in the increasing availability of the more fund-friendly term loan B/C.

2005 became the year in which the European leveraged loan market was truly revolutionised. Leveraged loan issuance increased by nearly 100 percent to reach an astronomic €123.5 billion. The ability of institutional investors to raise funding seemed without limitations as their total market share hit 40%. The number of vehicles under their active management now accounted for 126 provided by 53 different funds.

The evolution occurring during 2005 did not continue in 2006, which was characterised as a year of consolidation. The market remained strong throughout the year, and while increases of

recent years were unobtainable, primary volume did rise to €131.3 billion. The involvement of institutional investors, however, increased undauntedly and now accounted for 49.3% of the primary market.

With institutional investors gradually appropriating the position as the majority player over banks, 2007 appeared to be the year in which the European loan market would eventually carry similar characteristics to that of the more developed U.S. market. For the 12 months ending June 30, 2007, institutional investors accounted for 54.6% of new issuance while the involvement of banks fell to an all-time low of 40.4%.

Furthermore, 2007 became the year in which CLOs finally lost their momentum as institutional investors began to diversify investment strategies. This was predominantly attributable to hedge funds becoming more desirable due to their somewhat more aggressive approach in which capital arbitrage opportunities are sought.

Most influential, however, was the appearance of the credit crunch which hit the entire financial system during the summer of 2007, and sent the European loan market into an abrupt stand still. Banks and loan funds resigned as easy financing vanished and leveraged unwound. The leveraged lending business experienced a fundamental change as recent years' heavy demand for leveraged loans all of a sudden disappeared.

CLOs were first in line to experience the new reality. With the onset of the credit crunch institutional investors no longer desired structured finance products, making it extremely difficult to raise new funds. With a share of leveraged loans funded by CLOs at 40% LTM, ending June 2007, this obviously led to a massive hole in the investor base.

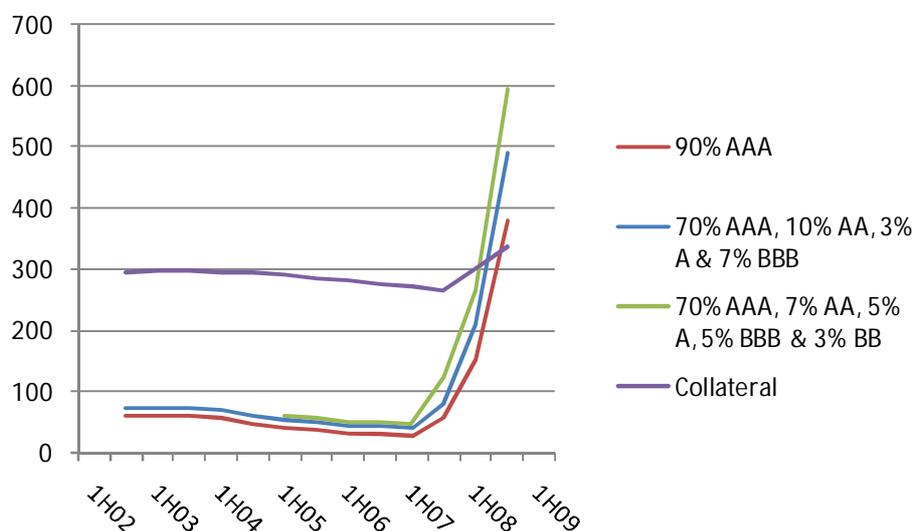
In addition, all funds structured to utilise mark-to-market approaches struggled significantly. Just as market value CLOs had begun to gain momentum, they were severely influenced by the steep decline in secondary market prices. This resulted in market value CLO managers exclusively focusing on their existing portfolio in an attempt to avert a looming liquidation. This left no spare attention to new fund issues.

5.1.1. The CLO Issuance Comes to an End

As earlier mentioned the cash flow CLO is an investment vehicle structured to generate arbitrage. Basically, this arbitrage is achieved by taking advantage of the difference between the payments associated with the collateral pool and the corresponding liabilities. In order to

explain the rapid growth in new CLO issuance and its sudden disappearance, we will examine the evolution in collateral spreads and liability spreads, respectively.

Figure 5.2: Average cost of CLO funding

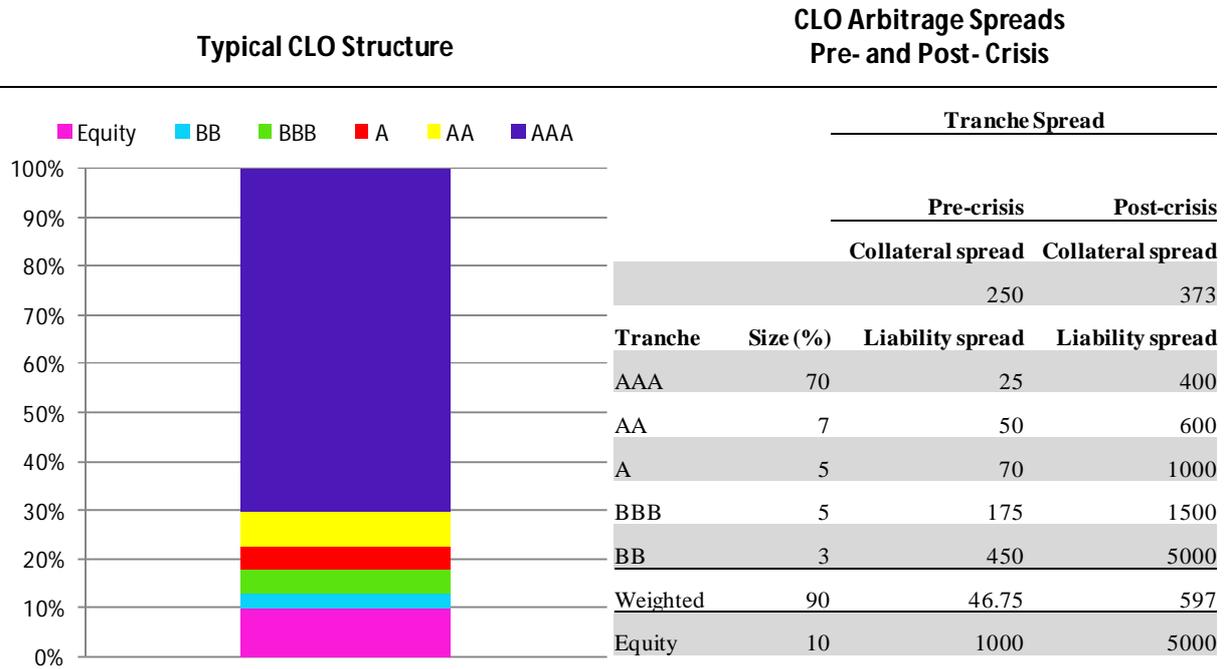


Source: Standard & Poors (Lukatsky, 2009)

The average cost of funding obtained in the period 2002 – 2007 reached remarkably low figures as the liquidity steadily increased in the leveraged loan market. In this period the average cost of funding went from around E + 80 bps to a record low of E + 43 bps. Even though collateral spreads naturally were falling as well, due to the higher degree of liquidity in the market, they clearly outstripped liability spreads. Thus, a significant arbitrage opportunity was created.

With the onset of the credit crises came along a severe increase in the average cost of funding. In December 2007 liability spreads reached E + 120 bps, up from the E + 43 bps registered merely 6 month earlier. As the crisis worsened so did the average cost of funding and by March 2008 liability spreads reached E + 181 bps. While collateral spreads naturally rose as well, they far from kept pace with the liability spreads. This inevitably meant that during these times arbitrage opportunities of the institutional investment vehicles all of a sudden disappeared. This is exemplified when looking at liability spreads compared to collateral spreads from before the crisis.

Figure 5.3: CLO Arbitrage Spreads



Source: Own Creation Based on Data from Eyerman (2009)

Looking at the required return of the individual tranches in a typical CLO structure, we find that the weighted average cost of funding constituted a spread of E + 46.75 bps preceding the credit crisis. With collateral assets paying E + 250 bps, an arbitrage of E + 203.25 bps was achieved; this offering a return of more than 20 percent to equity investors, which clearly exceeded their anticipated demand at 10 percent.

Considering the returns on the collateral pool under the conditions given at end year 2008, the weighted average return required by investors was E + 597 bps. In addition, equity investors required a weighted average return of E + 500 bps. With collateral spreads at E + 337 it is obvious that the arbitrage opportunities have broken as a consequence of the credit crisis. With the significant increase in liability spreads within all of the individual tranches, the collateral spread cannot even fulfill the requirements of the tranches senior to equity. This provides the answer to the abrupt decline in CLO issuance.

5.2. THE IMPACT OF THE CREDIT CRISIS ON THE PRIMARY MARKET

In the absence of institutional investors, the volume of the deal flow was suddenly dependent on banks' appetite for leveraged loans. Banks were once again set to be the dominant player in

the leveraged loan market, similar to the period preceding the blossoming private equity days - although at this time at a far more limited level than earlier seen.

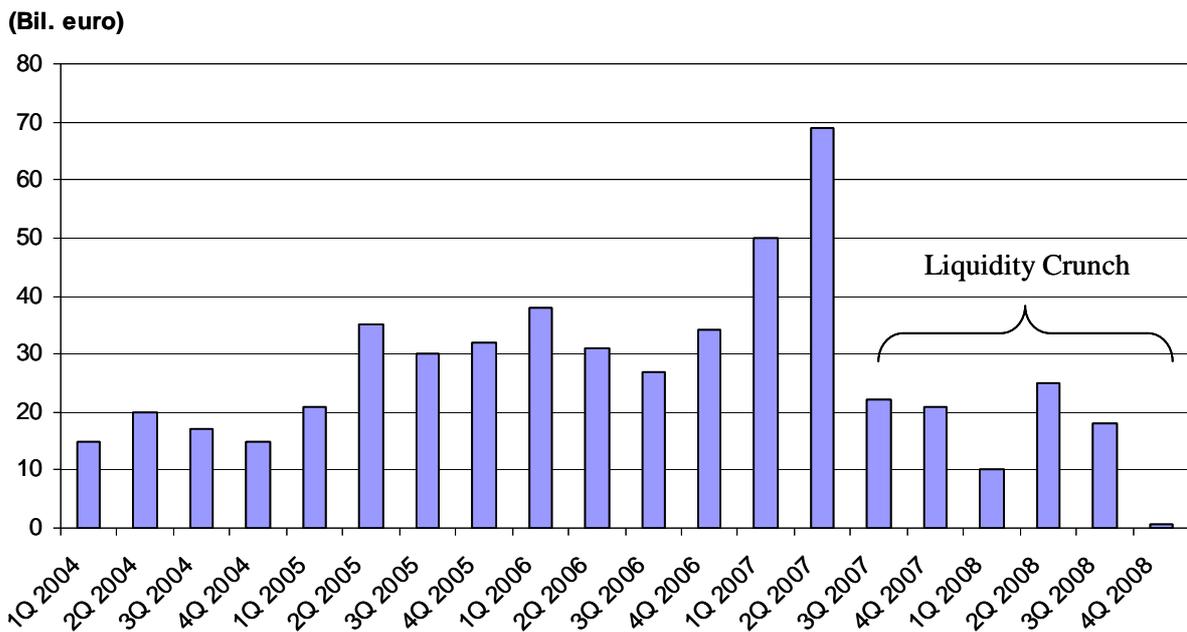
The leveraged finance departments, however, faced difficulties with existing credits which limited their accessibility to the scarce capital internally at banks disposal. The credit committees would immediately reject any commitments involving leveraged debt products, even when presented with potentially attractive deals. Focus was now being directed towards relationship borrowing and in particular investment-grade companies. Local corporate businesses were preferred over weaker relationships of private equity sponsors across Europe.

In addition, the financial system went into total chaos as one of the world's largest investment banks, Lehman Brothers, filed for bankruptcy on September 15, 2008. The final pinch of confidence in the banking system disappeared, and the interbank lending market collapsed - leaving numerous banks nationalised, bailed-out, forcibly merged, or broken up.

In this new environment, characterised by large government intervention and decreasing appetite for risk, banks in general made less capital available to be invested in leveraged finance products - favouring more stable and high-quality assets.

The volume of new issuance in the leveraged loan market decreased significantly in the second half of 2007 and for the whole of 2008, as a result of the shrunken investor base and carefulness of the few lenders still possessing available cash.

Figure 5.5: European Senior Leveraged Loan Volume



Source: Own Construction Based on Data from McGaiven & Yang (2009)

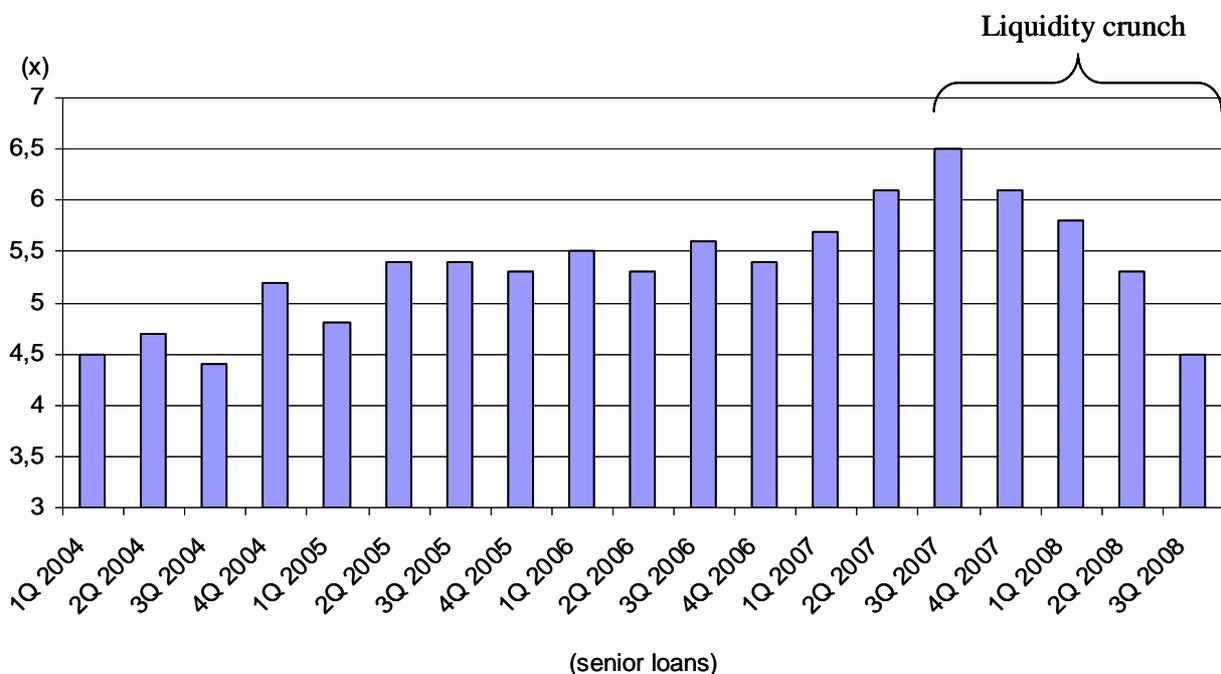
As illustrated in the figure, the primary market suffered in the second half of 2007. Volume for the full year was actually record high at €165.5 billion, but the first half of the year represented more than 70% of that. In addition, about 40% of total issuance in the second half occurred in July, before the crisis really began.

The pattern continued throughout 2008. Senior volume dropped to a total of €52.49 billion, of which 46% of all deals launched in the first half of 2008 where actually so-called legacy deals. The market experienced a steep decline in the end of 2008, when the influence of the excessive share of pre-mandated deals finally waned. This effectively revealed the true seriousness of the situation.

Likewise, the type of deals and the syndication process have changed as a consequence of the credit crisis. Loan facilities are no longer syndicated as underwriting deals, due to difficult trading conditions. Arrangers simply refuse to carry the increased underwriting risk by initially providing the entire commitment. Instead, the few smaller deals which actually have made it to the market are primarily launched through club-style syndication. In this way the arrangers are not depend on commitments from any kind of funds as the underwriting risk is divided into manageable pieces. The total amount, syndicated in the market, is simply not larger than it can be placed within a handful of relationship banks.

Besides the disappearance of liquidity, the utilisation of leverage has also been revised. With leverage unwinding in all corners of the financial system, it is inconceivable that the leveraged loan market will revive in the same form as before the credit crisis. According to figure 5.6, European LBOs were typically structured by means of leverage multiples exceeding 6x EBITDA. The deal-makers had obviously taken advantage of recent years' hyper-liquid market conditions. Consequently, many deals have simply been overleveraged in proportion to what the companies are able to service in an economic downturn of this magnitude - making the current deleveraging a key process. Leverage multiples must definitely come down, which is already to be seen.

Figure 5.6: Average Pro Forma Total Debt/EBITDA



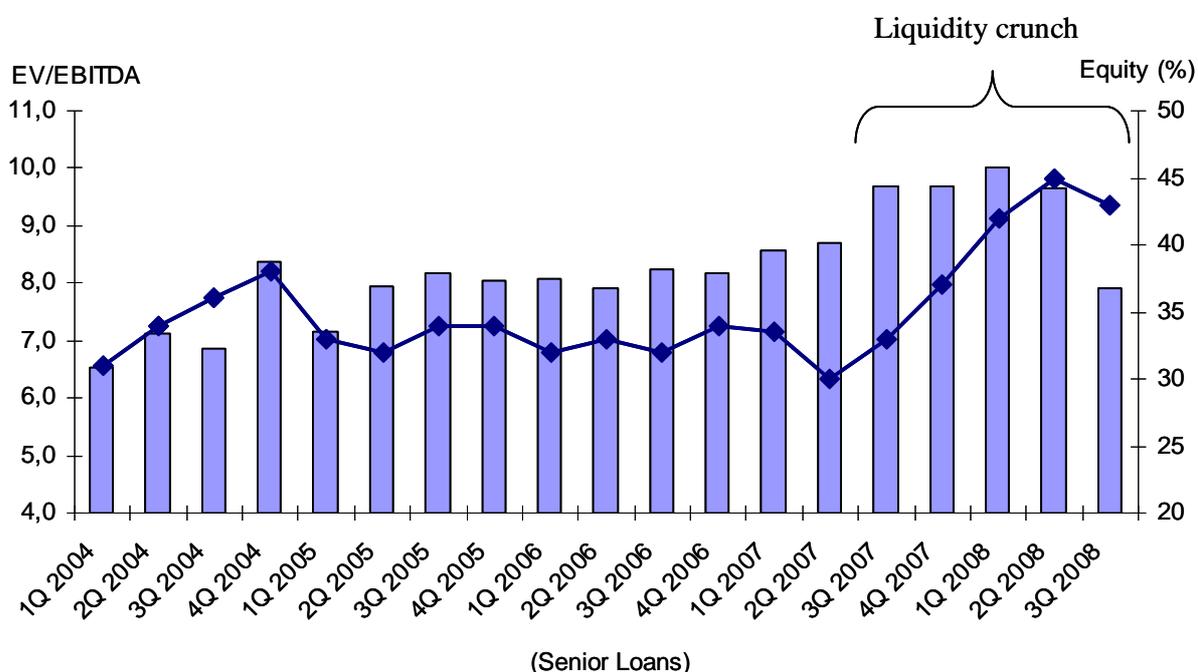
Source: Own Construction Based on Data from McGaiven & Yang (2009)

In the third quarter of 2007 some of the most risky deals were launched. In fact 78% of leveraged loan issuance carried total debt-to-EBITDA of 6x or higher, while 44% were leveraged at 7x or higher. Total leverage on some deals topped at 8x with second lien used to stretch senior leverage. However, leverage gradually went down from an average of 6.5x in the third-quarter of 2007 to 5.3x at the end of the second-quarter 2008. In the second half of 2008, the deleveraging in the market appeared more clearly - uninfluenced by the legacy deals structured in the more issuer-friendly environment of 2007. Effectively, in third-quarter 2008, leverage for LBOs dropped to 4.5x EBITDA.

In short, the reduction in the leverage ratio is to accommodate the reappearance of amortising debt, higher margins, and increased macro sensitivity.

As a result of 1) less debt available to support the financing of LBOs, 2) reduced earnings expectations, and 3) a 45% percent drop in stock prices throughout 2008, the purchase price multiples will inevitable be affected downwards. From figure 5.7, it appears that enterprise multiples already have started to adapt to the new realities with the latest figures now being below those of 2005. Applicable to existing portfolio companies as well as new transactions, enterprise valuations are falling significantly.

Figure 5.7: Average Purchase Multiples and Average Equity Contribution to Buyouts

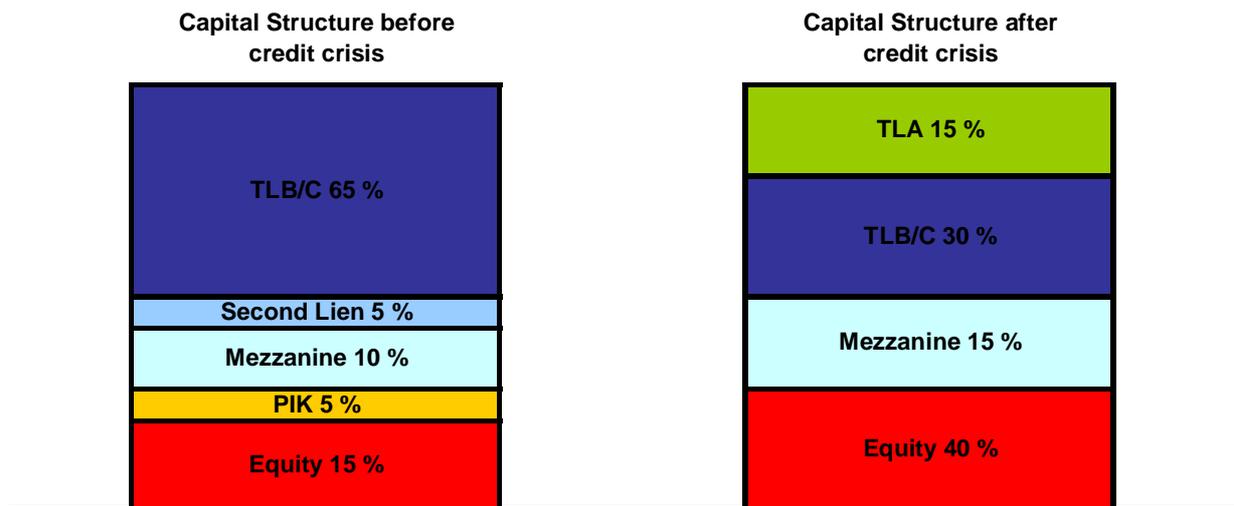


Source: Own Construction Based on Data from McGaiven & Yang (2009)

As illustrated above, purchase price multiples increased to massive 10x EBITDA in late 2007 and early 2008 - even though the credit crisis had started. However, the steady increasing amount of equity contribution suggests that the purchase multiple was kept artificially high. In the second quarter of 2007, private equity owners merely committed an average of 30.4% of equity and many got away with 25% or even less. Although equity commitments in the area of 40% to 45% became the norm, they could not keep the purchase prices at the same high level. In 2008, the purchase price multiple dropped to around 8.0x which was not seen the private equity wave in earnest accelerated in the beginning of 2005.

The capital structure of LBOs has not only changed regarding the overall debt-to-equity proportion. The proportions between the specific loan types have likewise been subject to change which is illustrated when comparing typical capital structures before and after the credit crisis.

Figure 5.8: Typically Capital Structures Before and After the Credit Crisis



Source: Own Construction Christiansen (2009)

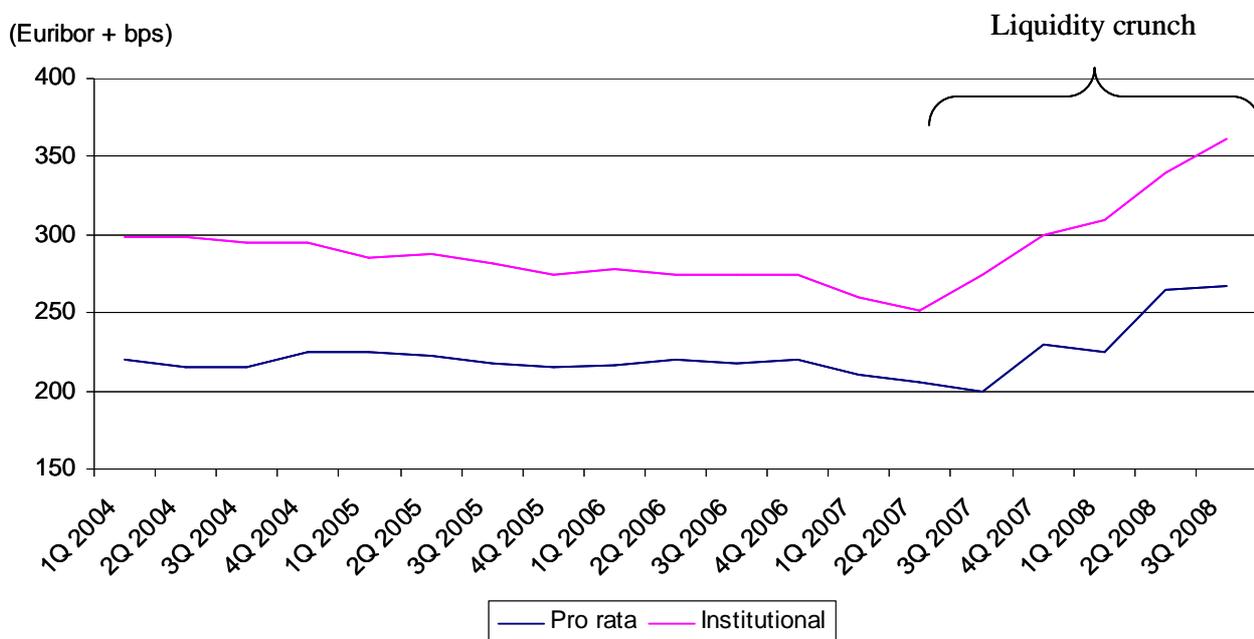
At first, it is worth noticing that the amortising term loan A facility - usually held by banks - has replaced part of the institutional tranche, TLB/C. This is a clear cut result from the earlier mentioned changes in the investor base.

Secondly, the overall distribution of debt between first lien, second lien, and mezzanine are no longer structured according to previous liquid market conditions. These market conditions were characterised by less expensive tranches - such as first or second lien - replacing the more expensive mezzanine debt. Today, new deals are simply launched without second lien. With the disappearance of this asset class, which has always been more popular with borrowers than lenders, the transactions are now executed with more simple corporate debt structures. In the second-quarter 2008 the classic senior/mezzanine capital structure reached 68% - up from just 14% in the same quarter of 2007.

A final fundamental change within the European leveraged loan market is the soaring spreads. Appearing from the graph below, the average institutional loan spread on new issuance was very stable from the beginning of 2004 to early 2007 - though experiencing a gradual descend from E + 300 bps to E + 275 bps. From the end of 2006 until the beginning of the credit crisis in

summer 2007, spreads were forced further down due to the earlier described significant investor demand at the time. As a result, the institutional term loan spreads reached a record low of E + 252.76 bps in May 2007, just months preceding the financial crisis.

Figure 5.9: Weighted Average Spreads



Source: Own Construction Based on Data from McGaiven & Yang (2009)

Clearly the credit crunch had a major impact on spreads. More or less from day one, spreads have been significantly increasing - way above previous highs. The lack of available investors funding has enabled the few lenders in possession of cash to demand greater yields in return for their commitments. This witnessed by mid 2008 where the average spread for institutional term loans reached E + 340 bps, which has been added an additional 21 bps in the third quarter - leaving it at a record high: E + 361 bps.

5.3. CHAPTER SUMMARY

It is obvious that the primary leveraged loan market has been afflicted due to the entrance of the credit crisis. Loan fund issuance which was the former engine of growth has stalled as a result of the broken arbitrage opportunities. This has changed the market from a hyper liquid condition to a standstill. The volume of loan issuances is, compared to earlier, more or less non-existing. The few deals making it to the market are launched through club-deal syndication restricted to bank participation. The former complex debt structures have become far more

simple and safe. The transactions have experienced a deleveraging process which has forced the purchase price multiples down while the equity contribution has gone up. At the same time, spreads have been rising due to the scarcity of investors. In this way it is clear that the quality and yields of the few new deals making it to the market have improved significantly from a lender perspective. It is, however, difficult to predict whether the improvements are sufficient enough to bring back the investors.

First of all, the crux seems to be stability and investor confidence. The collapse of the secondary market seems to be without an end – continuing to inhibit the primary market. Until arrangers are somewhat certain that the bottom has been reached, they will remain on the sideline. With the present market volatility, no arrangers are willing to take any underwriting risks on larger deals. Evidently, one should not expect larger transactions to be executed any time soon.

Secondly, the debt structures might experience an evolution towards even more simplicity than seen in today's Senior/Mezzanine composition. Although there appears to be a decent appetite among mezzanine funds, their required returns are getting closer to the equity sponsor's own expected returns. As a result, an all-senior deal seems more sensible. Rather than giving away large non-call provisions, the sponsor may as well just put in a load of equity and keep the option to refinance.

Finally, terms of the secondary market indicates that spreads need to go up and leverage further down. Characterised as a quality note in the secondary market, TDC trades in the upper 80s by the end of 2008. The corresponding margins are at E + 200-250 bps while the debt/EBITDA ratio equals 3.7x. Assuming a four-year maturity, these loans effectively yield E + 500-550 bps. Relative to actual primary market figures Q308, new deals are on average offered with a debt/EBITDA of 4.5x and spreads at E + 360 bps. This strongly suggests that primary issuance still has some catching up to do. For deals with leverage somewhere in the 3-4x territory, spreads at E + 500-600 bps could be considered the target yield for new issuance.

The above mentioned predictions do not exactly prompt an optimistic view of new leveraged lending activity in the near future. Even with improved terms and structures on new deals the way ahead still allows for more improvements before leveraged loan issuances once again become interesting investment objectives.

6. SECONDARY MARKET ANALYSIS

The forthcoming chapter contains an examination of the secondary leveraged loan market. This entails a preliminary description of the development in the secondary trading activity – in which the significantly improved market standards, and the increased number of institutional investors, have played a key role. Subsequently, the chapter provides a thorough analysis of how the financial crisis has made its mark on the loan prices in the secondary market. On the basis of the current market conditions, we end the section with a view into 2009, to point out the most looming risk factors in a new possible wave of forced selling.

The following relies on Bear (2007), McGaiven (2009), Taylor & Sansone (2006), Yang, Gupte & Lukatsky (2009), King et al. (2009). In addition to this personal communication with Christiansen (2009) and Skødeberg (2009).

6.1. DEVELOPMENTS IN THE SECONDARY MARKET

Making the leveraged loan market more efficient has been one of the most important recent developments in the leveraged loan market. To compare the market to some of the more traditional capital markets - such as bond and equity - the existence of greater transparency and liquidity was required. The growth of institutional investor participation has brought along major improvements in fulfilling these requirements.

First of all, the increased investor base has been the most influential factor for the foundation of a true secondary market. The European loan market was exclusively dominated by banks until the beginning of the century. Since these banks generally invested in loans with the intention of holding them until maturity, there was little need for a secondary market. However, the need for a reliable and liquid secondary market became evident as more institutional investors entered the loan market through CLOs and hedge funds. With their focus on an active total return management and trading, these investors are simply dependent on an efficient secondary market in which they can actively manage their portfolios.

According to Taylor & Sansone (2006) the development of the secondary market is actually a virtuous circle: "The development of a sophisticated nonbank lender base facilitates (and increasingly is contingent upon) the development of a liquid secondary loan market".

Starting in 1999, an increasingly liquid secondary market emerged as more institutional investors entered the loan market. With their entrance more loans were traded - increasing the liquidity of the secondary loan market. This encouraged more institutional investors to enter the loan market - creating a self-reinforcing mechanism.

With the growth rate of primary loan issuance dependent on the secondary market becoming more liquid - in order to fulfil institutional investor demands - several institutions and individuals worked diligently to accelerate the liquidity process. Indeed, the organisation of the Loan Syndication and Trading Association (LSTA) has been critical in developing trading norms and settlement time frames.

One of the greatest differences between loan trades and stock or bond trades is how they settle. Loans close on the exchange of negotiated documents because of their complexity, whereas bonds and stocks settle electronically. Consequently, a previous lack of standardised trade practices and documentation for purchasing, selling, or closing loans were a huge obstacle. Closing a trade could easily take weeks.

Although the LSTA is not a regulatory authority, their intensive work within shortening and facilitating this settlement process, has contributed significantly to the rapid development of a more liquid secondary loan market. However, participants are still faced with difficulties in closing their loan trades on a timely basis and in an efficient manner due to the nature of the complicated settlement procedure.

The availability of pricing information is another important aspect that has enhanced the transparency in the secondary loan market. In order to fulfil their more active investment strategies, institutional investors need a reliable and independent source of prices on a regular basis. As a result several banks, in particular investment banks, have established secondary trading desks in the loan market, offering trade prices.

Although minimum assignments and transaction fees tend to impede liquidity to some degree, trading costs are anticipated to decline concurrently with the market continuing to move towards more standardised trading practises and documentation.

To sum up, it is obvious that the days of the secondary market as a sleepy backwater market in terms of trade volume and liquidity is over. The secondary loan trading has improved significantly as a result of several factors. First of all, the increased number of institutional

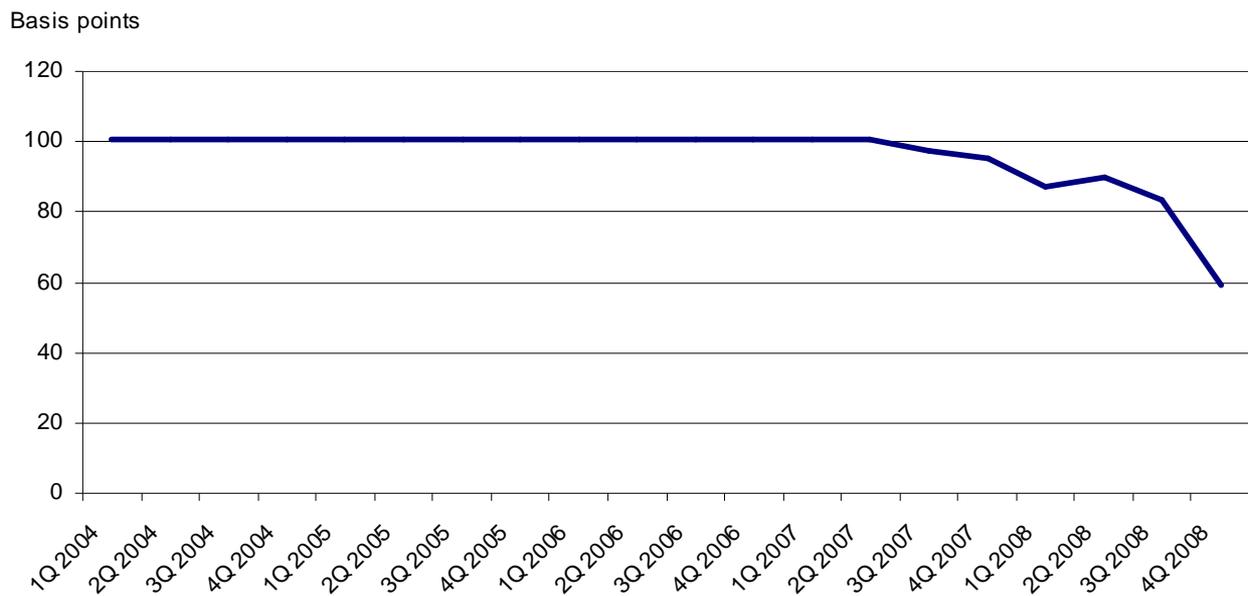
investors, with a more active trading approach, has spurred the trade volume. Secondly, LSTA has improved the liquidity by standardising documents and trading procedures. Finally, pricing services have supported assets managers' active trading possibilities. However, the market continues to suffer from impediments due to the nature of its more complicated trading procedure, larger transaction fees and minimum assignments.

6.2. THE IMPACT OF THE CREDIT CRISIS ON THE SECONDARY MARKET

The rate of new loan issuance and the general conditions in the primary leveraged loan market are contingent upon the circumstances in the secondary market. The secondary market stimulated the primary market during the bull-run of previous years. Similarly, it has greatly contributed to the deterioration in the leverage loan market since the onset of the credit crisis.

After several years with lots of liquidity, and leveraged loans trading at a premium to par, the summer of 2007 immediately changed the assumption that senior debt is a par instrument given the credit is performing. Seemingly overnight, leveraged went from hero to villain when it started a tidal wave of deleveraging within the financial system. In the process of bringing down balance sheet leverage banks tried to reduce their unsold inventory. Combined with the general diminishing investors' appetite for risk, this selling pressure was immediately reflected in the pricing of secondary leveraged loans. As illustrated in figure 6.2, the average bid in the S&P European Leveraged Loan Index (ELLI) went from 100.54 to 95.03 in the second half of 2007 - resulting in a market value return of negative 5.16%. In total return, the index experienced a loss of 3.39%, which was the first negative six-month return in its history.

Figure 6.2: Secondary Market Prices (ELLI Index)



Source: Own Construction Based on Data from McGaiven & Yang (2009)

While secondary pricing experienced a historical drop in the second half of 2007, 2008 showed that this was just the beginning. The main driver during the second wave of falling prices was forced selling caused by technical factors.

With banks managing their balance sheets more aggressively, prime brokerage services in the credit derivatives market became one of their main concerns. In their desperate attempt to reduce the exposure to this area, banks raised funding margins and haircuts on renewed TRS programs. Particularly influential was the sharply increased haircuts. Consequently, lots of hedge funds, which had committed their financing through TRSs, hit margin-call triggers and were forced to unwind (as described in section 4.4.). Before the credit crisis began, most hedge funds bought loans on 3 - 5 times leverage through total return swaps. Today this gearing has been significantly reduced to around 1 – 1.5 times, to accommodate the stricter lending conditions.

Furthermore, as the year progressed, the hedge funds which had managed to navigate higher haircuts were now experiencing large investor redemptions. In their struggle to get any possible liquidity, investors indiscriminately redeemed wherever they could - regardless of strategy, performance or associated losses. In fact, the problem got so comprehensive that many funds by the end of the year chose to freeze redemptions and establish "gates" limiting the amount of money investors could withdraw at once. In this way, funds are better protected against

short-term run on their assets, which helps to avoid selling at fire-sale prices and, thus, potentially relieve short-term market pressure. However, the trend is also causing tension between investors, who may be in urgent need of cash, and managers, who may be more interested in holding on to assets to protect their businesses. It appears to be a delicate matter for managers to protect their own interests while acting to preserve the value of the portfolio for investors.

Hedge funds have been forced to sell out en masse as a result of the above-mentioned deleveraging process. The twin forces of executed investor redemptions and swaps hitting price triggers has effectively left the loan prices in freefall.

In addition, several market value CLOs have breached their covenants due to severe losses in their portfolio. When the value of the underlying collateral comes below a certain price level, the CLO hit its market-value-trigger which forces the fund to unwind (as described in section 4.3.).

Managers looking to resolve market value issues are essentially faced with two options when trying to avoid liquidation. They can either restructure the market value vehicle into a cash flow CLO, or they can raise additional equity through asset sales or via equity injections. In a period with shortage of capital, most subordinated investors found themselves in a position where they chose not to "throw good money after bad". Instead most market value CLOs have deleveraged through a restructuring process where the best parts of the fund have created the foundation for a new cash flow CLO.

For the hedge funds and market value CLOs, which did not manage to survive the above mentioned difficulties, a total liquidation of the fund took place. Several funds tried to sell off their loans in larger chunks through so-called Bids Wanted In Competition (BWIC), due to the illiquid market conditions. This entails different dealers being allowed to make bids on the given portfolio. With total BWIC activity rolled out in 2008, more than 40% higher over 2007, this obviously created a tremendous selling pressure.

The outcome of the fund world pushing assets into a market already in its knees is depicted in figure 6.2 above. In a vicious cycle of forced selling and falling prices, the average bid fell nearly eight points from 95.03 to 87.07 in the first quarter 2008. With a total return of minus 8.56% the performance was more than twice as bad as the previous part of the credit crisis.

In the second quarter of 2008, months of bleak outlooks were suddenly replaced with a godsend gain in the market value. Given the horrors the market had suffered in January and February, market participants obviously were reluctant to tempt fate in believing the market would not crash again if more bad news appeared. However, it became clear that along with the quarterly positive total return of around 5%, some market participants actually started to gain faith in the market again. Earlier month's downswing could be explained with technical and liquidity driven factors rather than fundamental factors. Corporate balance sheets generally seemed in good shape (at least outside the financial sector) and default rates of senior secured loans were close to zero. It all appeared to be one of these great buying opportunities which you would not miss in the world. As a result, buyers were spotted in the market for the first time since the onset of the credit crisis - looking for what seemed to be good corporate credits at heavily discounted prices.

However, just as modest optimism had returned into the market, the third and most severe wave of falling prices accelerated. Up to this point, the collapse in secondary loan prices was mainly due to technical factors, but in the second half of 2008 the threat of recession was becoming ever more real. With a comprehensive economic slow-down at hand, outlooks of inevitable rising default rates and signs of shockingly low recoveries, was the new reality. In a risk adverse world, filled with distressed investors, the leveraged loan market turned into a true nightmare of falling prices.

Starting above par during the summer of 2007, when the credit crisis began, the year ended with prices around 95. In 2008, the prices just kept falling at a frightening pace. Investors' portfolios lost a total of 30% over the course of the year. At first, the average prices in the ELLI Index went below 80, then 70, and now the index has just moved below 60. The market players are still waiting on the sideline to see how low they can go. Investors have learned from earlier this year that it can be very costly to enter the market at what seems to be the bottom of this total collapse in the secondary market prices.

6.2.1. Looking Into 2009

Fears of credit deterioration seem to be the most conspicuous risk factor in a new possible wave of selling. Cash flow CLOs spent the first phase of the credit crunch largely protected by par-value accounting, while in particular market value CLOs and hedge funds were exposed to a

tremendous pressure throughout 2008. However, as the loan performance switched from being driven by technical factors to fundamental difficulties, it is now the turn of cash flow CLOs managers to feel the “excitement”.

Signs of distressed credits sharpened significantly in the latter of 2008, as a result of the declining corporate profitability. In mid-December 2008, LCD tracked 21 requests to amend or waive financial covenants for the year - of which one-third was submitted in the fourth quarter alone. In 2007, the total number of requests was merely five.

Furthermore, the share of issuers rated within the CCC/CC range in the ELLI Index more than quintupled - from 0.22% to 1.25%. In addition, a report from S&P in December showed that the share of CCC credit estimates had risen to 5.2% by mid- November 2008 - up from 3.4% at the end-June 2008, and just 1.6% at the end of 2007.

Given these severe credit problems already witnessed in the end of 2008, CLO managers are inevitably faced with a huge challenge consisting of a forthcoming wave of downgrades. While most vehicles have certain maximum levels of CCC rated assets in their collateral portfolio, any excess will have to be mark-to-market. As a consequence, it is a widespread market expectation that a relatively large number of CLOs will experience difficulties in passing their over-collateralisation tests.

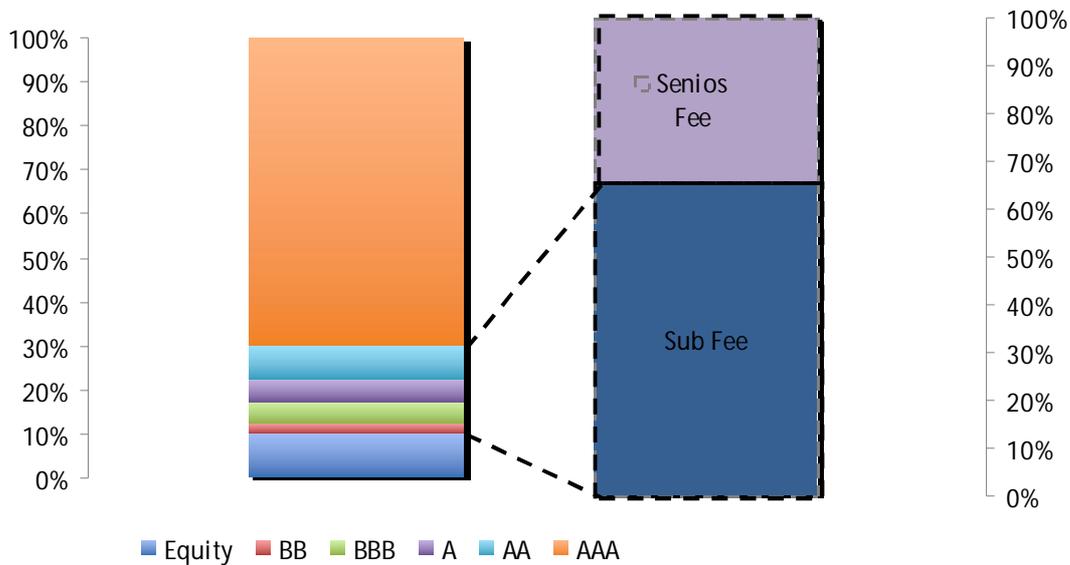
As described in section 4.3, a breached OC test will trigger an event of default and all the cash flows will be diverted to pay down interest and principal of the senior note holders in compliance with the payment waterfall. At this juncture, the direct control of the CLO is switched to the senior note holders, who can chose either to liquidate the CLO or follow the payment waterfall and gradually delever over time. Although this would not automatically lead to a massive round of forced selling, the controlling classes could opt to liquidate the portfolio in a scenario where a large portion of CCC rated assets carry low market valuations.

In fact, a principal-agent conflict arises from the fact that CLO managers’ sub-advisor fees are suspended due to the failed OC test. As figure 6.3 illustrates, in general more than 66% of aggregate fees to CLO managers are effectively generated by the junior notes. Without these fees CLO managers can become unable to maintain a minimum service platform, and may not be able to meet operational service requirements or remain solvent. Especially in Europe, this could become a problem since the CLO mangers usually do not have multiple funds creating a

stable fee platform. Given the insufficient payments accruing to the manager, one cannot expect him to behave in the best interest of the investors - he simply has no incentive. This fact could actually cause the CLO managers to trigger insolvency. Especially in cases when senior note holders have chosen to reject requests concerning changes in the size of the CCC bucket. Essentially, the senior note holder cuts off the main part of the managers' payments which leaves him no incentive to keep the CLO alive.

A round of liquidations could, however, be avoided through a consolidation among stand-alone CLO platforms into larger asset managers. In this way more stable fee platforms are effectively achieved and the vulnerability towards reduced management fees within the single CLO is considerably mitigated.

Figure 6.3: Manager Reliance on Subordinated Fees



Source: Own Construction Based on Data from Eyerma et al (2009)

6.3. CHAPTER SUMMARY

The secondary loan market has gone through a total meltdown since the onset of the credit crisis in summer 2007. For the first time in history, the market has experienced a longer period with negative returns. To begin with, in particular hedge funds and market value CLOs were subject to a comprehensive deleveraging process. This led to a vicious cycle of forced selling and falling prices. The threat of a looming recession magnified as the crisis progressed, and fundamental difficulties started to substitute technical factors. Bleak outlooks of rising default

rates and low recovery rates pushed the market into a total hysteria of falling prices. At the end of 2008, the average price of the ELLI Index stood at shockingly low 60 – these were loans that for many years were traded at premiums to par. Looking into 2009, the cash flow CLO seems to be the next investment vehicle experiencing difficulties. Given the severe economic slowdown, there is a widespread expectation that some CLO managers will breach their OC tests. Even though this does not necessarily lead to a slew of forced selling, the CLO structure is once again tested with respect to how well or badly it withstands the shocks of a downturn.

PART 4

Part 3 contained a thorough analysis of the primary and secondary leveraged loan market. Initially, the reader was provided with an explanation of the rapid growth in both markets, followed by an analysis of the effects from the credit crisis. It is clear that the increased institutional investor base significantly stimulated the market conditions during the bull-run. Likewise, they significantly contributed to the deterioration triggered by the credit crisis. The leveraged loan market has suffered heavily from hedge funds and market value CLOs being forced to unwind. This created a vicious self-reinforcing mechanism.

Effectively, part 3 has provided an analysis of the influences of institutional investors and the credit crisis to the leveraged loan market.

Part 4 includes chapter 7 and 8. In this section the reader is presented with the theoretical framework for pricing corporate debt when tranching according to priority. The model is derived to enable the later comparison of the theoretically obtained debt value of ISS with actual market prices. This allows for a determination of whether market prices are in correspondence with theory. Careful considerations concerning estimation methods are made to ensure the quality of the model output.

	Problem Identification and Method	Chapter 1
Part 1	<div style="display: flex; justify-content: space-around;"> <div style="border: 1px solid black; padding: 5px; width: 45%;">Syndicated loan market</div> <div style="border: 1px solid black; padding: 5px; width: 45%;">Leveraged loans</div> </div>	Chapter 2 & 3
Part 2	<div style="border: 1px solid black; padding: 5px; width: 60%; margin: auto;">CLO structure</div>	Chapter 4
Part 3	<div style="display: flex; justify-content: space-around;"> <div style="border: 1px solid black; padding: 5px; width: 45%;">Analysis of primary leveraged loan market</div> <div style="border: 1px solid black; padding: 5px; width: 45%;">Analysis of secondary leveraged loan market</div> </div>	Chapter 5 & 6
Part 4	<div style="border: 1px solid black; padding: 5px; width: 60%; margin: auto;">Theoretical framework for pricing corporate debt</div> <div style="border: 1px solid black; padding: 5px; width: 60%; margin: auto;">Theoretical frameworks for estimation of input variables</div>	Chapter 7 Chapter 8
Part 5	<div style="border: 1px solid black; padding: 5px; width: 60%; margin: auto;">Estimation of input variables</div> <div style="border: 1px solid black; padding: 5px; width: 60%; margin: auto;">Analysis of results from the model</div> <div style="border: 1px solid black; padding: 5px; width: 60%; margin: auto;">Conclusion</div>	Chapter 9 Chapter 10 Chapter 11

7. THEORETICAL FRAMEWORK FOR PRICING CORPORATE DEBT

The following chapter provides for a derivation of the theoretical foundation for pricing corporate debt when subordinated. On the basis of the Merton model (1974) and the Black Scholes model (1973), a model for pricing corporate debt when sequentially tranced is initially derived. Subsequently, the framework turns towards Leland (1994), who provides the necessary theory for pricing corporate debt when treated as a coupon bond. Finally, the theoretical framework of Leland is extended to handle debt when tranced in order of priority.

For a textbook treatment of section 7.1 see Lando (2004), and section 7.2 see Leland (1994). In addition to this personal communication with Christiansen (2009) and Skødeberg (2009).

7.1 THE MERTON MODEL

The Merton model views a company's equity as a call option on its assets in order to price the shares of a company. Applying the put-call parity the value of a put can be priced analogously to find the value of debt. The basic idea behind the model is to view all corporate securities issued by a firm as contingent claims on the firm's assets given the evolution of the market value of these assets.

In the theoretical framework certain assumptions must be satisfied in order for the model to be correct. The settings of the standard Black Scholes models are assumed satisfied, where

- Agents are price takers, i.e. trading in assets has no effect on prices,
- There are no transactions costs,
- There is unlimited access to short selling and no indivisibilities of assets, and
- Borrowing and lending through money-market account can be done at the same riskless, continuously compounded rate r .

Given the time horizon is \bar{T} , we wish to price a bond issued by a firm. Assuming that the value of the firm's assets follows a geometric Brownian motion, the stochastic process V_t can be expressed as

$$dV_t = \mu V_t dt + \sigma V_t dW_t$$

where W is a standard Brownian motion, μ is the asset drift, and σ is the asset volatility. Both μ and σ are constants. Here dW represents the uncertainty in the price history of the assets. Setting the initial value of the asset equal to V_0 , the equation yields the following solution

$$V_t = V_0 \exp \left(\left(\mu - \frac{\sigma^2}{2} \right) t + \sigma W_t \right)$$

which is a log-normally distributed random variable.

Now assuming the existence of a money market account with a constant riskless rate r . The price evolves deterministically as

$$\beta_t = \exp (rt)$$

We know that the price C_0 at time 0 of a contingent claim paying $C(V_T)$ at time T in an economy consisting of these two assets equals

$$C_0 = E^Q [\exp (-rt) C_T]$$

Expressing the value of C_0 as the expected value of C_T discounted by the constant riskless rate r at time t . Here Q is the equivalent martingale measure under which the dynamics of V are given as

$$V_t = V_0 \exp \left(\left(r - \frac{\sigma^2}{2} \right) t + \sigma W_t^Q \right)$$

where W^Q is a Brownian motion. The replacement of μ with the constant riskless rate r still satisfies the requirement of a constant drift embedded in the Brownian motion.

It is worth remembering, that the present market value of the future cash flows generated from an asset constitutes its market value. Any financing decisions made by the firm's owners are assumed without influence on the asset value.

To begin with our starting point is time 0 where we assume the firm has issued two types of claims consisting of debt and equity. For simplicity we will in the initiating phase treat debt as a zero-coupon bond with a face value D and a maturity date $T \leq \bar{T}$. We are now able to express payoffs to debt and equity at time T as follows

Payoff to debt: $B_T = \min(D, V_T) = D - \max(D - V_T, 0)$

Payoff to equity: $S_T = \max(V_T - D, 0)$

by which the view of equity as a call option on the firm's assets is exemplified. The underlying reasoning is that equity owners run the firm. The equity owners will only exercise their call option to pay off debt and retain ownership of the assets, when the total value of assets is higher than the total value of the debt. In the reverse scenario, where the face value of debt exceeds the value of the assets, equity owners are – due to limited liability – not obligated to pay the face value of debt and realise a negative pay-off. Instead they will rather renounce ownership and receive 0. Bond holders exercise their contingent claims and retain ownership of the remaining assets. They thereby receive a recovery of V_T which is less than the promised face value of debt. Effectively, debt can be expressed as the difference between a riskless bond and a put option.

With no corporate taxes or tax advantages associated with issuing debt, no other parties are to receive any payments from V which implies that the firm's assets equal the value of debt and equity

$$V_T = B_T + S_T$$

leaving the composition of the capital structure irrelevant as the relationship between debt and equity is without influence to the value of the firm's assets.

In order to value debt and equity prior to maturity date T , we incorporate Black Scholes formula for pricing options to our perception of payoff to debt and equity. Thereby we obtain the Merton model, as follows

Value of equity: $S_t = C^{BS}(V_t, D, \sigma, r, T - t)$

Value of debt: $B_t = D \exp(-r(T - t)) - P^{BS}(V_t, D, \sigma, r, T - t)$

where C^{BS} and P^{BS} is the Black Scholes price of a European call and put option, respectively. The face value of the bond, D , constitutes the strike price while T is time to maturity and r is the riskless rate. The unknown factors for later estimation then becomes the current level of V at time t and the corresponding volatility σ of the firm's assets.

With the asset value equal to the value of debt and equity, debt can be expressed as

$$B_t = V_t - C^{BS}.$$

The Merton model easily handles subordinated debt which is essential for the later valuation. The model deals with subordination as depicted in table 7.1. The senior most secured debt has a priority over junior debt, and can therefore be priced as if it were the only debt issue. Junior debt can be priced according to its position in the subordination which is below senior and above equity. When all senior debt has been repaid, the remaining value of the assets accrues to junior bond holders to the point where the asset value equals their face value. Equity owners will receive the value of the assets remaining after the senior and junior bond holders have been repaid. This means that equity can be priced by viewing the entire debt as one class. Table 7.1 illustrates the payoffs to senior and junior debt and equity at maturity. The face values of senior and junior debt represented are by D_S and D_J respectively.

Table 7.1: Payoff at maturity

Type of debt	$V_T < D_S$	$D_S \leq V_T \leq D_S + D_J$	$D_S + D_J < V_T$
Senior	V_T	D_S	D_S
Junior	0	$V_T - D_S$	D_J
Equity	0	0	$V_T - (D_S + D_J)$

Source: David Lando

With the payoff structure specified according to seniority an option representation can be illustrated as in table 7.2. $C(V, D)$ expresses the payoff at expiration of a call option. V is the value of the underlying asset while the face value of debt D represents the strike price.

Table 7.2: Option representation

Type of debt	Option payoff
Senior	$V - C(V, D_S)$
Junior	$C(V, D_S) - C(V, D_S + D_J)$
Equity	$C(V, D_S + D_J)$

Source: David Lando

The theoretical framework allows for a valuation of corporate debt when treated as a zero coupon bond. Leveraged loans, however, are issued as coupon bonds which mean that the

theoretical approach must be extended to provide a solution to this issue. Leland (1994) provides the necessary theory for pricing corporate debt incorporating continuous coupon payment. Moreover, Leland's model includes the tradeoff between the tax shield advantage of issuing debt and the bankruptcy cost arising hereof.

7.2. THE LELAND MODEL

The Leland model follows that of Merton which means the earlier assumptions still apply. However, some need alterations and additional assumptions must be satisfied, including

- The activities of the firm are unchanged by financial structure,
- Capital structure decisions, once made, are not subsequently changed,
- The face value of debt, once issued, remains static through time,
- A riskless asset that pays a constant rate of interest, r , exists.

The following theoretical framework allows for a valuation of time independent securities which implies that the corporate debt issued is perpetual debt. Leveraged term loans are, in general, issued with a maturity of approximately 7-10 years which justifies the assumption of perpetual debt. The asset value of the firm still follows a geometric Brownian motion with constant volatility and rate of return.

We now consider a claim on the firm that continuously pays a nonnegative coupon, C , per instant of time as long as the firm is solvent. The value of such a claim is denoted $F(V, t)$. Since the firm's capital structure must remain constant after the initial issuance, the net cost of the coupon can only be financed by issuing additional equity. From Black and Cox (1976) we know that any such asset's value must satisfy the partial differential equation

$$\frac{\sigma^2}{2} V^2 F_{VV}(V, t) + rV F_V(V, t) - rF(V, t) + F_t(V, t) + C = 0$$

With the assumption of time independence satisfied, the term $F_t(V, t) = 0$ and the equation becomes an ordinary differential equation with $F(V)$ satisfying

$$\frac{\sigma^2}{2} V^2 F_{VV}(V) + rV F_V(V) - rF(V) + C = 0$$

which general solution is

$$F(V) = A_0 + A_1V + A_2V^{-X} \quad , \quad X = \frac{2r}{\sigma^2}$$

where the constants A_0 , A_1 , and A_2 are determined by boundary conditions.

With the general solution to the value of contingent claims presented, we turn to the specific securities. The value of debt can be expressed $D(V; C)$, where C is the constant perpetual coupon payment promised unless the firm declares bankruptcy. For simplicity C is suppressed as an argument and debt value is denoted $D(V)$. The level of asset value at which bankruptcy is declared is denoted V_B . In the case of bankruptcy, a fraction $0 \leq \alpha \leq 1$ of value will be lost to bankruptcy costs. This leave debt holders with the value $(1 - \alpha)V_B$, and stock holders with nothing. Boundary conditions are given as

$$\begin{aligned} V = V_B : D(V) &= (1 - \alpha)V_B \\ V \rightarrow \infty : D(V) &\rightarrow \frac{C}{r} \end{aligned}$$

When the asset value increases, bankruptcy becomes irrelevant and the value of debt will approach the value of the capitalised coupon.

With the value of debt expressed in the general solution and the boundary conditions specified, we are now able to determine the constants A_0 , A_1 , and A_2 . With $V \rightarrow \infty$, we find that $V^{-X} \rightarrow 0$ which implies $A_1 = 0$ and $A_0 = \frac{C}{r}$. When $V = V_B$, we find $A_2 = \left[(1 - \alpha)V_B - \frac{C}{r} \right] V_B^X$. Consequently,

$$D(V) = \frac{C}{r} + \left[(1 - \alpha)V_B - \frac{C}{r} \right] \left[\frac{V}{V_B} \right]^{-X}$$

expresses the value of debt when issued as a coupon bond including bankruptcy costs.

The next step is to integrate the effects of taxes in the value of debt. The value of tax benefits associated with debt financing resemble a security that pays a constant coupon equal to the tax-sheltering value of interest payments, τC , as long as the firm is solvent and nothing in bankruptcy. The value of the security is denoted $TB(V)$ and equals the value of tax benefits associated with debt. Being time independent, it must satisfy the general solution with boundary conditions

$$\begin{aligned} V = V_B : TB(V) &= 0 \\ V \rightarrow \infty : TB(V) &\rightarrow \frac{\tau C}{r} \end{aligned}$$

In the case of bankruptcy, the firm loses the tax benefits. Conversely, with increasing asset value bankruptcy becomes irrelevant and the value of tax benefits approaches the capitalised value of tax benefit. With the given boundary conditions, the general solution yields

$$TB(V) = \frac{\tau C}{r} - \left(\frac{\tau C}{r}\right) \left(\frac{V}{V_B}\right)^{-X}$$

Tax legislation states that deductibility of coupon payments is only achieved when these are serviced by the firm's earnings before interest and taxes. We assume that $EBIT \geq C$ is satisfied at all times, and therefore the firm always benefits fully from the deductibility of coupon payments when it is solvent. Thus, the equation above holds.

Debt issuance consequently implies tax deductibility of coupon payments which increases the total value of the firm. Conversely, the possible bankruptcy costs related to debt issuance reduce total firm value. The current value of a security $BC(V)$, that pays no coupon, equals the bankruptcy costs αV_B when $V = V_B$. This reflects the market value of a claim to αV_B if bankruptcy is declared. The returns generated by this security are time independent, and therefore, the security satisfies the general solution with boundary conditions

$$V = V_B : BC(V) = \alpha V_B$$

$$V \rightarrow \infty : BC(V) \rightarrow 0$$

We find that, as asset value increases, bankruptcy becomes irrelevant. Given these boundary conditions the equation has the solution

$$BC(V) = \alpha V_B \left(\frac{V}{V_B}\right)^{-X}$$

We are now able to express the total value of the firm as

$$v(V) = V + TB(V) - BC(V)$$

which in its full length appears as

$$v(V) = V + \left(\frac{\tau C}{r}\right) \left[1 - \left(\frac{V}{V_B}\right)^{-X}\right] - \alpha V_B \left(\frac{V}{V_B}\right)^{-X}$$

This allows for an expression of the value of equity which is the total value of the firm less the value of debt.

$$E(V) = v(V) - D(V)$$

which in its full length appears as

$$E(V) = V - (1 - \tau) \frac{C}{r} + \left[(1 - \tau) \frac{C}{r} - V_B \right] \left[\frac{V}{V_B} \right]^{-X}$$

We now need to decide whether V_B is determined endogenously or exogenously. The former implies that the issuing company is not restricted by covenants and therefore shareholders will set the level of asset value at which bankruptcy is declared, V_B , where the value of equity is zero. The latter entails that debt is protected by positive net worth requirements restricted by covenants. In the theoretical framework this entails that bankruptcy will be declared if the asset value falls beneath the principal value of debt.

Leveraged loans are in general protected by covenants, working as a safeguard for investors to position themselves against potential future defaults. To ensure debt holders that cash flows generated by the issuing company are sufficient to service the debt, leveraged loan covenants usually restrict a minimum value of EBITDA (see section 3.2.3.). It seems fair to assume that a high correlation exists between asset value and EBITDA. On the basis of this, it is reasonable to assume that leverage loan covenants restricting EBITDA can be translated to covenants restricting the asset value. Effectively, we treat debt as protected by covenants restricting a minimum level of asset value and consequently V_B is determined exogenously.

When V_B is exogenously determined, we assume that the principal value of debt corresponds with the market value of debt when issued. This implies that $V_B = D_0$. In relation to this, it must be noted that minimum level of asset value should fulfill the requirements of share holders in which the value of equity is equal to or greater than zero. From the equation expressing the value of debt with $V_B = D_0$, we are able to write the value of protected debt at issuance as a function of the asset value, V_0 . The equation appears as

$$D_0(V_0) = \frac{C}{r} + \left[(1 - \alpha) D_0(V_0) - \frac{C}{r} \right] \left[\frac{V_0}{D_0(V_0)} \right]^{-X}$$

It is important to note that this equation only returns the value of debt at the initial asset value. The equation expressing the value of debt with $V_B = D_0(V_0)$ returns the value of debt as a function of the asset value, V .

7.3. EXTENSION OF THE MODEL FRAMEWORK TO INCORPORATE SUBORDINATION

The theoretical approach provided by Leland prices the total debt of the company without regards for a differentiation of debt. Leveraged buyouts are, however, typically structured with several tranches ranked according to priority. We therefore need to modify the model to handle subordination.

We look at total debt issuance as consisting of the different parts of debt - ranging from the senior most secured to the most junior unsecured. Total coupon must equal

$$C_{Total} = C_{Senior} + C_{Second Lien} + C_{Junior}$$

where C_{Senior} , $C_{Second Lien}$, and C_{Junior} represents the coupon to senior, second lien, and junior debt, respectively. In this definition only three types of debt issues are included. However, the specific composition of debt instruments varies greatly from company to company.

Total value of debt must equal

$$D(V; C) = D(V; C_{Senior}) + D(V; C_{Second Lien}) + D(V; C_{Junior})$$

where the different coupon payments are those observed within the specific tranches. The essential difference between senior and junior debt is their respective priority claim in the case of bankruptcy. We know that only a fraction of $(1 - \alpha)V_B$ accrues to debt holders when bankruptcy is declared. According to priority this fraction will solely accrue to senior debt holders until the repayment of their entire principal is satisfied. Any remaining recovery will accrue to the second lien debt holders until their entire principal is repaid. Finally, junior debt holders will receive whatever remains. When $V = V_B$, the value of debt issues, ranked in order of priority, can be expressed

$$D_S(V_B) = \min((1 - \alpha)V_B; V_{S,0})$$

$$D_{2nd\ lien}(V_B) = \min((1 - \alpha)V_B - D_S(V_B); V_{2nd\ lien,0})$$

$$D_J(V_B) = \min((1 - \alpha)V_B - (D_S(V_B) + D_{2nd\ lien}(V_B)); V_{J,0})$$

where $V_{i,0}$ of debt, $i = \{Senior; Second Lien; Junior\}$, expresses the notional value of the specific tranches. Furthermore, any given value of debt must satisfy $D_i(V_B) \geq 0$ as debt holders will never experience an additional loss in the case of bankruptcy.

From the equation expressing the value of debt, we know that the value of the continuous coupon until bankruptcy equals

$$\frac{C}{r} \left[1 - \left(\frac{V}{V_B} \right)^{-X} \right]$$

and the value of the repayment in case of bankruptcy equals

$$(1 - \alpha)V_B \left(\frac{V}{V_B} \right)^{-X}$$

where $\left(\frac{V}{V_B} \right)^{-X}$ represent the value of receiving 1 when V hits V_B , given the value today is V .

The principal value of senior, second lien, and junior debt are

$$D_S(V_0; C_S) = \frac{C_S}{r} \left[1 - \left(\frac{V}{V_B} \right)^{-X} \right] + \min((1 - \alpha)V_B; V_{S,0}) \left(\frac{V}{V_B} \right)^{-X}$$

$$D_{2nd\ lien}(V_0; C_{2nd\ lien}) = \frac{C_{2nd\ lien}}{r} \left[1 - \left(\frac{V}{V_B} \right)^{-X} \right] + \min((1 - \alpha)V_B - V_{S,0}; V_{2nd\ lien,0}) \left(\frac{V}{V_B} \right)^{-X}$$

$$D_J(V_0; C_J) = \frac{C_J}{r} \left[1 - \left(\frac{V}{V_B} \right)^{-X} \right] + \min((1 - \alpha)V_B - (V_{S,0} + V_{2nd\ lien,0}); V_{J,0}) \left(\frac{V}{V_B} \right)^{-X}$$

where any given $V_{i,0} * \left(\frac{V}{V_B} \right)^{-X}$ equals $D_i(V_B)$.

This entails two scenarios to which debt can be priced depending on the relationship between $V_{i,0}$ and $(1 - \alpha)V_B$. We begin with the scenario where $V_{S,0} \geq (1 - \alpha)V_B$ to which we have already provided the solution to $D_S(V_0; C_S)$ as

$$D_S(V_0; C_S) = \frac{C_S}{r} \left[1 - \left(\frac{V}{V_B} \right)^{-X} \right] + (1 - \alpha)V_B \left(\frac{V}{V_B} \right)^{-X}$$

Consequently, the value of debt junior to $D_J(V_0; C_J)$ is

$$X_J = \frac{C_J}{r} \left[1 - \left(\frac{V}{V_B} \right)^{-X} \right]$$

as all recovery accrue to senior debt holders.

We now turn to the derivation of $D_S(V_0; C_S)$ when $V_{S,0} \leq (1 - \alpha)V_B$ and find

$$D_S(V_0; C_S) = \frac{C_S}{r} \left[1 - \left(\frac{V}{V_B} \right)^{-X} \right] + V_{S,0} \left(\frac{V}{V_B} \right)^{-X}$$

Which under the assumption that returned recovery can be placed in debt with similar characteristics is

$$D_S(V_0; C_S) = \frac{\frac{C_S}{r} \left[1 - \left(\frac{V}{V_B} \right)^{-X} \right]}{\left[1 - \left(\frac{V}{V_B} \right)^{-X} \right]} = \frac{C_S}{r}$$

When full recovery is achieved in the case of bankruptcy, we find that the value of senior debt equals the value of the continuously compounded coupon - implying that the senior tranche is risk free. This is caused by the models deterministic approach to valuation of debt. Given the constant fraction lost to bankruptcy costs and certainty of the exact asset value when bankruptcy occurs, investors can pre-determine the exact amount of recovery returned when bankruptcy is triggered. However, it seems to be an invalid assumption that bankruptcy costs can be pre-determined given the uncertainties surrounding this variable. For example, it appears impossible to determine whether the company can be sold as a going concern or has to be liquidated in the case of bankruptcy - two scenarios which imply widely different bankruptcy costs.

In addition, the model assumes that an amount equal to $(1 - \alpha)V_B$ will be returned to debt holders when bankruptcy is triggered as $V = V_B$. For bankruptcy to be triggered at the exact moment $V = V_B$ would require that asset value is constantly monitored which is not the case. Consequently, it is fair to assume that bankruptcy might be declared in situations where $V < V_B$. This entails the asset value at bankruptcy not necessarily equals V_B , and therefore the total amount accruing to the investor as recovery will be less than initially assumed⁴.

In an attempt to circumvent these deterministic drawbacks of the model - which is especially reflected when pricing subordinated debt - we argue that the pricing of each individual tranche should be based on the likelihood of various recoveries to be realised. This is achieved by calculating the price of the individual debt tranche under different scenarios of α ranging from 0-1 which implies that the debt will be priced where $V_{i,0} \geq (1 - \alpha)V_B$ and $V_{i,0} \leq (1 - \alpha)V_B$. The

⁴ Leland (2006) provides a solution in which a simple mixed jump-diffusion process for firm value is treated. This will however not be included in this paper.

price returned in each individual scenario is then weighted by the probability of the specific recovery to be returned to investors.

We have chosen only to change the fraction lost to bankruptcy costs and let V_B remain constant. The reason is that changing both alpha and V_B does not necessarily provide a more accurate result, but merely returns more scenarios of the actual recovery returned in case of bankruptcy. In this way, the changes applied to alpha are meant to represent the combination of the two abovementioned uncertainties.

The individual debt tranches are still priced according to priority. However, the prices are obtained under various scenarios corresponding with expected probability of the specific recovery achieved. We have chosen to let the probability follow that of a binomial distribution which easily handles the determination of whether recovery is achieved or not. By including $\alpha = 0$ the scenario where debt is returned at maturity is represented.

7.4. CHAPTER SUMMARY

On the basis of the theoretical approach for valuation of corporate debt provided by Leland (1994), we have derived a model which handles subordination of debt when treated as a coupon bond. This implies that the senior most secured debt will only be affected according to its share size, while the most junior debt will be affected severely as it in addition to its own risk carries the risk of all debt senior to it. In addition, the deterministic drawback of the model has been limited by assuming various recoveries can be obtained when bankruptcy actually occurs. This is achieved by calculating the price returned under different recoveries weighted by the probability of the specific fraction lost to bankruptcy. With this approach the priority of the individual debt tranches remains unaffected and no tranche will be priced as a risk free investment.

8. THEORETICAL FRAMEWORK OF INPUT ESTIMATION

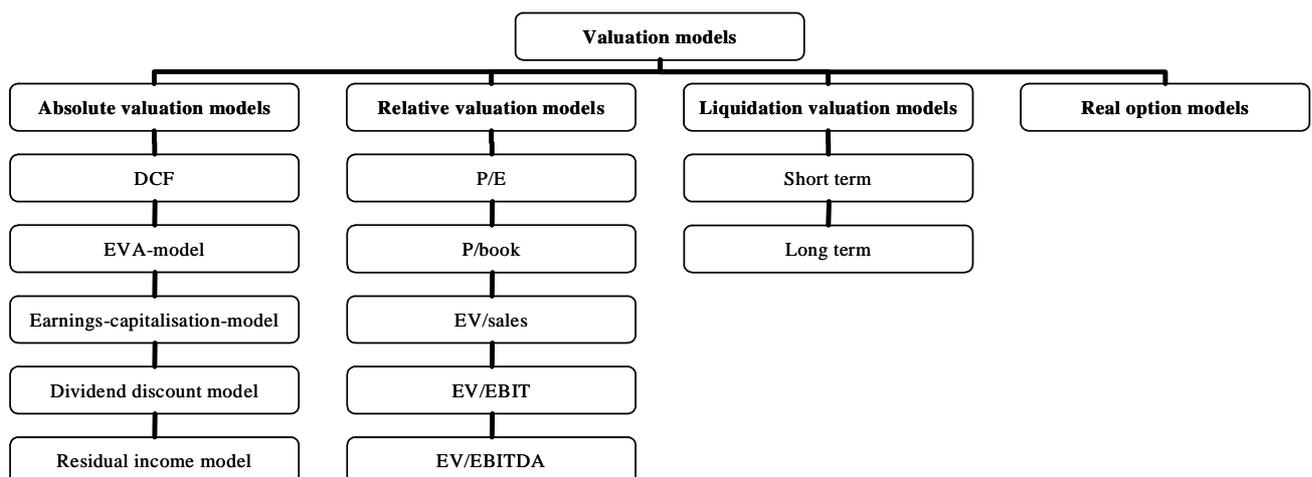
This chapter concerns approaches for estimation of the inputs needed in the model framework. Following a brief introduction of the different valuation methods available, the relative valuation approach is examined. In relation to this, the application of EBITDA will be discussed. Subsequently, we turn to the estimation of volatility and in continuation hereof, whether to measure volatility of the stock or of the enterprise value. Finally, the complicated matter of determining the fraction lost to bankruptcy costs is examined.

The following relies on McClure (2006), Plenborg & Petersen (2005), Raahauge (2009), Smith (2007), Zucchi (2006). In addition to this personal communication with Christiansen (2009) and Skødeberg (2009).

8.1. ESTIMATING ENTERPRISE VALUE

Determining a fair value of a company is a complicated and time consuming process. Being able to estimate the right inputs used in the chosen valuation model demands a comprehensive analysis within strategy, accounting and finance. The range of different valuation methodologies can be divided into four fundamental categories depending on their approaches. Figure 8.1 illustrates these, as follows:

Figure 8.1: Valuation models



Source: Plenborg (2000)

Several studies show that the absolute and relative valuation methodologies are the most widely used in practise. The usage of the different models within each of the two categories varies according to the specific purpose and surroundings of the company.

The liquidation method is typically only used in connection with companies experiencing a financial crisis while real options barely applies in situations characterised by great uncertainty about the future development.

We have chosen to apply a relative valuation approach in the later ISS case, because EV/EBITDA is a commonly accepted multiple indicating the cash flows ability to cover the purchase price of leveraged buyouts. As a consequence, the following sub-sections contain a brief introduction to general market multiple analysis and a theoretical exposition of our specific use of the EV/EBITDA multiple.

8.1.1. Relative Valuation Approach

Relative valuation is often referred to as a “quick and dirty” way to determine the value of a company. Consequently, the utilisation of comparative multiples is among the favourite valuation methodologies in practise. The underlying concept is straightforward: The value of a company is determined in relation to how comparable companies are priced in the market. Among public traded peers the procedure is as follows:

- Create a list of comparable companies⁵ (industry peers) and obtain their market values.
- Convert these market values into comparable trading multiples, such as P/E, price-to-book, EV/EBIT or EV/EBITDA.
- Utilise the multiples of the peers to calculate a fair value of the target company.

The general problem concerning comparative multiples is the misleading assumption of the procedure as a convenient and simple approach. This is simply a theoretical mistake which easily can lead to wrong conclusions. In order to compare trading multiples within peer-groups⁶ the following fundamental assumptions must be satisfied:

⁵ Alternatively, data from previous comparable transactions can be used.

⁶ Companies within the same industry

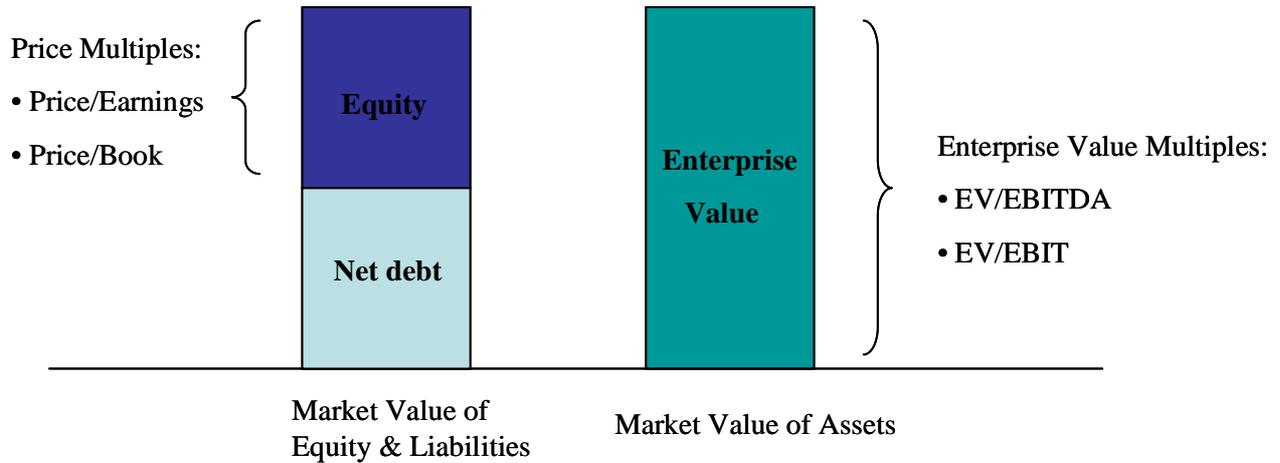
- The companies must bear the same risks⁷
- The same accounting principles must be applied
- The expected growth rates must be equal

It is obvious that such “carbon copies” do not exist in any industry. Theoretically, this leads to a necessary adjustment of the multiples, reflecting the different surroundings in which the companies find themselves. In practise, this implies that there are typically substantial differences in the companies’ valuation multiples within the same peer group. Whether a company is traded at a discount or premium to its peers is normally determined by a mixture of several factors within all of the above mentioned areas. Effectively, the challenge for investors is to spot the fundamental differences between comparable companies that might affect the multiples. This enables the investor to figure out whether a specific company deserves a higher or lower multiple than its peers.

Enterprise multiples estimate the value of a company on a debt-free basis. In this way the effect of financial gearing is avoided. EBIT is typically applied in the denominator which ensures consistency as this effectively measures earnings, assuming the company to be debt-free. To avoid possible differences in depreciation policies, EBITDA may be preferable (clarified in the following section). Figure 8.2 illustrates how the multiples EV/EBIT and EV/EBITDA look at a company as a potential acquirer would - taking debt into account. Financial ratios like P/E or P/Bonly look at the equity side of a company. Consequently, the latter ratios are simply not appropriate when a company’s enterprise value needs to be estimated.

⁷ This includes financial as well as operational risk

Figure 8.2: Relative Valuation Multiples



Source: Own Construction

8.1.2. The Utilisation of EBITDA

EBITDA is the most appropriate figure when calculating the enterprise value of a leveraged buyout according to industry practise. First of all, it is used as a figure to determine whether a company is expected to generate sufficient cash flows to service its debt in the near future. This is exemplified in its appearance as a key figure in the maintenance covenants outlined in the credit agreement. In addition to this, EBITDA is the point of origin when determining at what price the target company is bought. Effectively, the EV/EBITDA multiple is a widely accepted indicator of how easily the cash flows will be able to cover the purchase price within the leveraged buyout industry.

Based on this EV/EBITDA is applied in our later calculation of the enterprise value of ISS. In this relation, it could be interesting to examine whether the practical approach can be supported from a theoretical point of view.

In general, applying EBITDA as a single measure of cash flows can be very misleading. One way to illustrate this is by running through a typical cash flow statement, as depicted below.

Figure 8.3: Cash Flow Statement

	Sales Revenue		
-	Operating Costs		
=	Operating Profit (EBIT)	}	= EBITDA
+	Depreciation and Amortisation		
-	Taxes (from Operating Profit)		
=	Cash Earnings		
+/-	Change in Working Capital (Current Assets and Current Liabilities)		
=	Cash Flow from Operations		
+/-	Net investments		
=	Free Cash Flow (Available to Lenders and Owners)		

Source: Plenborg (2002)

Starting with the operating profit (EBIT), we add the non-cash items - depreciation and amortisation - to obtain EBITDA. At this point in the cash flow statement, we get to the measure which is commonly used in the leveraged buyout industry as a shortcut to estimate what is essential: The cash flows available to investors. However, in order to use EBITDA as a true measure, reflecting the actual cash flow, it needs to be adjusted with respect to the main differences between the two items. Working our way down the cash flow statement, it appears that there are several factors which are not incorporated in EBITDA, but still affects the cash flow. The most important ones are: (1) Net Working Capital (NWC) and (2) Capital Expenditures (CAPEX).

Changes in working capital are the cash needed to cover day-to-day operations. Private equity funds are known to pay great attention to the optimisation of operations due to their high leverage. In their attempt to make the company as lean as possible, minimisation of net working capital is an area of great importance. According to leveraged finance specialists, it is, thus, widely accepted that NWC is left out when predicting the future cash flows.

Capital investments are typically sized according to the current conditions of the company. In periods characterised by lower earnings a company will usually attempt to minimise its capital investments, whereas higher earnings allows for increased capital expenditures. As a result, CAPEX appears to disturb the transparency in the actual cash flows generated from the

underlying business. Thus, including CAPEX in determining the expected cash flows available to service debt holders can provide a misleading result. From a lender perspective it is actually more important to know what a company generates in cash flows before capital expenditures. Effectively, the negligence of capital expenditures in EBITDA seems of little importance.

Although it can be argued that capital expenditures should not be included when determining the expected cash flows available to service debt holders, they cannot completely be ignored.

Even though depreciation and amortisation are non-cash items added back to EBIT, they will inevitably become relevant as equipment wears out. As a result, EBITDA should be subtracted an amount reflecting the expenses needed to upgrade or replace worn out equipment to achieve a more accurate measure of the actual cash flow.

In this relation, it would be obvious to set CAPEX equal to depreciation. However, this will often not provide the true picture of the needed capital investments, as certain assets, like buildings and cars, are depreciated according to accounting principles - generally not reflecting their true wear. Instead it is more important to understand the underlying operations generating the cash flows. In this way the needed capital investments to achieve a steady state can be found. This level of capital expenditures is referred to as "maintenance CAPEX" and is highly dependent on the investment needs within the specific industry. Thus, EBITDA should theoretically be subtracted the maintenance CAPEX to achieve a more accurate measure of the cash flows available to service the debt holders. However, estimating maintenance CAPEX is a subjective assessment and it can be discussed if adjusting EBITDA for this amount gives a truer picture than neglecting it.

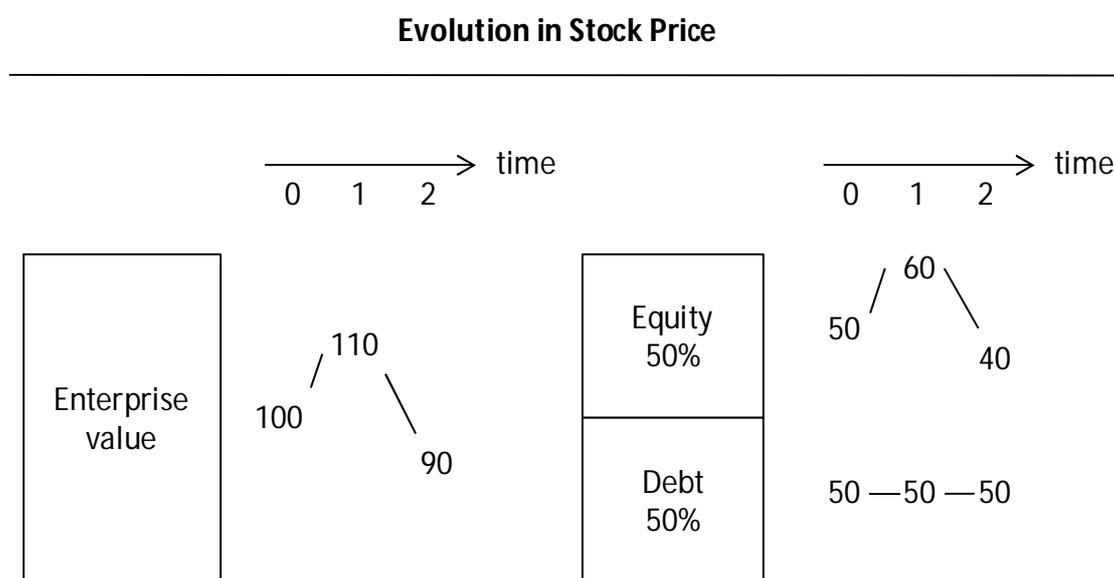
When all is said and done, "cash is king" still applies, since cash flows show the true profitability of a company. From this perspective, the utilisation of EBITDA as a single measure of the actual cash flow can therefore be very misleading. However, regarding leveraged buyouts, the need for cash is a crucial matter - making EBITDA a better proxy of the true cash flows relative to other companies. Effectively, we argue that the practical utilisation of EBITDA, as a measure of a company's ability to service debt, can be supported from a theoretical point of view.

With the correspondence between the practical approach and the theoretical foundation, we find that an application of the EV/EBITDA multiple will allow us to achieve an appropriate estimate of the enterprise value of ISS.

8.2. ESTIMATING VOLATILITY

Initiating the procedure of estimating volatility involves a determination of whether to measure the volatility on the stock or on the enterprise value. Especially when concerning highly leveraged companies the difference between the two becomes significant. As illustrated in figure 8.4, it appears how volatility on the stock increases as the debt share in the capital structure increases.

Figure 8.4: Volatility on Stock versus Enterprise Value



Source: Own Construction

On the left hand side the enterprise value of the unleveraged company evolves from 100 to 110 and finally 90. On the right hand side the same evolution occurs in the leveraged company. When debt is kept constant at 50, the stock price must reflect the total changes occurring in enterprise value over time. Thus, the stock price moves from 50 to 60 and finally 40. Percentage-wise this implies that volatility is double that of the unleveraged company.

In the model framework, volatility refers to the value of the assets and therefore the volatility implied becomes on the enterprise value. Faced with the task of estimating the volatility without any available enterprise values, it leaves us with one of two choices: (1) "Historical" volatility and (2) Peer group volatility.

In the case where the company previously has been listed, the historical volatility can be obtained. This is of course a question of assessment concerning the timeframe the company

has been de-listed and the amount of available historical values obtainable. The second approach is to estimate the volatility by measuring the historical volatility of a peer group of listed competitors where enterprise values are available. The latter will be the approach utilised in this paper, as this includes the impact on volatility resulting from the financial crisis.

To estimate volatility we have chosen to employ the Equally Weighted Moving Average (EWMA) approach⁸. This is described by following equation

$$\hat{\sigma}_t^2 = \frac{1}{N} \sum_{i=1}^n r_{t-i}^2$$

To begin with we must obtain a time series of the underlying asset. The time period selected should be limited when an estimation of the current volatility is desirable. However, the shorter the period the higher are the chances of estimation errors. In short, this means a tradeoff between precision and relevance. Since we initially are unable to tell which time span will create the best result we employ the Root Mean Squared Error (RMSE) approach to measure the fit. This is described in the equation below

$$RMSE = \sqrt{\frac{1}{T} \sum_{t=1}^T (r_t^2 - \hat{\sigma}_t^2)^2}$$

RMSE measures the average distance between the realised and predicted volatility. The time length resulting in the smallest *RMSE* is preferable.

8.3. THE FRACTION α LOST TO BANKRUPTCY COSTS

Determining the fraction lost to bankruptcy costs is a very complicated matter. The extensive amount of empirical studies, which, in vain, have struggled to provide a fair estimate of the costs associated with bankruptcy, indicates the degree of complexity surrounding the approach. Consensus in the performed studies is, however, achieved concerning which factors

⁸ Since the focus of this paper is on pricing of leveraged loans and not volatility estimation, we will refrain from employing several models to find the best measure of volatility.

are the most influential. In general, bankruptcy costs can be divided into two categories: (1) Direct costs and (2) Indirect costs.

The direct costs mainly consist of tangible expenses such as fees to lawyers, accountants, restructuring advisors, turnaround specialists, etc.. With these expenses relatively easy to identify it seems reasonable to believe that a fair estimate can be achieved.

The indirect costs consist of an extensive range of unobservable opportunity costs. For example, customers opting out on dealing with a firm entering bankruptcy might result in lost sales and profits. The firm may as well face increased costs related to poorer terms with suppliers due to the financially vulnerable position. Furthermore, lost opportunities resulting from management's diversion - running a distressed firm - is also included in the indirect costs.

From an investor perspective, predicting the unobservable effects, resulting from entering financial distress and the subsequent bankruptcy, is more or less impossible. Therefore, the best estimation will often rely on historical industry specific recovery rates along with empirical studies of similar firms, assuming these studies display relatively high consistency.

8.4. CHAPTER SUMMARY

In the process of determining the most appropriate valuation method for estimation of the enterprise value, we find that market participants in general apply the EV/EBITDA multiple approach. The underlying reasoning is that leveraged buyout practitioners primarily focus on how well cash flows of the acquired company can cover the purchase price. In this relation, EBITDA is generally assumed the best proxy for the actual cash flow.

With respect to its later application, volatility is to be found on the enterprise value utilising the Equally Weighted Moving Average approach. In addition, the Root Mean Squared Error is employed to ensure the most accurate estimation is chosen. Finally, we found that the task of determining the fraction lost to bankruptcy costs is a process of great difficulty surrounded by high uncertainty. The best estimate will in this relation rely on historical recovery rates and empirical studies.

PART 5

In part 4 Leland's model framework was extended to handle subordination of debt. To circumvent the deterministic drawbacks of the model, prices should be obtained under various scenarios of alpha weighted by the possibility of their occurrence. The subsequent examination of input estimations, revealed the most appropriate approaches. Effectively, we are now capable of pricing leveraged loans from a theoretical point of view.

In this way, part 4 provides a derivation of a theoretical approach to pricing leveraged loans.

Part 5 includes chapter 9, 10 and 11. The section contains a case study of ISS in which the institutional knowledge concerning the leveraged loan market and the derived model for pricing leveraged loans are applied. Beginning with an estimation of the various inputs needed in the model framework, the section moves on to an actual model implementation. This provides us with the prices of ISS's individual debt tranches. Subsequently, we compare the prices returned by the model with actual market prices. Finally, the part summarises the finding of the thesis in the conclusion

	Problem Identification and Method	Chapter 1
Part 1	<div style="display: flex; justify-content: space-around; margin-bottom: 5px;"> Syndicated loan market Leveraged loans </div>	Chapter 2 & 3
Part 2	CLO structure	Chapter 4
Part 3	<div style="display: flex; justify-content: space-around; margin-bottom: 5px;"> Analysis of primary leveraged loan market Analysis of secondary leveraged loan market </div>	Chapter 5 & 6
Part 4	Theoretical framework for pricing corporate debt	Chapter 7
	Theoretical frameworks for estimation of input variables	Chapter 8
Part 5	Estimation of input variables	Chapter 9
	Analysis of results from the model	Chapter 10
	Conclusion	Chapter 11

9. INPUT ESTIMATION

In the following chapter, the methods for estimation of model inputs are executed. This entails an initial peer group analysis, the result of which is applied in the following estimation of enterprise value and volatility. Concurrently, different factors influencing the estimation of these values will be discussed. Subsequently, we determine the fraction lost to bankruptcy costs based on an empirical approach. Finally, the tax rate and the risk free interest rate is found.

9.1. THE ISS CASE

In 2005, the world's largest cleaning services company, ISS A/S, was bought in a leveraged buyout transaction performed by the private equity funds EQT and Goldman Sachs Capital Partners. ISS was bought through the newly created vehicle, PurusCo A/S, of which EQT owned 55% and Goldman Sachs 45%.

The outstanding share capital of ISS was bought at DKK 470 cash per share, which reflected a premium of 31.3% to the last trading day prior to the firm announcement of the offer. In this relation PurusCo received valid acceptance representing 91.55% of the outstanding share capital after which a mandatory takeover for the remaining shares was launched.

The offer price valued the entire listed share capital of ISS at DKK 22.25 billion. In addition to equity, the transaction was funded through the issuance of debt secured by the shares of ISS, referred to as leveraged loans. The lead arrangers were Citigroup and Goldman Sachs in cooperation with Danske Bank, Nordea, Den Norske Bank, HSBC, HVB, and Societe General. The debt facilities were successfully syndicated to a broad array of international banks and funds, including all of the larger Nordic banks.

In addition to the entire listed share capital, PurusCo would assume DKK 6.338 million EMTN (due 2010) and DKK 1.118 million EMTN (due 2014) issued by ISS.

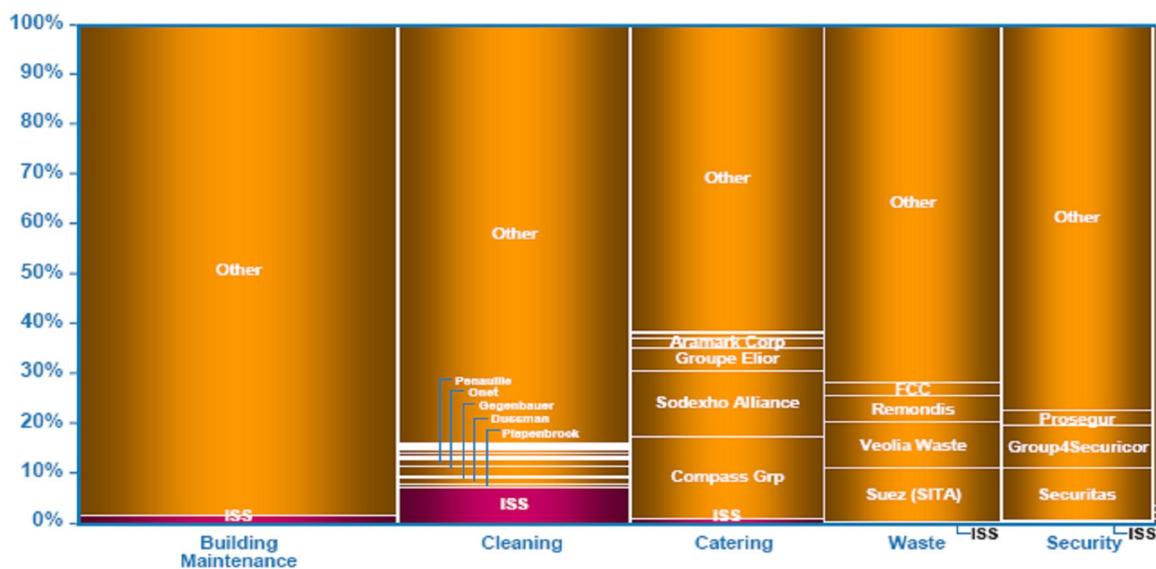
With an EBITDA of DKK 2.889 million (ending year 2004) the purchase was effectively realised at a multiple of 10.5 times EBITDA.

9.2 PEER GROUP ANALYSIS

In our estimation of ISS's enterprise value, and subsequent volatility, we rely on peer group estimates to provide a true and fair view of the evolution of ISS, since it was de-listed. To identify the most suitable peers, we will initially scan the industry in which ISS operates.

ISS is characterised as a company within the industry concerning integrated facility services (IFS), which is a somewhat diffuse business segment. The industry can be divided into 5 different services in an attempt to generalise the operating fields. These constitute property management, cleaning, security, catering and office support. The most significant players are represented by roughly a handful of businesses which are ISS, Compass Group, Sodexo, G4S, Rentokil, Mitie, Aramark, and Serco.

Figure 9.1: Competitive Landscape



Source: ISS Prospect (2005)

Characteristic to the industry of IFS is that none of the players possess significant market shares in more than one of the services. This indicates that each company specialises within a single service, and provides the rest in order to fulfill the concept of IFS.

Furthermore, each of the different service segments is only covered by a small percentage of the providers of IFS. This suggests that while a company might be large with respect to IFS, its market share within a single service could easily be of a small magnitude when compared to total market size. In the case of ISS, this is exemplified in its presence within the cleaning segment. Even though cleaning services is their core business, and they possess a position as market leader, their share of the total market is relatively small. For example, in Denmark alone, ISS must compete against 3-4 thousand cleanings companies whose accumulated market share naturally exceeds that of ISS.

In the process of identifying suitable peers, some of the above mentioned competitors were initially excluded due to operations within areas other than IFS. Consequently, the effects of these additional operations would be reflected in the obtained multiples - resulting in an incorrect foundation. Furthermore, some have been excluded as a consequence of not being listed. This is inevitably a requirement when peers are utilised with respect to obtaining trade multiples.

To obtain the most accurate peer group among the remaining companies, the peers selected should carry similar characteristics to those of ISS. In this respect, the characteristics identified as being most influential are growth, strategic position, and operational risk (as described in section 8.1.1). Analysis performed on each individual competitor reveals that Sodexo, Compass Group, and G4S (formerly Group 4 Securicor) possess similar characteristics to those of ISS.

Firstly, in recent years, growth rates have resembled each other - primarily achieved through aggressive acquisition strategies.

Secondly, all companies possess a dominating strategic position within their respective field of core operations, as illustrated in figure 9.1.

Finally, even though the services within their different core businesses are not alike, the operational risk associated is fairly assumed similar, as the industries in question carry relatively consistent characteristics. The companies alike provide services through long term contractual agreements which ensure relatively stable earnings.

We recognise the fact that three companies constituting a peer group analysis could be considered a relatively small foundation. However, emphasis on the correctness of peers is preferred as opposed to the share basis of comparison.

9.3. ESTIMATION OF ENTERPRISE VALUE

As described in the theoretical part of the paper, the estimation of the enterprise value of ISS will be performed on the basis of a multiples analysis. The basic idea is to find the average trading multiple of the peer group compared to ISS at the time of the takeover. This returns a ratio at which ISS was traded, compared to its peer group. The multiple ratio is then applied to year end 2008 multiples of the peers - providing a fair estimate of the current ISS multiple.

The analysis is initiated by obtaining market capitalisation and net debt of the peer group and ISS before it was de-listed. The enterprise values are then divided by the corresponding EBITDA

of the same period, which yields the trading multiple EV/EBITDA. These results appear in table 9.2.

Table 9.2: EV/EBITDA Multiples

Company	Multiples						
	EV/EBITDA 04	EV/EBITDA 29/03/2005	EV/EBITDA 05	EV/EBITDA 06	EV/EBITDA 07	EV/EBITDA 08	EV/EBITDA 31/03/2009
G4S	9,1	9,3	8,2	8,5	12,6	10,5	5,7
Sodexo	6,1	6,9	8,7	10,5	8,2	7,6	6,3
Compass	7,5	7,7	7,6	10,5	9,4	8,5	5,9
Average	7,6	8,0	8,2	9,8	10,1	8,9	6,0
ISS	7,6	10,5					
ISS Adjusted	7,6	8,6					8,0

Source: Own construction

Trading multiples obtained at the day of the buyout, are based on realised 2004 EBITDA, while market cap are actual figures of the current time and net debt is adjusted⁹ for the purpose. On the basis of these figures an EV/EBITDA multiple of the ISS transaction is 10.5x.

When the leverage buyout of ISS was performed in March 2005, the acquisition was completed at a price in which a considerable premium of 31.3 % was included. This premium reflected expectations of increased earnings contained in concentrated ownership. We assume that, during the four years in which ISS has been de-listed, these opportunities have been fulfilled and are, thus, contained in the current EBITDA. Consequently, the premium paid should not be reflected in the current multiple as the higher enterprise value is now expressed through the increased EBITDA. This implies that the multiple of 10.5x should be cleansed of the premium when applied as the foundation on which the multiple ratio is based. Calculating market cap less premium and solving for the adjusted multiple yields 8.6x. This provides the multiple ratio $8.6/8.0 = 1.075$ of which ISS traded to its peer group at the time of the takeover.

In our peer group analysis we carefully selected comparable companies which we assume carry the same risk and similar growth expectations as that of ISS. The assumption of “carbon copies” allows us to transfer the multiple ratio obtained from the day of the buyout directly, up to

⁹ The method of adjusting the debt is provided in section 9.4

today. Applying the multiple ratio to the average peer group EV/EBITDA multiple, based on 2008 figures, results in an estimated ISS multiple of 9.6x¹⁰.

However, the general assumption is that the stock market is traded on expectations for the future. An approach built on expectations for EBITDA 09 of the peers, returns an estimated ISS multiple of 6.5x. In light of the unpredictable market conditions following the credit crisis, the uncertainty surrounding expectations to 2009 is, in our assessment, too great to be fully relied upon. It is evident that investors will not fully reward the expectations of an increased EBITDA in conditions of high uncertainty.

Based on the considerations of uncertainty, we assume that an equally weighted average of the two estimates, provided by realised EBITDA 08 and expected EBITDA 09, satisfies a true and fair estimate of the actual ISS multiple today. This results in a final ISS multiple of 8.0x EV/EBITDA. In the perspective of current buyout activity, the achievement of a trading multiple of 8.0x seems rather realistic. In section 5.2, we provided evidence that current leverage buyouts are on average executed at 7.9x EV/EBITDA.

With the given multiple we are now able to find the estimated enterprise value of ISS end year 2008. This is achieved simply by multiplying EBITDA with EV/EBITDA, which returns an estimated enterprise value of ISS = 4936.5¹¹ * 8.0 = DKK 39.492 billion.

9.4. ESTIMATION OF VOLATILITY

When estimating the volatility of the enterprise value of ISS, peer group characteristic is once again utilised. The following calculations appear in full in appendix B and C which are based on figures provided by Factset (formerly JCF).

Estimation of volatility is initiated by calculating the enterprise value of each company on a daily basis beginning from 01/01/2004 to 31/12/2008. In the case of ISS the enterprise is derived until it was de-listed as of 29/03/2005. In order to perform these calculations we need to obtain daily share values, shares outstanding and net debt. While share values are easily obtained, shares outstanding and net debt are not widely available on a daily basis. In an attempt to circumvent this problem, shares outstanding and net debt is obtained on a yearly basis. To create an evolving development throughout each year, the difference from year to

¹⁰ 8.9x * 1.075 = 9.6x

¹¹ Since we have applied an equally weighted EBITDA to the peers we utilize an equally weighted EBITDA of ISS as well. Realized EBITDA 2008 was 4837 and expectations to EBITDA in 2009 are 5036.

year is divided by the number of trade days in between. This creates a fraction which is added/subtracted for each day moving forward to get the day by day evolution. Although shares outstanding and net debt do not evolve at the exact same fraction consistently during each year, we assume this approach satisfies the actual evolution within each company.

On the basis of the estimated parameters above, enterprise values are calculated on a daily basis. The enterprise values are then treated as returns in the equally weighted moving average approach, where they are taken as inputs to volatility estimation. We have chosen to measure the annualised historical volatility for each specific day based on an average of 2 month, 1 month, 2 weeks, and 1 week. In order to estimate which of the four time frames provide the best fit, we perform a Root mean Squared Error (RMSE) analysis. This reveals how well the historical volatility predicts the excess change the following day. The period providing the smallest result is the best measure.

Table 9.3: Root Mean Squared Average

Root Mean Squared Average								
Date	29-03-2005				31-12-2008			
Time frame	2 month	1 month	2 week	1 week	2 month	1 month	2 week	1 week
G4S	0,0002849	0,0003164	0,0003349	0,0003492	0,0003715	0,0003741	0,0003787	0,0003812
Sodexo	0,0005559	0,0005425	0,0005497	0,0005614	0,0007086	0,0006993	0,0007041	0,0007328
Compass	0,0027193	0,0026540	0,0008454	0,0011655	0,0014912	0,0014935	0,0006815	0,0008309
ISS	0,0001279	0,0001280	0,0001290	0,0001344				

Source: Own Calculations

We find that RMSE differs between each company within the peer group. However, this has no influence when calculating the average peer group volatility, as it is only an expression of the best measure. The standard deviations obtained from differentiating time frames across the companies are not affected.

We now pick the volatilities at the two given dates of each company corresponding with the time frame providing the best fit. The volatility of ISS is compared to the peer group on the day before its de-listing. The ratio between ISS and its peers is forwarded to the average volatility of the peer group as of 31/12/2008. This returns the estimated volatility of ISS at 0.22.

Table 9.4: Volatility

Volatility		
Date	29-03-2005	31-12-2008
G4S	0,23	0,30
Sodexo	0,21	0,38
Compass	0,10	0,32
ISS	0,12	0,22

Source: Own Calculations

9.5. DETERMINATION OF BANKRUPTCY COSTS, TAX, AND RISK FREE RATE

We have chosen to direct our focus on empirical studies performed on highly leveraged firms due to the high degree of uncertainty and complexity in estimating the fraction lost to bankruptcy costs. Studies by Bris, Welch and Zhu (2004) estimates that direct costs amount to 9.5% while Andrade and Kaplan (1998) estimates the indirect cost of financial distress to be somewhere between 10 to 20 % of firm value. By adding these findings the total bankruptcy costs seem to be in the area of 20 - 30 %.

Turning our attention towards more industry specific recovery rates a Credit Suisse rapport (Blau et al., 2008) states that the recovery rate of leveraged loans in the service sector have been 49.5 percent in LTM September 2008. Comparing a fraction lost to bankruptcy costs of 50.5 percent with the findings of the empirical studies reveals relatively large inconsistencies. However, considering the characteristics of ISS and the industry in which it operates it seems reasonable that the service sector will be affected more severely than the average industry findings in the empirical studies. Consequently, we have chosen to rely on the industry specific recovery rate which yields a fraction lost to bankruptcy costs at 50.5 percent.

The tax rate applied in the model is the effective tax rate calculated from the annual report of 2008 of ISS which is 15.5 %¹².

The risk free rate is obtained from a Danish government bond with a maturity of 10 years. As of 31/12/2008, the effective rate was 3.4 percent (Nationalbanken, 2009).

¹² This is achieved by dividing taxes paid with pre-tax profit.

9.6. CHAPTER SUMMARY

In the estimation of the enterprise value we found the leveraged buyout transaction of ISS was performed at an EV/EBITDA multiple of 8.6x excluding the premium paid. Utilisation of comparative multiples determine the present ISS multiple at 8.0x. Effectively, the present enterprise value of ISS is DKK 39.492 million.

The volatility estimation was similarly performed on the basis of peer group comparison. Applying the EWMA approach we found the present volatility of ISS to be 0.22.

The fraction lost to bankruptcy costs is determined at 0.505 based on the historical industry specific recovery rate of leveraged buyouts. Finally, we found the effective tax rate of ISS to be 15.5 percent, while the risk free interest rate was determined at 3.4 percent.

10. THE PRICING OF ISS'S DEBT

With the general inputs obtained and estimated where necessary, we now turn to the task of pricing the debt of ISS. The different facilities constituting the debt structure of ISS as of 31/12/2008 are depicted in table 10.1.

As described at the beginning of the paper leveraged loans are structured with floating rate coupons. With the model not allowing for changes in coupon payments, the base rate is assumed fixed at LIBOR 3 as of 31/12/2008. For the sake of simplicity, all tranches are assumed issued in the same currency. With 91 % of ISS' total debt issued in Euros, we choose to employ the LIBOR 3 rate denoted in Euros. As a result a constant coupon payment is achieved.

Table 10.1: ISS Debt Structure 31/12/2008

ISS Debt Structure 31/12/2008						
Facility	Principal MDKK	Percentage of Total Debt	x EBITDA 2008 PF	Base Rate	Cash Margin	Cash Coupon
Senior	17.591	53,96	3.6x	2,894 %	2,375 %	5,269 %
EMTN	7.155	21,95	1.5x	0,000 %	4,750 %	4,750 %
Second Lien	4.471	13,71	0.9x	2,894 %	4,500 %	7,394 %
Senior Sub Notes	3383	10,38	0.7x	0,000 %	8,875 %	8,875 %
Total Cash Pay Debt	32.600	100 %	6,7x	1,958 %	3,862 %	5,821 %

Source: Own construction based on data from ISS (2009)

With the given debt structure we are now able to find the value of each debt tranche individually. As previously mentioned this is performed with various recoveries weighted by the probability of their occurrence. The fraction lost to bankruptcy is varied to reflect the uncertainties in determining the actual recovery achieved.

The probability of the various recoveries is constructed to follow a binomial distribution. Success (s) is defined as receiving recovery and failure (f) is defined as not receiving recovery. In section 9.5 we found that the industry specific recovery rate of leveraged loans within the service sector is 49.5%. This entails that success occurs with probability 49.5% and failure with probability 50.5%. We have chosen to execute 5 trials which will provide 6 different outcomes of alpha. The following scenarios of the fraction $\alpha = \{0; 0.2; 0.4; 0.6; 0.8; 1\}$ represent possible outcomes of obtained recovery. Table 10.2 provides the probability of their occurrence.

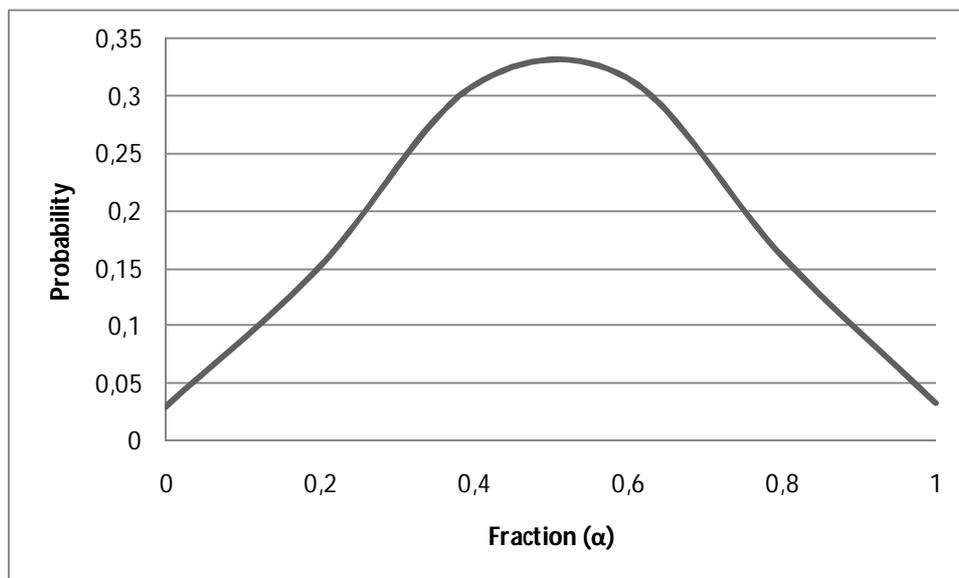
Table 10.2: Probability Distribution

Binomial Distribution						
α	0	0,2	0,4	0,6	0,8	1
u	sssss	ssssf	sssff	ssfff	sffff	fffff
P(u)	0,0297	0,0303	0,0309	0,0316	0,0322	0,0328
X	1	5	10	10	5	1
P(X)	0,0297	0,1516	0,3093	0,3156	0,1610	0,0328

Source: Own Calculations (See Appendix D)

The binomial probability distribution in figure 10.3, displays the probability of all possible scenarios of alpha occurring.

Figure 10.3: Binomial Probability Distribution



Source: Own Construction

The approach incorporates an element of uncertainty of alpha and thereby avoids the deterministic drawbacks consisting of pre-determination of recovery. From the theoretical framework, we know that the individual debt value consists of two parts: (1) The discounted return on the continuous compounded coupons until bankruptcy occurs, and (2) The discounted return on the obtained recovery. We have chosen to let V_B remain fixed in order not to affect the determination of when bankruptcy is declared, expressed by $\left(\frac{V}{V_B}\right)^{-x}$. This

implies that the former remains constant at all times, while the latter is affected by the different values of α .

We are now able to initiate the model calculations. The different parameters required in the model framework are listed in table 10.4.

Table 10.4: Model Inputs

Estimated and obtained values	
Enterprise Value (V)	39.492
Volatility (σ)	0.220
Fraction lost to Bankruptcy (α)	0.505
Tax Rate (τ)	0.115
Riskless Rate (r)	0.034
Constant Base Rate (LIBOR 3)	0.029

Source: Own Construction

It is worth noting that the fraction lost to bankruptcy at 50.5 percent works as our foundation in determining the possibilities of achieving various recoveries.

With the inputs employed in the model we obtain the price of ISS's debt in the different scenarios of α . These are provided in the table 10.5.

Table 10.5: ISS Debt Prices in Various Scenarios of Alpha

Price Calculation in Various Scenarios												
Facility	Principal MDKK	Price when $\alpha = 0$	Price when $\alpha = 0.1$	Price when $\alpha = 0.2$	Price when $\alpha = 0.3$	Price when $\alpha = 0.4$	Price when $\alpha = 0.5$	Price when $\alpha = 0.6$	Price when $\alpha = 0.7$	Price when $\alpha = 0.8$	Price when $\alpha = 0.9$	Price when $\alpha = 1.0$
Senior	54%	112,98	112,98	112,98	112,98	112,98	107,38	93,22	79,07	64,92	50,76	36,61
EMTN	21%	109,38	109,38	109,38	88,82	54,02	33,00	33,00	33,00	33,00	33,00	33,00
Second Lien	14%	127,75	127,75	74,16	51,37	51,37	51,37	51,37	51,37	51,37	51,37	51,37
Senior Sub	11%	138,04	64,44	61,66	61,66	61,66	61,66	61,66	61,66	61,66	61,66	61,66

Source: Own Calculations (See Appendix E)

It appears how the priority of the different tranches is in correspondence with their respective claims to achieved recovery. This is for example seen in the senior subordinated tranche which is affected as soon as alpha is increased from 0 to 0.1. The tranche is precluded from receiving recovery as alpha increases to 0.2. At this point the second lien tranche becomes affected which corresponds with the size of the senior subordinated tranche and the two tranches individual placement in the capital structure. The price of the senior tranche is not affected until the fraction lost to bankruptcy costs exceeds 50 percent.

With the implementation of the probability distribution, the prices of the different tranches are derived. The results are shown in table 10.6.

Table 10.6: Prices Weighted According to Probability

Prices According to the Probability of Achieved Recovery							
Facility	Price when $\alpha = 0$ probability 0.03	Price when $\alpha = 0.2$ probability 0.15	Price when $\alpha = 0.4$ probability 0.31	Price when $\alpha = 0.6$ probability 0.32	Price when $\alpha = 0.8$ probability 0.16	Price when $\alpha = 1.0$ probability 0.03	Total Price
Senior	3,36	17,13	34,95	29,42	10,45	1,20	97
EMTN	3,25	16,58	16,71	10,41	5,31	1,08	53
Second Lien	3,80	11,24	15,89	16,21	8,27	1,69	57
Senior Sub	4,10	9,35	19,07	19,46	9,93	2,03	64

Source: Own Calculations (See Appendix D + E)

With the prices calculated according to the probability of their occurrence, we are now able to obtain the total price of each individual debt tranche returned from our model. This is achieved simply by summarising the weighted prices from the different scenarios of α .

In table 10.7 the theoretical prices returned from the model are compared with actual market prices as of 31/12/2008.

Table 10.7: Debt Prices

Facility	Prices	
	Market Price	Model Price
Senior	67	97
EMTN	84	53
Second Lien	55	57
Senior Sub	60	64

Source: Own Construction (See Appendix E)

The capital structure of ISS differentiates greatly from that of normal leverage buyouts (see figure 3.1 section 3.1). The utilisation of two fixed rate bonds in the debt structure is very unusual and especially the EMTN notes are unique to ISS. Due to the presence of this atypical debt product, we will briefly look at the result of these notes, before turning to a more general examination of the remaining prices returned by the model.

The EMTN is the only tranche returned by the model at a reduced price compared to actual market prices. According to the model the price of the EMTN should be 53, while the market price is 84. This price difference can primarily be explained by the inconsistency between the

model assumption of perpetual debt and the actual maturity of the tranche in 2010. From a theoretical perspective, the tranche is priced as all the other tranches, namely as the discounted return on the continuous compounded coupons until bankruptcy and the discounted return on the obtained recovery. However, with a repayment in the near future, market participants almost exclusively value debt according to the probability of receiving the full principal at maturity. In the case of ISS where the EMTN constitutes a minor part of the capital structure, the risk of ISS not being able to refinance the tranche is low, and therefore it is only natural that the price goes up. Consequently, the price on the EMTN returned from the model is much lower than the price observed in the market (Christiansen, 2009).

With the exception of the somewhat unusual EMTN notes, we will, in the following section, attempt to provide an explanation for the general inconsistencies between actual market prices and the prices returned by the model. These are analysed from two different approaches: (1) Practical and (2) Theoretical. The practical point of view identifies model specific sources including input errors which might pollute the returned results, while the theoretical point of view explains potential sources for any inconsistencies not model related.

10.1 PRACTICAL FOUNDATION FOR INCONSISTENCIES

The construction of the model relies on several assumptions to be satisfied, which are not in precise correspondence with actual market conditions. In the following, we will pinpoint some of the most influential ones causing price inconsistencies.

One of the factors determining the occurrence of bankruptcy is the size of coupon payments. In the theoretical approach coupon payments are assumed fixed, but the senior debt and second lien of ISS are actually based on floating rate coupons. This implies that fluctuations in coupon payments will be neglected by the model, and consequently the determined occurrence of bankruptcy could become incorrect. In defense of the model, it should be noted that leveraged companies tend to hedge substantially against their exposure to LIBOR. Nevertheless, the treatment of floating rate coupons as fixed can be a contributing factor in deviations from observed prices.

Another assumption of the model is time independence which implies that debt is issued as perpetual debt. In theory this seems to be a valid assumption as leveraged loans are issued with long term maturities. However, this approach excludes the possibility of an early repayment.

The discrepancy which arises in this respect is that leveraged loans are, in general, issued as callable debt. This necessitate that any prices more than insignificantly above par are highly unlikely to occur. Had the obtained recovery rate been slightly higher in the case of ISS, this discrepancy would have been displayed in the pricing of senior debt. Effectively, the theoretical price of the senior tranche would have been above par.

According to Torben Skødeberg, market valuation of leveraged loans is primarily based on a thorough examination of the cash flows generated by the underlying company. This is due to the fact that the cash flows are the primary determinant of bankruptcy declaration. In this way, it is important to ensure that the cash flows generated by the firm are sufficient to cover the coupon payments until maturity. The model, in contrast, assumes that the reach of a pre-determined lower value of the enterprise will trigger bankruptcy. Although there is a high correlation between cash flows and enterprise value, the two approaches can return different determinations of when bankruptcy occurs. This implies that the comparison of theoretical and market prices relies on two different valuation methods with respect to bankruptcy determination.

Finally, it is worth noting that the capital structure of ISS is not a plain vanilla example of a leveraged buyout. However, the model treats all tranches as if they were issued as leveraged loans. This can obviously lead to pricing errors with respect to the debt products, besides leveraged loans. Beyond the previously mentioned EMTN tranche, this implies that the returned theoretical price of the senior subordinated tranche might be misleading.

Several of the input variables are based on estimations which imply that inconsistencies can be caused directly from errors in the performances of these. Performing stress tests will reveal to which degree flaws in the different estimations influence the total outcome. We have chosen to perform stress tests on the variables: volatility, enterprise value and the fraction lost to bankruptcy costs. The results of which are presented in table 10.8.

Table 10.8: Stress Test

Stress Test															
Facility	-10%			-5%			0%			5%			10%		
	Volatility	EV	Alpha	Volatility	EV	Alpha	Volatility	EV	Alpha	Volatility	EV	Alpha	Volatility	EV	Alpha
Senior	100	87	100	98	92	98	97	97	97	95	100	94	94	104	92
EMTN	59	40	59	56	47	56	53	53	53	51	59	51	49	64	48
Second Lien	67	32	60	62	45	58	57	57	57	53	68	56	49	77	55
Senior Sub	76	32	65	70	49	65	64	64	64	59	77	63	54	89	63

Source: Own Calculations (See Appendix F)

The stress tests performed cover deviations from the estimated values in a range of +/- 10 percent. This provides an overview of the affects of changes in the different input variables to the individual tranches.

Basically, increasing the volatility lowers the value of X which increases the last term of the model, $\left(\frac{V}{V_B}\right)^{-X}$. This implies that the more volatile the enterprise value is, the larger becomes the determinant of when bankruptcy is declared. Naturally, these affects are reverse when decreasing the volatility. As a result, an increase in the volatility is equivalent to a more imminent reach of V_B . This will affect the prices negatively as total coupon payments are decreased. The occurrence of changes in volatility has a fairly large impact on the lower tranches whereas the most senior tranche hardly is affected. This is due to the priority of debt which implies that the lower tranches are more dependent on generating cash flows while alive compared to the senior tranche. The latter will collect the most substantial part of the returned recovery and therefore does not suffer the same exposure as to when V_B reached.

Of the three input variables, changes applied in the enterprise value prove to affect the prices of the debt tranches most significantly. The effects are the least obvious in the most senior tranche, while the two lower tranches in particular are influenced. There reasons are the same as those provided with respect to V_B when changing the volatility. However, this time V_B remains fixed while V either approaches or moves away. In addition, there exist a natural relationship between the changes applied and the effects on the prices. However, it's worth noting how negative changes entail stronger affects to the price than positive ones do. Lowering the enterprise value implies that $V \rightarrow V_B$ which indicates that bankruptcy is becoming more possible to occur. As such, the affects of the changes highly resemble those, one would expect to see in the real world.

The affects on prices when changing alpha are of a smaller magnitude compared to those of the other two variables. However, when exposed to changes alpha proves to be the only variable which affects the EMTN tranche more severely than any of the other tranches. With the given capital structure and the base case fraction this is in perfect compliance with what is to be expected. The reason being when increasing alpha the weight of the scenarios dominated by failure will increase while lowering alpha increase the influence of the success scenarios.

10.2. THEORETICAL FOUNDATION FOR INCONSISTENCIES

The model returns prices which in general are higher than actual market prices - disregarding the obvious flaw appearing in the low price of the unique EMTN. Consequently, we will attempt to locate possible issues which from a theoretical point of view can explain some of the inconsistencies not related to the model.

Even though the leveraged loan market has been strongly influenced by an increased institutional investor base, it is worth remembering that the European leveraged loan market is still affected by banks possessing a substantial market share. Leveraged loans are to some extent still treated as bank products, and therefore not yet fully driven by capital market forces as oppose to the more traditional bond market. The advantages of possessing the role as relationship bank calls for speculations concerning whether banks have been willing to issue the loans at reduced margins in order to acquire this role. The existence of loans not priced in complete correspondence with actual returns, implies a possible contortion of leveraged loan prices.

In this relation, bank credit has during the last decade evolved from the approach of the traditional relationship banking towards originate-to-distribute. In particular, the bull-run days provided banks the opportunity to originate loans, earn the fees, and then sell the loans to other investors. Studies provided by Berndt and Gupta (2008) provide evidence of a risk-adjusted underperformance of these loans of approximately 10 percent compared to other bank loans. In general, two reasons for this underperformance exist. These are adverse selection and moral hazard. The first explanation deals with banks' superior information about the credit quality of their loans, which gives rise to concerns about adverse selection. The underperformance of the loans could be explained by banks originating and, subsequently, selling bad loans based on unobservable private information. Secondly, the increasing

outdistancing to traditional relationship banking meant a severance of the bank-borrower relationship. In the absence of the discipline of bank monitoring, borrowers were provided the opportunity to undertake suboptimal operating and investment decisions. Effectively, the syndication fee structure combined with a high degree of information asymmetry calls for speculations of adverse selection and moral hazard problems within the leveraged loan market.

Based on the structure of remuneration to the CLO manager indications of a possible principal agent problem seem present. In section 6.2.2 we found that the lack of sub-fees in relation to a potential breach of the CCC-bucket may result in the CLO manager behaving opportunistically as he is left no incentive to do otherwise. Effectively, the preclusion of the substantial sub fees implies that the CLO manager would trigger insolvency which is absolutely not in the interest of the investors. However, if he cannot maintain a minimum service platform this will result in an inability to comply with operational service requirements and in the long run remain solvent.

10.3 RECAPITULATION

When comparing theoretical prices to actual market prices, we find that the model in general prices the loans higher – setting aside the inconsistencies concerning EMTN.

The theoretical prices of the two most junior tranches are only marginal above those observed in the market. This causes us to believe that the existing differences might be based on one of the identified practical factors found in section 10.1. Especially the results of the stress tests suggest that minor flaws in the estimation of input variables can explain the observed differences. We have identified volatility and enterprise value as the most likely estimated inputs to be polluted by flaws. We find that less than a 5% decrease in enterprise value would result in theoretical prices similar to market prices. Likewise, an increase of less than 5 percent in volatility returns compliant prices.

The model prices the senior tranche highly above the observed market prices. Given the magnitude of the deviation it seems unlikely that this is solely caused by practical or theoretical factors. In compliance with the knowledge obtained in the market analysis (see part 3) it appears that a liquidity premium currently is being offered in the market with respect to senior secured debt.

Assuming that the theoretical price of the senior tranche reflects the actual conditions of ISS, we have chosen to perform a calibration of the fraction lost to bankruptcy costs. This illustrates at which fraction actual market prices are traded. The results are provided in table 10.9.

Table 10.9: Calibration

Facility	Calibration of Fraction lost to Bankruptcy Cost					Market Price
	50%	60%	70%	78%	80%	
Senior	97	88	77	67	64	67
EMTN	53	44	38	35	35	84
Second Lie	57	54	52	52	52	55
Senior Sub	64	62	62	62	62	60

Source: Own Calculations (See Appendix G)

We concentrate on the senior secured tranche in our attempt to identify at which fraction lost to bankruptcy costs the loans are traded. This is because this tranche seems to be the only one offering a liquidity premium.

It appears that increasing the expected fraction highly narrows the existing gap between theoretical and market prices. With a fraction lost to bankruptcy costs of 78 percent the theoretical price reaches the price observed in the market. This implies that leveraged loans are currently traded with an implied recovery rate of merely 22 percent. In addition, this provides the answer as to why no liquidity premium is offered in the two most junior tranches. The implied recovery rate at which leveraged loans are currently being traded only affects the prices of the junior tranches insignificantly. This is due to their placement in the capital structure. With the actual recovery rate of 49.5 percent they are both almost entirely precluded from receiving recovery in the event of bankruptcy. Therefore a decrease in the implied recovery becomes without influence to the pricing of these tranches.

Effectively, we find that potential investors of senior secured leveraged loans are currently being offered a fairly substantial liquidity premium. This is tantamount to senior leveraged loan prices not currently reflecting the actual conditions of leveraged buyouts.

11. CONCLUSION

In the final chapter of the thesis, the main findings identified throughout the analysis will be drawn together in a conclusion. In compliance with the structure of the thesis, this is performed through a systematic assessment of the five analyses which finally leads to an answer of the main research question proposed in the problem statement.

The first part of the thesis has provided the reader with an understanding of the most fundamental characteristics of the leveraged loan market. Typically leveraged loans are issued by companies involved in leveraged buyouts. One of the main characteristics differentiating leveraged loans from more traditional high yield debt products is the way they are launched to the market. Instead of entering a series of bilateral arrangements with each bank, a group of banks share the same loan agreement. In this way private equity funds have been able to access larger pools of funding than otherwise available. Likewise, the syndicated loan market offers several advantages to banks according to their role in the syndicate. Especially the mandate as lead arranger became attractive due to recent years' pleasant market conditions. Acting more like investment banks, the battle of winning the mandate became more intense, resulting in increasingly aggressive loan structures. Consequently, a moral hazard problem arose between lead arrangers and other loan participants.

Looking at a typical capital structure of a leveraged buyout company it is apparent that it consists of a wide range of different debt products. According to their priority, the most common leveraged loans appear within the categories of senior, second lien and subordinated debt. Denoted as either first or second lien, the vast majority of loans are senior secured floating rate papers. Mezzanine loans are ranked as subordinated debt and are a direct alternative to high yield bonds. In consequence of being a highly leveraged company the issuers are restricted by comprehensive covenant packages which state how loose they can operate and carry themselves financially.

The second part of the thesis has introduced the reader to the fundamental CLO structure. In general, a CLO is a special purpose vehicle established to hold and manage a diversified pool of leveraged loans. To finance the purchase of these loans, the CLO issues a series of rated notes which are tranching according to priority. Created as an arbitrage vehicle the CLO generates equity returns through the issuance of debt several times its equity contribution. The utilisation of various credit enhancement techniques mitigates the risk associated with default in the

collateral pool and ensures that certain target ratings of the specific notes are achieved. Most remarkable in this relation is the payment waterfall which dictates the priority of payments accruing to investors of different tranches. This ensures that the claims of the higher rated tranches to interest and principal proceeds are protected. The latter implies that increasingly higher levels of subordinated capital provide protection against losses in the collateral pool. Effectively, the CLO structure enables the issuance of tranches with different interest rates and credit ratings. This has allowed for investments in leveraged loans to achieve investment-grade ratings which entailed that institutional investors could enter the leveraged loan market as the solvency burden associated with the lower rated leveraged loans was mitigated. Furthermore, institutional investors were offered the opportunity to invest in diversified portfolios of leveraged loans managed by experienced market participants. This made their limited expertise within the area redundant. From the perspective of banks, the CLO structure has provided them the opportunity to achieve off-balance financing while simultaneously generating fees from servicing the loans and remaining the corporate relationship bank.

Through an in-depth analysis of the European primary and the secondary leveraged loan market, it is clear that the increased institutional investor base have had major impacts on the evolution of the leveraged loan market. In the years preceding the credit crisis, the hyper liquid market conditions were attributed to a rapidly increasing institutional investor attention. Yet, besides stimulating the leveraged loan market in the bull-run the institutional investors also highly contributed to its total collapse.

The primary leveraged loan market has clearly been afflicted by the entrance of the credit crisis. The volume of loan issuance has abruptly stalled and previous years' hyper liquid market conditions seem far away. The structures of the few new transactions have improved significantly. First of all leverage has gone down as a result of increasing equity contributions. As a consequence purchase price multiples have fallen. Furthermore, the former years' increasing complex debt structures have changed to more transparent and classic senior/mezzanine capital structures. Finally, the shrunken investor base has forced spreads to rise.

Since the onset of the credit crisis in summer 2007, the secondary loan market has gone through a total meltdown and experienced a longer period of historically negative returns. A comprehensive deleveraging process among hedge funds and market value CLOs lead to a

vicious circle of forced selling and falling prices. Such technical factors affecting the market were later substituted with fundamental difficulties concurrently with the recession becoming ever more real. In a risk adverse world, filled with distressed investors, outlooks of rising default rates and low recovery rates pushed the market further in its knees. Starting above par during the summer 2007, the ELLI Index ended below 60 at end year 2008.

In the fourth part of the thesis the reader has been provided a thorough exposition of the theoretical framework for pricing corporate debt when tranced according to priority. The derivation of the model was initiated on the basis of theoretical work provided by Merton, Black & Scholes and Lando. This provided a theoretical framework for pricing sequentially tranced corporate debt when issued as zero-coupon bonds. With leveraged loans primarily issued as coupon bonds, we turned to the pricing theory provided by Leland. The original model of Leland for pricing corporate debt issued as coupon bonds was derived. Afterwards we extended the model to handle prioritised debt. The extension proved to accentuate the deterministic drawbacks of the model. In order to circumvent these, we found that the implementation of a binomial distribution with respect to the fraction lost to bankruptcy costs solved the problem. This enabled the model to return theoretical prices comparable with actual market prices.

The extensive knowledge obtained, regarding the leveraged loan market, enabled an examination of the theoretical results. The findings of our model implementation and the current conditions of the leveraged loan market form the foundation for a qualified answer to the main research question.

Can market prices of leveraged loans be supported from a theoretical point of view?

We find that no precise answer can be provided based on the finding throughout this thesis. The results related to the individual tranches are of an ambiguous character which makes a general answer to the main research question impossible.

The theoretical price of the EMTN tranche is affected by the model assumption of time independence which excludes this tranche as a foundation for comparison with actual market prices.

Generally seen, the market prices of the two most junior tranches appear to be supported from a theoretical point of view. We find that practical and theoretical issues might explain some of

the observed deviations between model and market prices identified. In particular, the results of the stress tests suggest that minor estimation flaws with respect to enterprise value and volatility could be present.

The theoretical obtained price of the senior tranche suggests that senior secured leveraged loans are currently traded at market prices which are too low. The difference between observed and theoretical prices of the senior tranche in the ISS case is more than 40 percent. This implies that neither theoretical nor practical factors are likely to explain this gap in prices. With the current condition of the leveraged loan market we believe that a liquidity premium reflects the existing difference.

These indications let to a calibration of the fraction lost to bankruptcy costs. The finding of which indicated an implied recovery rate of merely 22 percent is utilised in the market. In compliance with the knowledge obtained in the performed market analysis, this entails that a liquidity premium is being offered to potential senior secured leveraged loan investors. As a result of the credit crisis, the leveraged loan market has experienced a longer period of forced selling. In particular hedge funds and market value CLOs were heavily afflicted by a broader credit system that was severely overextended. The forced deleveraging process among these institutional investment vehicles, along with a rapidly contracting investor base, has created a significant supply/demand imbalance in the market. Severely influenced by technical factors, market prices of senior secured leveraged loans cannot be supported from a theoretical point of view.

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Appendix overview

Appendix A: Excess Spread	122
Appendix B: Volatility.....	123
Appendix C: Root Mean Squared Error.....	124
Appendix D: Binomial Distribution.....	125
Appendix E: Model Implementation.....	126
Appendix F: Stress Tests.....	127
Appendix G: Calibration.....	128

For a full review of all calculations please see attached CD-ROM

Appendix A: Excess Spread

Collateral return (LIBOR + 300 bps):	300 bps	300
Weighted average cost of debt capital : (50 bps on 92% of the capital structure)	46 bps	-46
Collateral management fees :	50 bps	-50
Fees and expences :	5 bps	-5
Credit losses : (2% defaults, 75% recoveries)	50 bps	-50
<hr/>		
Excess spread (the arbitrage) :		149

Appendix B: Volatility

2 month				1 month				2 weeks				1 week			
G4S	Sodexo	Compass	ISS												
2008				2008				2008				2008			
Historical volatility															
0,000336	0,000858	0,001214		0,000245	0,000543	0,000698		0,000163	0,000136	0,000399		0,000218	0,000126	0,000226	
Yearly std															
0,30	0,47	0,56		0,25	0,38	0,43		0,21	0,19	0,32		0,24	0,18	0,24	

29. marts 2005				29. marts 2005				29. marts 2005				29. marts 2005			
G4S	Sodexo	Compass	ISS												
Historical volatility															
0,000203	0,000183	0,000060	0,000055	0,000166	0,000167	0,000038	0,000037	0,000136	0,000147	0,000035	0,000020	0,000135	0,000188	0,000027	0,000004
Yearly std															
0,23	0,22	0,13	0,12	0,21	0,21	0,10	0,10	0,19	0,20	0,10	0,07	0,19	0,22	0,08	0,03

Appendix C: Root Mean Squared Error

G4S	Sodexo	Compass	ISS
2008			
2 month			
0,0003715	0,0007086	0,0014912	
1 month			
0,0003741	0,0006993	0,0014935	
2 weeks			
0,0003787	0,0007041	0,0006815	
1 week			
0,0003812	0,0007328	0,0008309	
G4S	Sodexo	Compass	ISS
29. marts 2005			
2 month			
0,0002849	0,0005559	0,0027193	0,0001279
1 month			
0,0003164	0,0005425	0,0026540	0,0001280
2 weeks			
0,0003349	0,0005497	0,0008454	0,0001290
1 week			
0,0003492	0,0005614	0,0011655	0,0001344

Appendix D: Binomial Distribution

Recovery	Fraction
(s) = 0,22	(f) = 0,78

4 trials																
u	ssss	sssf	ssfs	ssff	sfss	sfsf	sffs	sfff	fsss	fssf	fsfs	fsff	ffss	ffsf	fffs	ffff
P(u)	0,002343	0,008305	0,008305	0,029447	0,008305	0,0294466	0,029447	0,104401	0,008305	0,029447	0,029447	0,104401	0,029447	0,104401	0,104401	0,370151

5 trials						
u	5*s	4*s	3*s	2*s	1*s	0*s
P(u)	0,000515	0,001827	0,006478	0,022968	0,081433	0,2887174
Occurrence	1	5	10	10	5	1
Acc prob	0,000515	0,009136	0,064782	0,229683	0,407166	0,2887174

Appendix E: Model Implementation

ISS Debt Structure 31/12/2008							
Facility	Principal MDKK	Percentage of Total Debt	x EBITDA 2008 PF	Base Rate	Cash Margin	Cash Coupon	Coupon Payment
Senior	17,591	53,96%	3.6x	2,894%	2,375%	5,269%	926,83
EMTN	7,155	21,95%	1.5x	0,000%	4,750%	4,750%	339,86
Second Lien	4,471	13,71%	0.9x	2,894%	4,500%	7,394%	330,57
Senior Sub Notes	3383	10,38%	0.7x	0,000%	8,875%	8,875%	300,24
Total Cash Pay Debt	32,600	100%	6,7x	1,958%	3,862%	5,821%	1897,50

Estimated and obtained values	
Enterprise Value (V)	39,492
Volatility (σ)	0,220
Fraction lost to Bankruptcy (α)	0,505
Tax Rate (τ)	0,115
Riskless Rate (r)	0,034
Constant Base Rate (LIBOR 3)	0,029

Price Calculation in Various Scenarios												
Facility	Principal MDKK	Price when $\alpha = 0$	Price when $\alpha = 0.1$	Price when $\alpha = 0.2$	Price when $\alpha = 0.3$	Price when $\alpha = 0.4$	Price when $\alpha = 0.5$	Price when $\alpha = 0.6$	Price when $\alpha = 0.7$	Price when $\alpha = 0.8$	Price when $\alpha = 0.9$	Price when $\alpha = 1.0$
Senior	54%	112,98	112,98	112,98	112,98	112,98	107,38	93,22	79,07	64,92	50,76	36,61
EMTN	21%	109,38	109,38	109,38	88,82	54,02	33,00	33,00	33,00	33,00	33,00	33,00
Second Lien	14%	127,75	127,75	74,16	51,37	51,37	51,37	51,37	51,37	51,37	51,37	51,37
Senior Sub	11%	138,04	64,44	61,66	61,66	61,66	61,66	61,66	61,66	61,66	61,66	61,66
Total	1											

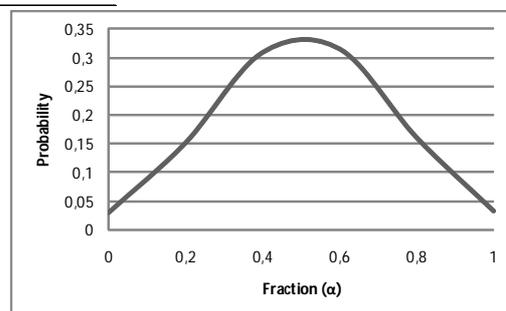
EURIBOR
0,0289375

Binomial Distribution					
0,0297184	0,151594058	0,30931313	0,3155619	0,16096843	0,0328441
0,030	0,152	0,309	0,316	0,161	0,033

Prices According to the Probability of Achieved Recovery							Total Price
Facility	Price when $\alpha = 0$ probability 0.03	Price when $\alpha = 0.2$ probability 0.15	Price when $\alpha = 0.4$ probability 0.31	Price when $\alpha = 0.6$ probability 0.32	Price when $\alpha = 0.8$ probability 0.16	Price when $\alpha = 1.0$ probability 0.03	
Senior	3,36	17,13	34,95	29,42	10,45	1,20	97
EMTN	3,25	16,58	16,71	10,41	5,31	1,08	53
Second Lien	3,80	11,24	15,89	16,21	8,27	1,69	57
Senior Sub	4,10	9,35	19,07	19,46	9,93	2,03	64
Total							

Prices		
Facility	Market Price	Model Price
Senior	67	97
EMTN	84	53
Second Lien	55	57
Senior Sub	60	64

Probability Distribution						
Fraction (α)	0	0,2	0,4	0,6	0,8	1
Probability	0,03	0,15	0,31	0,32	0,16	0,03



Appendix F: Stress Tests

ISS Debt Structure 31/12/2008							
Facility	Principal	Percentage	x EBITDA	Base Rate	Cash	Cash	Coupon
Senior	17.591	53,96%	3.6x	2.894%	2,375%	5,269%	926,83
EMTN	7.155	21,95%	1.5x	0,000%	4,750%	4,750%	339,86
Second Lien	4.471	13,71%	0.9x	2.894%	4,500%	7,394%	330,57
Senior Sub	3.383	10,38%	0.7x	0,000%	8,875%	8,875%	300,24
Total Cash Pay Debt	32.600	100%	6,7x	1,958%	3,862%	5,821%	1897,50

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0,0289375

Price Calculation in Various Scenarios												
Facility	Principal MDKK	Price when $\alpha = 0$	Price when $\alpha = 0.1$	Price when $\alpha = 0.2$	Price when $\alpha = 0.3$	Price when $\alpha = 0.4$	Price when $\alpha = 0.5$	Price when $\alpha = 0.6$	Price when $\alpha = 0.7$	Price when $\alpha = 0.8$	Price when $\alpha = 0.9$	Price when $\alpha = 1.0$
Senior	17.591	112,98	112,98	112,98	112,98	112,98	112,98	112,98	112,98	112,98	112,98	112,98
EMTN	7.155	109,38	109,38	109,38	109,38	109,38	109,38	109,38	109,38	109,38	109,38	109,38
Second Lien	4.471	127,75	127,75	127,75	127,75	127,75	127,75	127,75	127,75	127,75	127,75	127,75
Senior Sub	3.383	138,04	138,04	138,04	138,04	138,04	138,04	138,04	138,04	138,04	138,04	138,04
Total	32.600											
		0,00	0,01	0,06	0,23	0,41	0,29					

Prices According to the Probability of Achieved Recovery								
Facility	Principal	Price	Price	Price	Price	Price	Price	Total
Senior	17.591	0,06	1,03	7,32	25,95	46,00	32,62	113
EMTN	7.155	0,06	1,00	7,09	25,12	44,54	31,58	109
Second Lien	4.471	0,07	1,17	8,28	29,34	52,01	36,88	128
Senior Sub	3.383	0,07	1,26	8,94	31,71	56,21	39,85	138
Total	32.600							

Estimated and obtained values	
Enterprise Value (V)	39.492
Volatility (σ)	0.22
Fraction lost to Bankruptcy (α)	0.3
Tax Rate (τ)	0.115
Riskless Rate (r)	0.034
Constant Base Rate (LIBOR 3)	0,02894

Facility	Volatility Stress Test				
	-10%	-5%	0%	5%	10%
Senior	100	98	97	95	94
EMTN	59	56	53	51	49
Second Lien	67	62	57	53	49
Senior Sub	76	70	64	59	54

Facility	Fraction lost to Bankruptcy costs Stress Test				
	-10%	-5%	0%	5%	10%
Senior	100	98	97	94	92
EMTN	59	56	53	51	48
Second Lien	60	58	57	56	55
Senior Sub	65	65	64	63	63

Facility	Enterprise Value Stress Test				
	-10%	-5%	0%	5%	10%
Senior	87	92	97	100	104
EMTN	40	47	53	59	64
Second Lien	32	45	57	68	77
Senior Sub	32	49	64	77	89

Prices		
Facility	Market Price	Model Price
Senior	67	113
EMTN	84	109
Second Lien	55	128
Senior Sub	60	138

Facility	Volati #	-10%		-5%		0%		5%		10%					
		EV	Alpha	Volatility	EV	Alpha	Volatility	EV	Alpha	Volatility	EV	Alpha			
Senior	#	87	100	98	92	98	97	97	97	95	100	94	104	92	
EMTN	#	40	59	56	47	56	53	53	53	51	59	51	49	64	48
Second Lien	#	32	60	62	45	58	57	57	57	53	68	56	49	77	55
Senior Sub	#	32	65	70	49	65	64	64	64	59	77	63	54	89	63

Appendix G: Calibration

ISS Debt Structure 31/12/2008						
Facility	Principal MDKK	Percentage of Total Debt	x EBITDA 2008 PF	Base Rate	Cash Margin	Coupon Payment
Senior	17.591	53,96%	3.6x	2,894%	2,375%	926,83
EMTN	7.155	21,95%	1.5x	0,000%	4,750%	339,86
Second Lien	4.471	13,71%	0.9x	2,894%	4,500%	330,57
Senior Sub Notes	3.383	10,38%	0.7x	0,000%	8,875%	300,24
Total Cash Pay Debt	32.600	100%	6,7x	1,958%	3,862%	1897,50

Estimated and obtained values	
Enterprise Value (V)	39,492
Volatility (σ)	0,22
Fraction lost to Bankruptcy (α)	0,3
Tax Rate (τ)	0,115
Riskless Rate (r)	0,034
Constant Base Rate (LIBOR 3)	0,02894

Price Calculation in Various Scenarios											
Facility	Principal MDKK	Price when $\alpha = 0$	Price when $\alpha = 0.1$	Price when $\alpha = 0.2$	Price when $\alpha = 0.3$	Price when $\alpha = 0.5$	Price when $\alpha = 0.6$	Price when $\alpha = 0.7$	Price when $\alpha = 0.8$	Price when $\alpha = 0.9$	Price when $\alpha = 1.0$
Senior	17.591	112,98	112,98	112,98	112,98	112,98	112,98	112,98	112,98	112,98	112,98
EMTN	7.155	109,38	109,38	109,38	109,38	109,38	109,38	109,38	109,38	109,38	109,38
Second Lien	4.471	127,75	127,75	127,75	127,75	127,75	127,75	127,75	127,75	127,75	127,75
Senior Sub	3.383	138,04	138,04	138,04	138,04	138,04	138,04	138,04	138,04	138,04	138,04
Total	32.600										

Results of changes in the Binomial Distribution

0,00	0,01	0,06	0,23	0,29
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0,0289375

Prices According to the Probability of Achieved Recovery							
Facility	Principal MDKK	Price when $\alpha = 0$ probability	Price when $\alpha = 0.2$ probability	Price when $\alpha = 0.4$ probability	Price when $\alpha = 0.6$ probability	Price when $\alpha = 1.0$ probability	Total Price
Senior	17.591	0,06	1,03	7,32	25,95	32,62	113
EMTN	7.155	0,06	1,00	7,09	25,12	31,58	109
Second Lien	4.471	0,07	1,17	8,28	29,34	36,88	128
Senior Sub	3.383	0,07	1,26	8,94	31,71	39,85	138
Total	32.600						

Facility	Calibration of Fraction lost to Bankruptcy Cost					Market Price
	50%	60%	70%	78%	80%	
Senior	97	88	77	67	64	67
EMTN	53	44	38	35	35	84
Second Lien	57	54	52	52	52	55
Senior Sub	64	62	62	62	62	60

Prices		
Facility	Market Price	Model Price
Senior	67	113
EMTN	84	109
Second Lien	55	128
Senior Sub	60	138